

The Decision to Move House and Aggregate Housing-Market Dynamics*

L. Rachel Ngai[†]

London School of Economics

Kevin D. Sheedy[‡]

London School of Economics

29th June 2016

Abstract

Using data on house sales and inventories, this paper shows that housing-market dynamics are driven mainly by listings and less so by transaction speed, thus the decision to move house is key to understanding the housing market. The paper builds a model where moving house is essentially an investment in match quality, implying that moving depends on macroeconomic developments and housing-market conditions. The endogeneity of moving means there is a cleansing effect — those at the bottom of the match quality distribution move first — which generates overshooting in aggregate variables. The model is applied to the 1995–2004 housing-market boom.

JEL CLASSIFICATIONS: D83; E22; R31.

KEYWORDS: housing market; search and matching; endogenous moving; match quality investment.

*We are grateful to Johannes Boehm, Adam Guren, Allen Head, Yannis Ioannides, Boyan Jovanovic, Steven Laufer, Kurt Mitman, Chris Pissarides, Morten Ravn, Richard Rogerson, and Rob Shimer for helpful comments. We thank Lucy Canham, Thomas Doyle, and Lu Han for providing data. We also thank seminar participants at Atlanta Fed, Bank of Canada, Bank of England, U. Bern, Boston U., CREI, EUI, GWU-FRB Real Estate Seminar, U. Helsinki, U. Hong Kong, IIES, U. Louvain, U. Mannheim, Norwegian Business School, São Paulo School of Economics, Southwest U. of Finance and Economics, Stockholm School of Economics, Sveriges Riksbank, Trinity College Dublin, UCL, the Anglo-French-Italian macroeconomics workshop, Conference on Research on Economic Theory and Econometrics (2014), ESSIM 2015, HULM 2015 — St. Louis, Midwest Macro Meeting (Fall 2013), NBER Summer Institute 2015, Search and Matching Network annual conference (2014), and SED (2014) for their comments. Rachel Ngai acknowledges support from the British Academy Mid-Career Fellowship. This paper was previously circulated under the title ‘Moving House’.

[†]LSE, CEPR, and CfM. Email: L.Ngai@lse.ac.uk

[‡]LSE, CEPR, and CfM. Email: K.D.Sheedy@lse.ac.uk

1 Introduction

The number of transactions in the housing market is a widely watched statistic with implications for many sectors of the economy. The U.S. in particular has seen a dramatic rise and fall of transactions in recent decades. The number of transactions is jointly determined by how quickly houses come off the market and how quickly they come on to the market. How quickly houses come off the market depends on a time-consuming and costly search process for buyers and sellers. On the other hand, how quickly houses come on to the market depends on the decisions of homeowners to put a house up for sale as well as changes in the housing stock.

The first contribution of this paper is to present evidence establishing that the main driver of transactions is changes in how frequently houses come on to the market. Furthermore, U.S. data imply that the dominant factor in explaining the number of houses coming on to the market is homeowners' decisions to move house, rather than changes in the housing stock. Following on from this, understanding the decision to move house is crucial for explaining changes in transactions. The second contribution of the paper is to build a model of moving house. The model is based on the idea that moving house constitutes an investment in the quality of the match between a homeowner and a particular house. Such a model where moving house is endogenous is necessary to think about how the aggregate moving rate might be affected by macroeconomic and policy variables such as interest rates and taxes.¹ Finally, the model is calibrated to the U.S. economy to study the housing-market boom.

The claim that the moving rate of homeowners is of much greater importance for transactions than the selling rate of houses on the market can be understood with some minimal empirical discipline combined with a basic stock-flow accounting identity. Compared to the average time spent in a house (more than a decade), the average time taken to sell a house is very short (a few months). This means the average sales rate is around twenty to thirty times higher than the average moving rate, and the stock of houses for sale is about twenty to thirty times smaller than the stock of occupied houses. An increase in the sales rate with no change in the moving rate would rapidly deplete the stock of houses for sale leaving little overall impact on transactions. On the other hand, an increase in the moving rate adds to the stock of houses for sale, which increases transactions even with no change in the sales rate.

Using data on sales and inventories of existing single-family homes from the National Association of Realtors (NAR), this paper is the first to construct a time series for listings (houses put up for sale) and to calculate the associated listing rates. This provides an estimate of homeowners' moving rates. Furthermore, this paper also calculates the selling rates of houses on the market using a measure of inventories that reflects the actual number of houses available for sale, as opposed to the usual approach of taking the number of vacant houses for sale.

A counterfactual exercise using U.S. data confirms the claim that the moving rate is the dominant factor in explaining changes in transactions. The counterfactual exercise considers the number of

¹The implication that interest rates have a negative impact on mobility is consistent with the empirical evidence presented by [Quigley \(1987\)](#) and [Ferreira, Gyourko and Tracy \(2010\)](#).

transactions that would have occurred if the moving rate were constant at its average value while the sales rate varied as in the data. This hypothetical sales series fails to capture any of the major movements in actual transactions. On the other hand, if the sales rate were held constant at its average value while the moving rate and the housing stock varied as in the data, the hypothetical transactions series tracks closely the main changes in actual transactions. Finally, if both the sales rate and moving rate were held constant at their average values while the housing stock varied as in the data, the hypothetical series captures less than a third of the rise in transactions during the boom and almost none of the collapse during the bust. Since changes in the owner-occupied housing stock (including those for sale) can occur either through new construction or houses switching from being rented to being owner occupied, this counterfactual exercise reveals the limited role played by the construction boom and the rise in the homeownership rate in accounting for the boom in transactions.²

To understand what might drive changes in the moving rate, this paper presents a search-and-matching model of endogenous moving. Central to the model is the idea of match quality: the idiosyncratic values homeowners attach to the house they live in. This match quality is a persistent variable subject to occasional idiosyncratic shocks, representing life events such as changing jobs, marriage, divorce, and having children.³ These shocks degrade existing match quality, following which homeowners decide whether to move. Eventually, after sufficiently many shocks, current match quality falls below a ‘moving threshold’ that triggers moving to a new house and a renewal of match quality.

Moving house is a process with large upfront costs that is expected to deliver long-lasting benefits, and is thus sensitive to macroeconomic and policy variables such as interest rates and taxes that influence other investment decisions. These variables affect the threshold for existing match quality that triggers moving. Thus, while idiosyncratic shocks are the dominant factor in moving decisions at the individual level, changes in the moving threshold lead to variation in the aggregate moving rate. In contrast, in a model of exogenous moving, the aggregate moving rate is solely determined by the arrival rate of an idiosyncratic shock that forces moving.

The endogeneity of moving generates new transitional dynamics that are absent from models imposing exogenous moving. Endogenous moving means that those who choose to move are not a random sample of the existing distribution of match quality: they are the homeowners who were only moderately happy with their match quality. Together with the persistence over time of existing match quality, endogenous moving thus gives rise to a ‘cleansing effect’. An aggregate shock that changes the moving threshold leads to variation in the degree of cleansing of lower-quality matches. Since match quality is a persistent variable, more cleansing now leads to less cleansing in the future, which implies overshooting of the moving rate and other housing-market variables.

The modelling of the buying and selling process for houses on the market is close to the existing

²The homeownership rate, as defined in the Census, is the stock of owner-occupied homes divided by the stock of all occupied homes (including those that are rented).

³These are the main reasons for moving according to the American Housing Survey. Match quality is modelled as a persistent variable because there are many dimensions to what is considered a desirable house, and a life event will typically affect some but not all of those dimensions.

literature. There are search frictions in the sense that time is needed to view houses, and viewings are needed to know what idiosyncratic match quality would be in a particular house. Buyers and sellers face transaction costs and search costs. There is a ‘transaction threshold’ for match quality above which a buyer and a seller agree to a sale. The housing-market equilibrium is characterized by the moving threshold and the transaction threshold, and together with the distribution of existing match quality, these thresholds determine the sales and moving rates, and inflows to and outflows from the stock of houses for sale.

The model is applied to study the U.S. housing market in the decade from 1995 to 2004, which is noteworthy as a period of booming activity. Using NAR data, three stylized facts emerge during those years: transactions rise, houses are selling faster, and houses are put up for sale more frequently. The increase in the listing rate is consistent with the independent empirical finding by [Bachmann and Cooper \(2014\)](#) of a substantial rise in the own-to-own moving rate using household-level PSID data.⁴

The 1995–2004 period featured a number of developments in the U.S. that have implications for moving decisions according to the model. To name a few of these: the post-1995 surge in productivity growth, the rise of internet-based property search, and cheaper and more easily accessible credit. These developments are represented in the model by changing parameters, and the model is solved analytically to conduct a series of comparative statics exercises. These illustrate the interpretation of moving house as an investment in match quality, and how incentives to invest are affected by macroeconomic conditions and changes in the housing market.

The implication of the model is that all three developments unambiguously increase the moving rate. This rise in the moving rate works through a higher moving threshold. An increase in productivity growth raises income and increases the demand for housing, which raises the marginal benefit of a better match. This increases the incentive to move to a house with a higher match quality. The adoption of internet technology reduces search frictions, making it cheaper for homeowners to move in order to invest in a better match. Finally, lower mortgage rates, interpreted as a fall in the rate at which future payoffs are discounted, create an incentive to invest in improving match quality because the capitalized cost of moving is reduced.

The parameters of the model are calibrated to match the U.S. housing market. More specifically, the cost parameters match data on transaction costs, search costs, and maintenance costs; while the other four key parameters determining housing-market turnover match the expected duration of a new match, the average time home-owners have owned their homes, the number of viewings per sale, and the average time-to-sell. The baseline result is that the three developments together imply a 31% rise in the moving rate in the short run and a 15% rise in the long run, which accounts for a substantial fraction of the rise in the empirical moving rate during the boom. There is a considerable amount of overshooting due to the cleansing of the match quality distribution, and this continues for around a decade. The model can thus generate large and long-lasting changes in transactions as

⁴At first sight, the rise in the listing rate might seem inconsistent with the long-run decline in the U.S. mobility rate. [Bachmann and Cooper \(2014\)](#) show that the declining mobility rate is accounted for by a fall in the rent-to-rent moving rate.

observed in the data. While it would be possible to match the change in transactions in a model of exogenous moving simply by considering an exogenous shock to the moving rate, that model would predict falling house prices at a time of rising transactions.

There is a large literature (starting from [Wheaton, 1990](#), and followed by many others) that studies frictions in the housing market using a search-and-matching model as done here. See, for example, [Albrecht, Anderson, Smith and Vroman \(2007\)](#), [Anenberg and Bayer \(2013\)](#), [Caplin and Leahy \(2011\)](#), [Coles and Smith \(1998\)](#), [Díaz and Jerez \(2013\)](#), [Krainer \(2001\)](#), [Head, Lloyd-Ellis and Sun \(2014\)](#), [Moen, Nenov and Sniekers \(2014\)](#), [Ngai and Tenreyro \(2014\)](#), [Novy-Marx \(2009\)](#), [Piazzesi and Schneider \(2009\)](#), [Piazzesi, Schneider and Stroebel \(2015\)](#), and the survey by [Han and Strange \(2014\)](#).⁵ The key contribution of this paper to the literature is in studying moving house and showing its importance in understanding the dynamics of transactions. Moving is exogenous in the earlier papers with the exception of [Guren \(2014\)](#) and [Hedlund \(2013\)](#), but those papers are about price fluctuations and foreclosures.⁶

While much of the existing literature has focused on house prices, there are at least two reasons to think that number of transactions in the housing market is a more informative statistic than house prices. At a fundamental level, each transaction leads to a reallocation of the housing stock with gains from trade for both the buyer and the seller. On the other hand, house prices are a transfer related to how the surplus is divided between the parties. While falling prices may be associated with a smaller surplus to share, falling transactions more directly signify that there are fewer positive-surplus trades to be made. For example, as depicted in [Figure 1](#), between the final quarter of 2005 and 2007, a much more accurate picture of the gains from trade in the housing market is given by the sharply falling transactions not the still-rising prices. Understanding transactions is therefore essential to knowing how the housing market affects welfare.

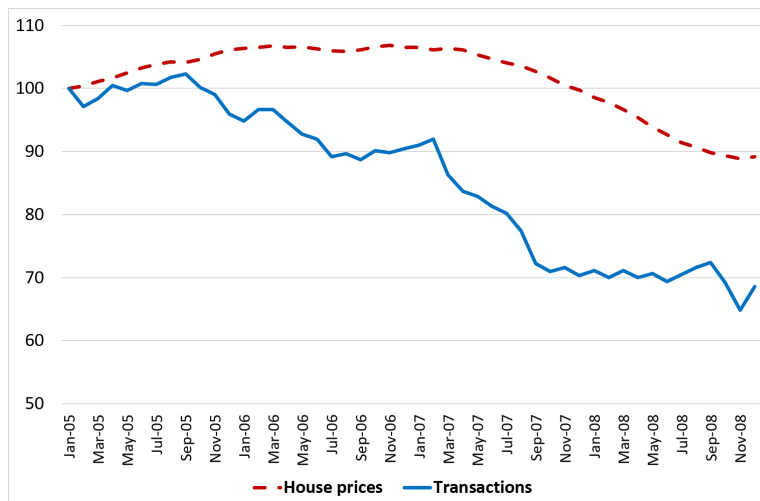
Moreover, house-price indices are averages of prices only for those houses that are actually sold. If there is a deterioration in housing-market conditions that means some transactions would now not have a positive surplus, these transactions will not occur and the loss of surplus will not show up in a house-price index — but will be observed through lower volumes. Consider two scenarios. First, house prices are unchanged, but transactions drop by a third. Second, transactions are unchanged, but house prices fall by 10%. Clearly, the first scenario indicates a greater deterioration in housing-market conditions. As seen in [Figure 1](#), these two scenarios essentially describe the state of the U.S. housing market between 2005 and 2007, and from 2007 to 2008, respectively. The deterioration in the housing market is apparent from the final quarter of 2005 when looking at the transactions series, long before house prices show any significant fall.

The plan of the paper is as follows. [Section 2](#) uses NAR data to substantiate the claim that changes in the listing rate are the key determinant of housing-market dynamics. [Section 3](#) presents the model of endogenous moving, and [section 4](#) solves for the equilibrium analytically. [Section 5](#) calibrates the model to study developments in the U.S. economy that can help understand the

⁵See [Davis and Van Nieuwerburgh \(2014\)](#) for a survey of housing and business cycles, including models without search frictions.

⁶[Karahan and Rhee \(2013\)](#) use a similar framework to [Hedlund \(2013\)](#) and study when a homeowner chooses to move to another region to look for a job.

Figure 1: *Transactions and house-price indices*



Notes: Monthly data (January 2005–December 2008), rebased to January 2005 = 100. The house-price series is deflated by the PCE price index.

Sources: Transactions, National Association of Realtors seasonally-adjusted single-family home sales; House prices, FHSA purchase-only seasonally-adjusted price index.

1995–2004 housing-market boom. [Section 6](#) concludes.

2 The importance of changes in the moving rate

The existing literature on housing markets has focused mainly on the decision processes of buyers and sellers that lead to sales of houses on the market. This section presents evidence showing that the decision of homeowners to put their houses up for sale is important not only for understanding the behaviour of listings, but is also crucial for understanding aggregate housing-market dynamics.

2.1 The basic idea

It is possible to grasp the relative importance of changes in sales and listing rates with some minimal empirical discipline combined with a basic stock-flow accounting identity.

A stock-flow accounting identity is a natural starting point when thinking about any market with search frictions:

$$\dot{U}_t = n(K_t - U_t) - sU_t,$$

where U_t is the number of existing houses for sale, \dot{U}_t is the derivative of U_t with respect to time t , K_t is the stock of owner-occupied houses (including those for sale), s is the rate at which houses for sale are sold, and n is the rate at which homeowners decide to move. The variable U_t is defined as existing houses for sale (excluding newly constructed houses for sale) to make it consistent with the

data from NAR used below. The number of transactions is sU_t . The growth rate of K_t is denoted by g , where changes in K_t are due to newly constructed houses being bought by owner-occupiers or existing houses switching from being rented to being owner occupied. The term $n(K_t - U_t)$ is the number of existing houses put on the market for sale.

Let u_t denote existing houses for sale as a fraction of the total housing stock, which satisfies the following equation:

$$\dot{u}_t = n(1 - u_t) - (s + g)u_t. \quad [2.1]$$

Given the flow rates s , n , and g , there is a steady state for the fraction of houses for sale:

$$u = \frac{n}{n + s + g},$$

and transactions S_t when u_t is at its steady-state value are:

$$S_t = \frac{sn}{s + n + g}K_t. \quad [2.2]$$

Convergence to the steady state for u_t occurs at rate $s + n + g$ (the coefficient of u_t in 2.1), and given that houses sell relatively quickly (a few months on average), s is large enough that transitional dynamics are of limited importance. Therefore, understanding the evolution of transactions over any period of time longer than a few months is mainly a question of understanding how changes in s , n , g , and K_t affect equation (2.2). The total derivative of transactions S_t is:

$$\frac{dS_t}{S_t} = \frac{s + g}{s + n + g} \frac{dn}{n} + \frac{n + g}{s + n + g} \frac{ds}{s} - \frac{g}{s + n + g} \frac{dg}{g} + \frac{dK_t}{K_t}. \quad [2.3]$$

This implies the relative size of the effects on transactions of a one percent change in n and a one percent change in s depends on the ratio of the sales rate s to the moving rate n , given that g is rather small empirically. Any change in the level of K_t has a proportional effect on transactions.

The average time taken to sell a house is $1/s$, and the average time homeowners spend living in a house is $1/n$. The impact of a change in the moving rate relative to the same proportional change in the sales rate is therefore related to the ratio of the average time spent in a house to the average time to sell. The former is more than a decade and the latter is a few months, suggesting s is around 300%, n is about 10%, and the ratio of the two is approximately 30. Any plausible value of g would be far smaller than $s + n$. Since this means $(n + g)/(s + n + g)$ is very small, huge changes in sales rates would be required to have any significant lasting effect on transactions.

Intuitively, with no change in the moving rate, the stock of houses for sale would be rapidly depleted by faster sales, leaving overall transactions only very slightly higher. On the other hand, since $(s + g)/(s + n + g)$ is close to one, changes in the moving rate can have a large and lasting impact on transactions. This is because even if the moving rate increased slightly, as the stock of potential movers is so large relative to the stock of houses for sale (the ratio $(1 - u)/u$ is equal to $(s + g)/n$), this can have a sustained impact on the number of homeowners who move.

This simple exercise establishes that any attempt to understand sustained changes in transactions through changes in the sales rate will founder. This leaves two potential explanations: changes in the moving rate, or changes in the housing stock. The next section uses U.S. data to show that changes in the housing stock contribute relatively little to understanding transactions compared to changes in the moving rate.

2.2 Empirical evidence

A quantitative analysis of stocks and flows in the housing market can be performed by using data on transactions and inventories of unsold houses to construct a measure of new listings (the number of houses put up for sale). NAR provides monthly estimates of transactions during each month and inventories of houses for sale at the end of each month for existing homes including single-family homes and condominiums.⁷ The NAR data on transactions and inventories are for existing homes, so sales of newly constructed houses are excluded. The focus here is on data for single-family homes, which represent around 90% of total sales of existing homes. Monthly data on transactions and inventories covering the period from January 1989 to June 2013 are first deseasonalized.⁸ The data are then converted to quarterly series to smooth out excessive volatility owing to possible measurement error. Quarterly transactions are the sum of the monthly transaction numbers, and quarterly inventories are the level of inventories at the beginning of the first month of a quarter.

Let N_t denote the inflow of houses that come on to the market during quarter t (new listings), and let S_t denote transactions (the outflow from the market) during that quarter. If I_t denotes the beginning-of-quarter t inventory (or end-of-quarter $t - 1$) then the stock-flow accounting identity is:

$$N_t = I_{t+1} - I_t + S_t. \tag{2.4}$$

A quarterly listings series N_t is constructed that satisfies the accounting identity above.⁹ Assuming inflows N_t and outflows S_t both occur uniformly within a time period, the average number of houses U_t available for sale during quarter t is equal to:

$$U_t = I_t + \frac{N_t}{2} - \frac{S_t}{2} = \frac{I_t + I_{t+1}}{2}. \tag{2.5}$$

Since the time series for inventories I_t is quite persistent, the measure U_t of the number of houses for sale turns out to be highly correlated with inventories (the correlation coefficient is equal to 0.99). This way of measuring of houses for sale is an improvement on the usual measure based on the ‘vacant for sale’ series from the American Housing Survey (AHS) because the most houses for

⁷The methodology and recent data are available at <http://www.realtor.org/research-and-statistics/housing-statistics>.

⁸Multiplicative monthly components are removed from the data.

⁹It is possible that listings as measured this way do not perfectly correspond to moving because S_t and I_t include non-owner-occupied houses, and because unsold houses might be withdrawn from sale. Both issues are addressed in [appendix A.1](#).

sale are not actually vacant (on average, ‘vacant for sale’ is less than half of inventories). More importantly, there is considerable variation over time in the ratio between ‘vacant for sale’ and inventories. Using the constructed series U_t for houses for sale, the sales rate is $s_t = S_t/U_t$.

The listing rate n_t is defined as the ratio of new listings N_t to the stock of owner-occupied houses not already for sale, that is, $n_t = N_t/(K_t - U_t)$. The housing stock K_t is defined as the stock of single-family homes excluding renter-occupied houses and homes for rent.¹⁰ These data are available only at a biennial frequency, so linear interpolation is used to produce a quarterly series. Figure 2 plots transactions, listings, houses for sale, and the total housing stock in the upper panel, and the sales and listing rates and the fraction of houses for sale in the lower panel. All series are plotted as differences in log points relative to the first quarter of 1989.

The figure shows that both the sales rate and the listing rate rise and fall with transactions. At first sight, the rise in the listing rate between 1993 and 2007 might seem inconsistent with the long-run decline in the U.S. mobility rate. Empirical work by Bachmann and Cooper (2014) has shown that the declining mobility rate is accounted for by a fall in the rent-to-rent moving rate, while they find that the own-to-own moving rate actually rises over this period.¹¹

A simple counterfactual exercise is used to quantify the importance of the listing rate in understanding changes in housing-market activity. Given that convergence to the steady state in equation (2.2) occurs within a few months, the evolution of transactions over time can be understood through the lens of the following equation:

$$S_t^* = \frac{s_t n_t}{s_t + n_t + g_t} K_t, \quad [2.6]$$

where s_t and n_t are the empirical sales and listing rates and $g_t = (K_t - K_{t-1})/K_{t-1}$ is the growth rate of the housing stock. The variable S_t^* is what the steady-state transactions volume would be at each point in time given the (time-varying) sales and listing rates and the housing stock. The correlation between S_t^* and actual transactions S_t is very high (the correlation coefficient is 0.90), which is not surprising given that convergence to the steady-state fraction of unsold houses is fast.

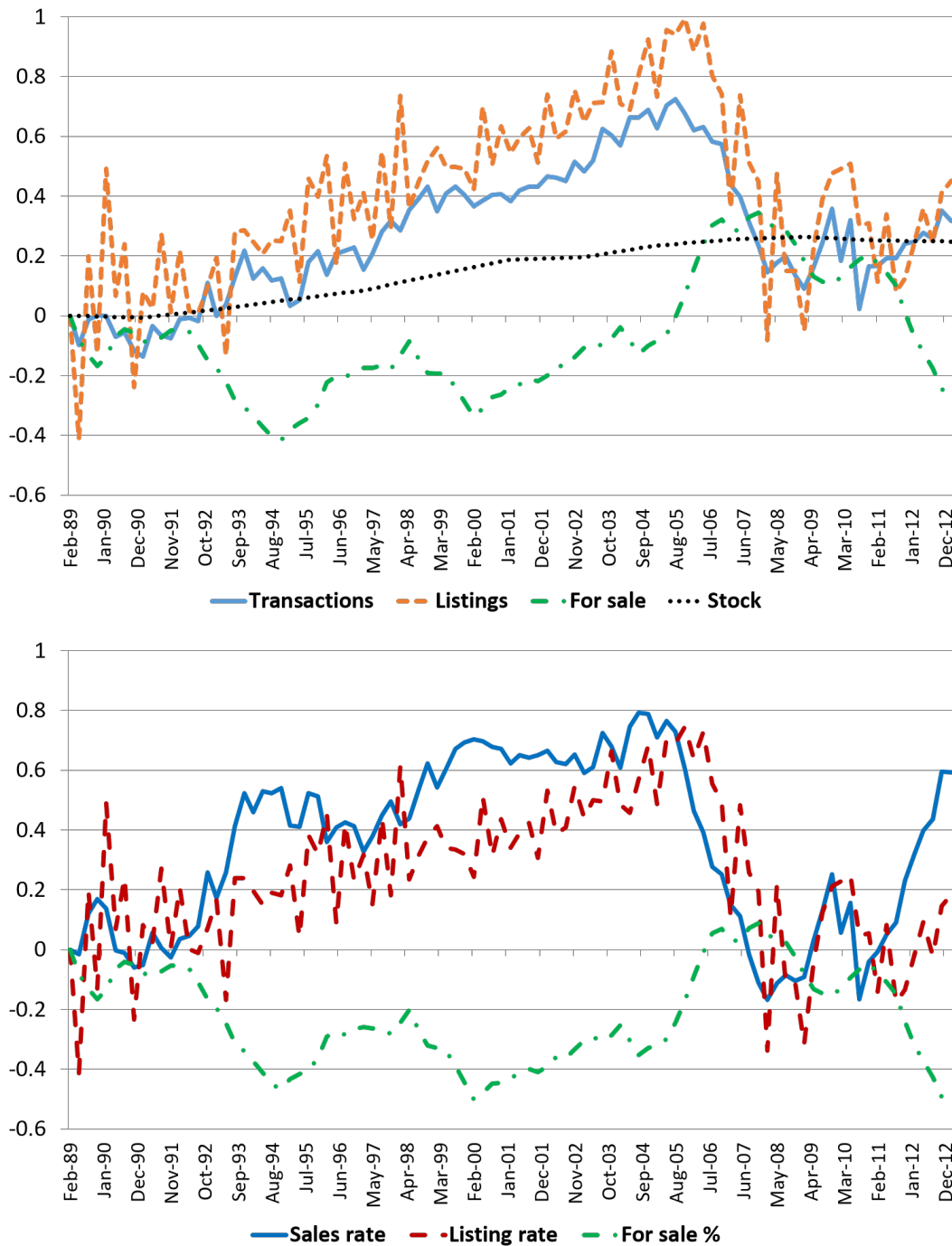
To see the relative importance of the sales rate, the listing rate, and the housing stock, consider what (2.6) would be in turn if the sales rate were held constant, the listing rate were held constant, and both rates were held constant (with g_t and K_t varying as in the data in all cases):

$$S_{n,t}^* = \frac{\bar{s} n_t}{\bar{s} + n_t + g_t} K_t, \quad S_{s,t}^* = \frac{s_t \bar{n}}{s_t + \bar{n} + g_t} K_t, \quad \text{and} \quad S_{g,t}^* = \frac{\bar{s} \bar{n}}{\bar{s} + \bar{n} + g_t} K_t,$$

¹⁰The housing stock is the sum of one-unit structures in the ‘owner occupied’, ‘vacant for sale’, and ‘vacant, but rented or sold’ categories of Table 1A–1 in the AHS. The third category is included because it is likely houses that are sold are the dominant component of that category. In any case, the third category is tiny compared to the first two.

¹¹Bachmann and Cooper (2014) use an approach similar to many studies of the labour market to compute transition rates between and within the renter-occupied and owner-occupied segments of the housing market using data from the PSID. As shown in their Figure 13, the own-to-own moving rate rises by approximately 30% during the period considered here. Moreover, they point out that the CPS data used by most studies of mobility do not include information on households’ previous tenancy status, so they cannot be used to compute disaggregated moving rates. They show that their aggregate moving rate is comparable to those derived from CPS data, suggesting that the disaggregated moving rates they computed using PSID data are a good representation of U.S. trends.

Figure 2: Housing-market activity

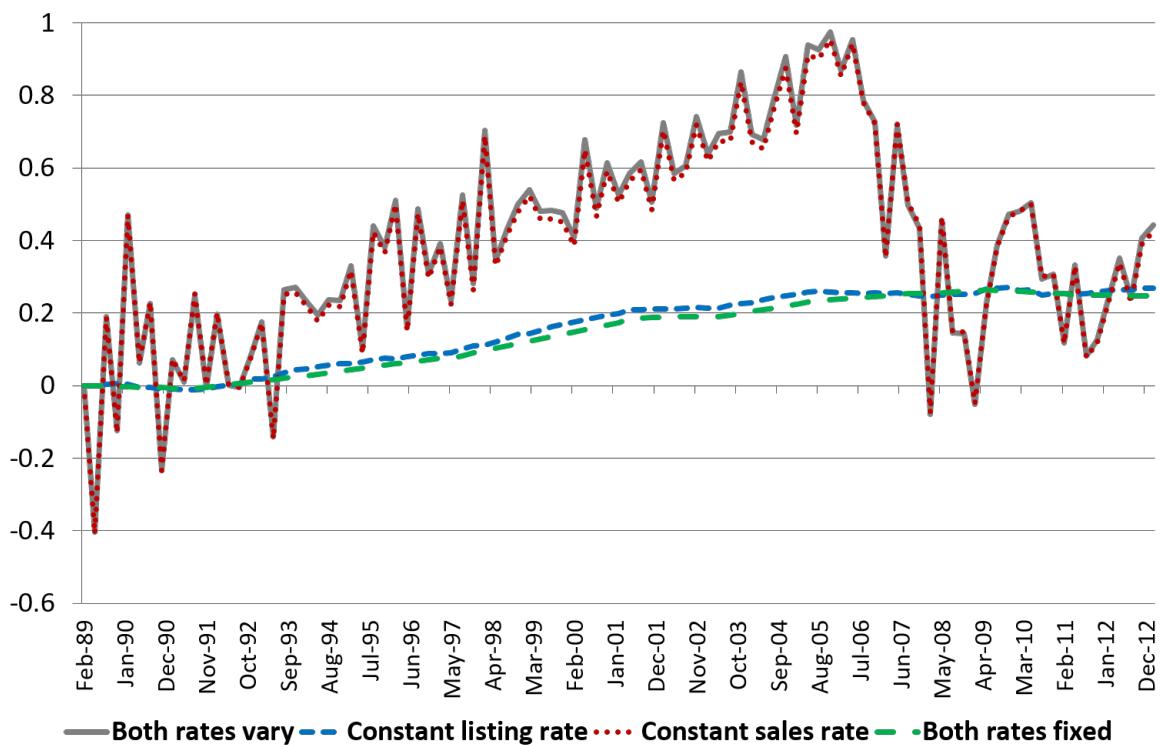


Notes: Series are logarithmic differences from the initial data point. Monthly data (January 1989–June 2013), seasonally adjusted, converted to quarterly series. Definitions are given in section 2.2. Sources: National Association of Realtors, American Housing Survey.

where \bar{s} and \bar{n} are the average sales and listing rates. The time series of S_t^* , $S_{s,t}^*$, $S_{n,t}^*$, and $S_{g,t}^*$ are plotted in Figure 3 below as log differences. The series $S_{n,t}^*$ (the red line) closely resembles S_t^* (the grey line), whereas $S_{s,t}^*$ (the blue line) misses much of the variation in S_t^* . It is striking, yet consistent

with the basic idea set out above, that even large changes in the sales rate account for hardly any of the large variation over time in transactions. Note that almost all the variation in $S_{s,t}^*$ (the blue line) comes from changes $S_{g,t}^*$ (the green line), which is driven only by changes in the housing stock. More interestingly, both $S_{s,t}^*$ and $S_{g,t}^*$ fail to capture the sustained boom and subsequent crash in transactions. This is especially so for the rapid and sustained drop in transactions during the crash. Note that the fall in the sales rate cannot explain the fall in transactions for the reasons explained in [section 2.1](#). As shown in (2.3), the drop in transactions could be due to a decline of a similar magnitude in the owner-occupied housing stock, but the observed change in this variable is far smaller (see [Figure 2](#)).

Figure 3: *Actual and counterfactual transactions*



Notes: The construction of these series is described in [section 2.2](#). The series are reported as log differences relative to their initial values.

The series $S_{g,t}^*$ (the green line) also reveals the limited role played by the construction boom and the rise in the homeownership rate during the period when transactions were increasing. The homeownership rate is defined as the stock of owner-occupied homes divided by the stock of all occupied homes (including those that are rented). Changes in the housing stock as defined and measured earlier can thus occur either through new construction or houses switching from being rented to being owner occupied. Both the construction boom and the rise in the homeownership rate are therefore captured by the housing stock series, and this accounts for relatively little of the change in transactions.

The analysis above assumes that the housing market is always at its steady state in terms of houses for sale as a fraction of the housing stock. This assumption is not too strong when the time horizon is longer than a year owing to the rapid rate of convergence to the steady state. However, as a robustness check, [appendix A.2](#) performs the counterfactual exercises without any assumption on the speed of convergence to the steady state and reaches the same conclusions.

This section has shown that understanding changes in listings is the dominant factor in understanding aggregate housing-market dynamics. The next section builds a tractable model with both endogenous listings and sales.

3 A model of investment in housing match quality

This section presents a search-and-matching model of the housing market that studies both the decision of when to move for an existing homeowner, and the buying and selling decisions of those in the market to buy a new house or sell their current house. The model focuses on the market for existing houses. It abstracts from new entry of houses from either new construction or previously rented houses, and it abstracts from the entry of first-time buyers to the market. As shown using the data in [section 2.2](#), changes in the stock of owner-occupied houses have not been the dominant factor in understanding transaction volumes, so new construction and changes in the homeownership rate have played only a limited role.

3.1 Match quality

The mere existence of an inventory of houses for sale together with a group of potential buyers indicates the presence of search frictions in the housing market. There are broadly two kinds of search frictions: the difficulty of buyers and sellers meeting each other, and the difficulty for buyers of knowing which properties would be a good match prior to viewing them. The first friction is usually modelled using a meeting function.¹² The second friction relates to the number of properties that buyers would need to view before a desirable property is found.

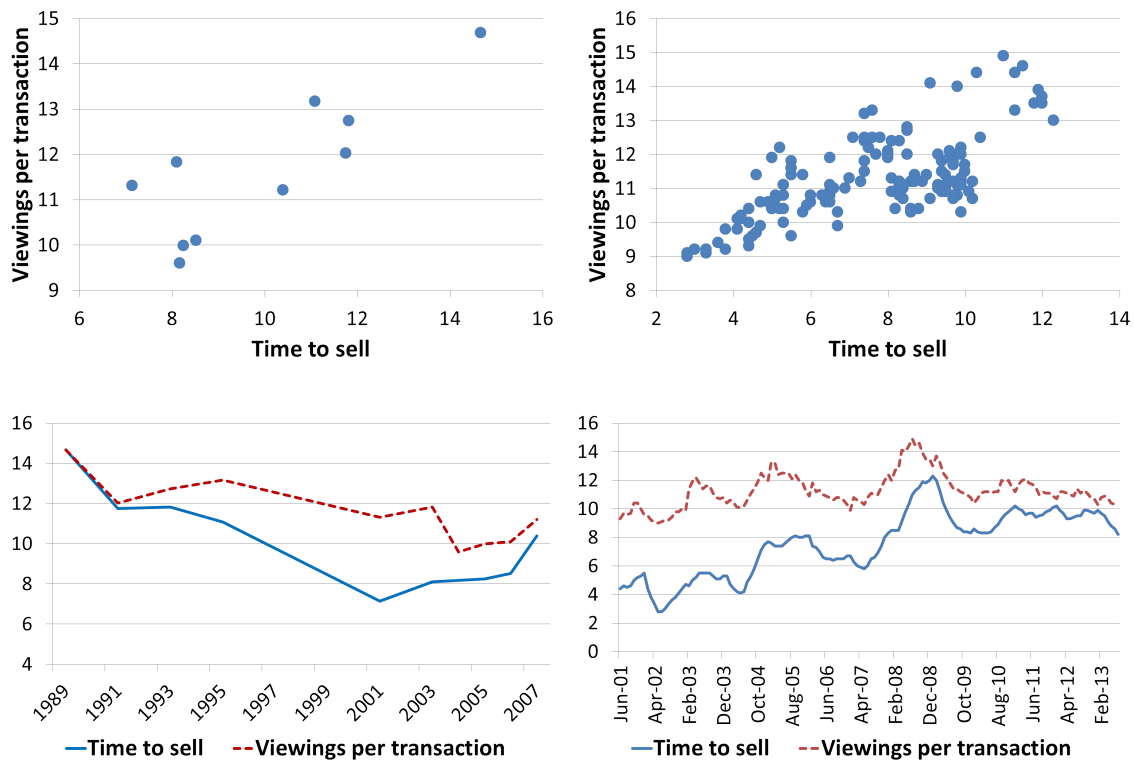
Whether a property is desirable is not easily determined simply by knowing objective features such as the number of bedrooms. What is desirable is a good match between the idiosyncratic preferences of the buyer and the idiosyncratic characteristics of the house for sale. This type of search friction can be modelled as a stochastic match-specific quality that only becomes known to a buyer when a house is actually viewed. The first friction can then be seen as an initial step in locating houses for sale that meet a given set of objective criteria such as size, and the second friction can be seen as the time needed to view the houses and judge the match quality between the buyer and the house.

A measure of the importance of the second friction is the average number of viewings needed before a house can be sold (or equivalently, before a buyer can make a purchase), referred to here as viewings-per-transaction. [Genesove and Han \(2012\)](#) report data on the number of homes visited

¹²The term ‘matching function’ is not used here because not all viewings will lead to matches.

and the time taken to sell using the ‘Profile of Buyers and Sellers’ surveys from the NAR in the U.S. for various years from 1989 to 2007. In the UK, monthly data on time-to-sell and viewings-per-sale are available from the Hometrack ‘National Housing Survey’ from June 2001 to July 2013.¹³ The data are shown in Figure 4. Viewings-per-transaction are far greater than one, indicating that there is substantial uncertainty about match quality prior to a viewing.¹⁴ The figure illustrates that variation in time-to-sell is associated with movements in viewings-per-transaction in the same direction, and is not simply due to variation in the time taken to meet buyers, in other words, a meeting function alone is not sufficient.

Figure 4: *Viewings per transaction and time to sell*



Notes: Left panels, U.S. data, annual frequency (years in sample: 1989, 1991, 1993, 1995, 2001, and 2003–2007); Right panels, U.K. data, monthly frequency (June 2001–July 2013). Time-to-sell is measured in weeks.

Sources: U.S. data, Genesove and Han (2012); U.K. data, Hometrack (www.hometrack.co.uk).

The existence of multiple viewings per sale indicates that the quality of the match with a particular house varies among potential buyers. Given an initial level of match quality when a buyer moves in, and the plausible assumption of some persistence over time in match quality, it is natural

¹³Hometrack data are based on a monthly survey starting in 2000. The survey is sent to estate agents and surveyors every month. It covers all postcodes of England and Wales, with a minimum of two returns per postcode. The results are aggregated over postcodes weighted by the housing stock.

¹⁴Correctly measured, both homes visited and viewings-per-sale are equal to viewings-per-transaction. However, if houses are listed with multiple realtors then viewings-per-sale might underestimate the number of viewings per transaction.

to think that moving is not simply exogenous: there is a comparison of what homeowners already have to what they might hope to gain by moving.

3.2 Houses

The economy contains a unit continuum of families and a unit continuum of houses. Each house is owned by one family (though families can in principle own multiple houses). Each house is either occupied by its owning family and yields a stream of utility flow values, or is for sale on the market while the family searches for a buyer.¹⁵ A family can occupy at most one house at any time. If all a family's houses are on the market for sale, the family is in the market searching for a house to buy and occupy.

It is implicit in the model that families moving house might temporarily use the rental market in between selling and buying. However, there is no explicit modelling of the rental market: effectively, this is treated as a distinct segment of the housing market. This view is consistent with Glaeser and Gyourko (2007) who argue that there is little evidence in support of significant arbitrage between the rental and owner-occupied segments of the housing market because owner-occupied homes typically have different characteristics from rental units, as is also the case for homeowners themselves in comparison to renters. More recently, Bachmann and Cooper (2014) calculate gross flows across and within the owner and renter categories using PSID data. They conclude that rental and owner-occupied markets are distinct segments owing to the dominance of moves within the same tenure category. Moreover, between 1970 and 2009, they find that most transactions are associated with own-to-own moves, rather than own-to-rent moves (the former is 2.3 times the latter), suggesting the majority of owners selling their houses are buying another house.¹⁶

3.3 Behaviour of homeowners

To understand the decision to move, the key variable for homeowners is their match quality ϵ , which will be compared to owners' outside option of search. Match quality is the idiosyncratic utility flow value of an occupied house. This is match specific in that it is particular to both the house and the family occupying it. A homeowner with match quality ϵ receives a utility flow value of $\epsilon\xi$ over time while the house is occupied, where ξ is a variable representing the exogenous economy-wide level of housing demand. Homeowners also incur a flow maintenance cost M irrespective of whether houses are occupied or on the market for sale. Housing demand ξ is common to all homeowners, whereas ϵ is match specific. Moving decisions will lead to an endogenous distribution of match quality across

¹⁵The model abstracts from the possibility that those trying to sell will withdraw from the market without completing a sale.

¹⁶Using a different data source (AHS data from 2001), Wheaton and Lee (2009) find 42.6% of house purchases are by existing homeowners, as opposed to renters and newly formed households. To reconcile this with the conclusion drawn from Bachmann and Cooper's (2014) facts that the majority of owners selling their houses are buying another house, note the following observations. First, using Wheaton and Lee's (2009) data, 57.1% of listings of existing houses occur through own-to-own transitions, rather than through own-to-rent or owner exit. Second, some own-to-rent and rent-to-own transitions may be extremely short lived as part of what is effectively an own-to-own move, for example, someone who lives temporarily in a rented home while a newly purchased home is under refurbishment.

homeowners.

A family's match quality ϵ with its house is a persistent variable subject to occasional idiosyncratic shocks that degrade match quality. These shocks can be thought of as life events that make a house less well suited to the family's current circumstances. The arrival of these shocks follows a Poisson process with arrival rate a (time is continuous). If no shock occurs, match quality remains unchanged. If a shock occurs, match quality ϵ is scaled down from ϵ to $\delta\epsilon$, where δ is a parameter that determines the size of the shocks ($\delta < 1$). Match quality following a shock is still positively related to match quality before the shock because there are many dimensions to what is considered a desirable house, only some of which will be affected by a particular life event. For example, a new job might affect commuting time, but leave other desirable aspects of a particular house unchanged. Note that while the arrival time of the shocks is stochastic, the size of the shock δ is deterministic. If homeowners are ever to consider moving it must be the case that $\delta < 1$.

Following the arrival of an idiosyncratic shock, a homeowner can decide whether or not to move. Those who move become both a buyer and a seller simultaneously. Those who do not experience an idiosyncratic shock face a cost D if they decide to move.¹⁷ For tractability, the model is set up so that a homeowner will always choose not to move in the absence of an idiosyncratic shock (formally, this is done by assuming the limiting case of $D \rightarrow \infty$).¹⁸

The decision of whether or not to move for those who receive shocks depends on all relevant variables including homeowners' own idiosyncratic match quality, and current and expected future conditions in the housing market. The value function for a homeowner occupying a house with match quality ϵ at time t (after a decision not to move has been made) is denoted by $H_t(\epsilon)$. The derivative of the value function with respect to time is denoted by $\dot{H}_t(\epsilon)$. The Bellman equation for $H_t(\epsilon)$ is

$$rH_t(\epsilon) = \epsilon\xi - M + a(\max\{H_t(\delta\epsilon), W_t\} - H_t(\epsilon)) + \dot{H}_t(\epsilon), \quad [3.1]$$

where r is the discount rate, and W_t is the sum of the values of being a buyer and owning a house for sale. The value function $H_t(\epsilon)$ is increasing in ϵ . Thus, when a shock to match quality is received, a homeowner decides to move if match quality ϵ is now below a 'moving threshold' x_t defined by:

$$H_t(x_t) = W_t. \quad [3.2]$$

This equates the value of a marginal homeowner to the outside option of selling an existing house and searching for a new one. The values of being a buyer and a seller are now characterized.

¹⁷This cost represents the 'inertia' of families to remain in the same house, which is in line with empirical evidence. According to the American Housing Survey and the Survey of English Housing, common reasons for moving include being closer to schools, closer to jobs, or because of marriage or divorce.

¹⁸The assumption of a positive D for those who do not receive idiosyncratic shocks has no consequences for the analysis of the steady state of the model. Furthermore, even in the analysis of the model's dynamics, if aggregate shocks are small in relation to the size of transaction costs then the assumption of a positive D has no consequences for those homeowners who have not yet received an idiosyncratic shock.

3.4 Search behaviour

The housing market is subject to two types of search frictions. First, it is time-consuming for buyers and sellers to arrange viewings of houses. Let u_t denote the measure of houses available for sale and b_t the measure of buyers. At any instant, each buyer and each house can have at most one viewing. The arrival rate of viewings is determined by the meeting function $\mathcal{V}(u_t, b_t)$. For houses, viewings have Poisson arrival rate $\mathcal{V}(u_t, b_t)/u_t$. For buyers, the corresponding arrival rate is $\mathcal{V}(u_t, b_t)/b_t$. During this process of search, buyers incur flow search costs F (and homeowners continue to incur maintenance costs M). The meeting function $\mathcal{V}(u_t, b_t)$ is assumed to have constant returns to scale.

Given the unit measure of houses, there are $1 - u_t$ houses that are matched in the sense of being occupied by a family. As there is also a unit measure of families, there must be u_t families not matched with a house, and thus in the market to buy. This means the measures of buyers and sellers are the same ($b_t = u_t$). The arrival rates of viewings for buyers and sellers are then both equal to the constant $v = \mathcal{V}(u_t, u_t)/u_t$. This arrival rate summarizes all that needs to be known about the frictions in locating houses to view.

The second aspect of the search frictions is heterogeneity in buyer tastes and the extent to which any given house will conform to these. As a result of this friction, not all viewings will actually lead to matches.¹⁹ When a viewing takes place, match quality ϵ is realized from a distribution with cumulative distribution function $G(\epsilon)$. For analytical tractability, new match quality is assumed to be drawn from a Pareto distribution (with minimum value 1, a normalization, and shape parameter λ satisfying $\lambda > 1$):

$$G(\epsilon) = 1 - \epsilon^{-\lambda}. \tag{3.3}$$

When a viewing occurs, the value of ϵ that is drawn becomes common knowledge among the buyer and the seller. The value to a family of occupying a house with match quality ϵ is $H_t(\epsilon)$. By purchasing and occupying this house, the buyer loses the option of continuing to search, with the value of being a buyer denoted by B_t . If the seller agrees to an offer to buy, the gain is the transaction price, and the loss is the option value of continuing to search, with the value of owning a house for sale denoted by U_t ('unsatisfied owner'). Finally, the buyer and seller face a combined transaction cost C . The total surplus resulting from a transaction with match quality ϵ at time t is given by

$$\Sigma_t(\epsilon) = H_t(\epsilon) - W_t - C, \tag{3.4}$$

where $W_t = B_t + U_t$ is the combined buyer and seller value function. Given that $H_t(\epsilon)$ is increasing in ϵ , purchases will occur if match quality ϵ is no lower than a threshold y_t , defined by $\Sigma_t(y_t) = 0$. This is the 'transaction threshold'. Intuitively, given that ϵ is observable to both buyer and seller, and the surplus is transferable between the two, the transactions that occur are those with positive

¹⁹The two search frictions are also present in the labour-market model of [Pissarides \(1985\)](#), who combines the meeting function with match quality, where the latter is the focus of [Jovanovic \(1979\)](#). Both frictions also feature in [Novy-Marx \(2009\)](#).

surplus.²⁰ The transactions threshold y_t satisfies the following equation:

$$H_t(y_t) = W_t + C. \quad [3.5]$$

The combined value W_t satisfies the Bellman equation:

$$rW_t = -F - M + v \int_{y_t} (H_t(\epsilon) - W_t - C) dG(\epsilon) + \dot{W}_t. \quad [3.6]$$

Intuitively, the first term on the right-hand side captures the flow costs of being a buyer and a seller, while the second term is the combined expected surplus from searching for a house and searching for a buyer.

Market tightness (b/u) does not play a role in the model because the numbers of buyers b and sellers u perfectly comove. Limited data on time-to-buy from [Genesove and Han \(2012\)](#) show that there is a strong positive correlation at low frequencies between time-to-buy and time-to-sell (years in sample: 1987, 1989, 1991, 1993, 1995, 2001, 2003–2007), suggesting a trend in market tightness cannot be the dominant factor. If it were, time-to-buy and time-to-sell would be negatively correlated. This positive correlation points to other factors such as the efficiency of the meeting function v or any factor that influences the endogenous transaction threshold y_t . It is important to note that a rise in the homeownership rate does not imply there is an upward trend in market tightness. The homeownership rate is defined in terms of the fraction of owner-occupied houses, so a rise in the homeownership rate does not mean that there are more buyers relative to the number of houses.

3.5 Price determination

While the equations (3.5) and (3.6) for the transactions threshold y_t and the value function W_t do not depend on the specific price-setting mechanism, this section briefly discusses price determination under Nash bargaining.

Suppose the seller has bargaining power ω . The buyer and the seller directly bear transaction costs C_b and C_v respectively (with $C_b + C_v = C$). The individual value functions of buyers and sellers are B_t and U_t . If a house with match quality ϵ is sold at a price $p_t(\epsilon)$, the surpluses of the buyer and seller are:

$$\Sigma_{b,t}(\epsilon) = H_t(\epsilon) - p_t(\epsilon) - C_b - B_t, \quad \text{and} \quad \Sigma_{u,t}(\epsilon) = p_t(\epsilon) - C_v - U_t, \quad [3.7]$$

with $\Sigma_{b,t}(\epsilon) + \Sigma_{u,t}(\epsilon) = \Sigma_t(\epsilon)$ being the total surplus given in (3.4). The Bellman equations for the buyer and seller value functions are:

$$rB_t = -F + v \int_{y_t} \Sigma_{b,t}(\epsilon) dG(\epsilon) + \dot{B}_t, \quad \text{and} \quad rU_t = -M + v \int_{y_t} \Sigma_{u,t}(\epsilon) dG(\epsilon) + \dot{U}_t. \quad [3.8]$$

²⁰Some extra assumptions are implicit in this claim, namely that there is no memory of past actions, so refusing an offer yields no benefit in terms of future reputation.

The Nash bargaining solution implies the surplus-splitting equation $(1 - \omega)\Sigma_{u,t}(\epsilon) = \omega\Sigma_{b,t}(\epsilon)$, which determines the transaction price $p_t(\epsilon)$. As shown in [appendix A.4](#), the average transactions price P_t is

$$P_t = \frac{\omega}{1 - G(y_t)} \int_{y_t} H_t(\epsilon) dG(\epsilon) + (1 - \omega)C_v - \omega C_b + \frac{\omega F - (1 - \omega)M}{r}. \quad [3.9]$$

The ratio of the seller's transaction cost C_v to the total transaction cost C is subsequently denoted by κ , and the model will be parameterized in terms of C and κ rather than C_b and C_v .

3.6 Stocks and flows

Let n_t denote the rate at which the stock $1 - u_t$ of houses occupied by their owners are listed (put up for sale), and let s_t denote the rate at which the stock u_t of houses for sale are sold. The accounting identity that connects stocks and flows is

$$\dot{u}_t = n_t(1 - u_t) - s_t u_t. \quad [3.10]$$

The listing (inflow) and sales (outflow) rates n_t and s_t are endogenously determined by the moving decisions of individual homeowners and the transactions decisions of individual buyers and sellers.

Given that transactions occur when the match quality ϵ from a viewing exceeds the transactions threshold y_t , by using the Pareto distribution of new match quality (3.3) the sales rate s_t is:

$$s_t = v\pi_t, \quad \text{with } \pi_t = y_t^{-\lambda}, \quad [3.11]$$

where π_t is the proportion of viewings for which match quality is above the transactions threshold y_t . This term captures the second search friction due to buyers' idiosyncratic tastes. The first friction is captured by the viewing rate v .

The moving rate n_t is derived from the distribution of existing match quality among homeowners together with the moving threshold x_t . The evolution over time of the distribution of match quality depends on the idiosyncratic shocks and moving decisions. The derivation of the moving rate is much more complicated than the sales rate. Surviving matches differ along two dimensions: (i) the initial level of match quality, and (ii) the number of shocks received since the match formed. By using the Pareto distribution assumption (3.3) for new match quality, the following moving rate n_t is derived in [appendix A.5](#):

$$n_t = a - \frac{a\delta^\lambda x_t^{-\lambda} v}{1 - u_t} \int_{\tau \rightarrow -\infty}^t e^{-a(1-\delta^\lambda)(t-\tau)} u_\tau d\tau. \quad [3.12]$$

This equation demonstrates that given the moving threshold x_t , the moving rate n_t displays history dependence. The reason is the persistence in the distribution of match quality among existing homeowners.

The tractability that results from the Pareto distribution assumption comes from the property

that a truncated Pareto distribution is also a Pareto distribution with the original shape parameter. Together with the nature of the idiosyncratic shock process, this is what allows the explicit expression (3.12) to be derived. This property of the truncated Pareto distribution is also useful in calculating the expected surplus from searching for a new house taking into account future moving decisions. Since matches receiving idiosyncratic shocks will survive only if $\delta\epsilon > x$, the calculation of the value function involves only an integral starting from x/δ . This integral can be easily obtained with the Pareto distribution $(\underline{\epsilon}, \lambda)$ because its probability density function is only a function of $\epsilon/\underline{\epsilon}$.²¹

The occurrence of idiosyncratic shocks and the moving and buying decisions affect the distribution of match quality across all current homeowners. Summarizing this distribution by its first moment, let Q_t denote the average of match quality ϵ . The law of motion of Q_t is shown in appendix A.5 to be:

$$\dot{Q}_t = s_t \frac{u_t}{1 - u_t} \left(\frac{\lambda}{\lambda - 1} y_t - Q_t \right) - (a - n_t) \left(Q_t - \frac{\lambda}{\lambda - 1} x_t \right). \quad [3.13]$$

Average match quality Q_t is a state variable owing to the persistence of individual match qualities. The rate of change of match quality is increasing in both the moving and transaction thresholds x_t and y_t .

4 The equilibrium of the model

The equilibrium of the model is derived in two stages. First, moving and transaction thresholds x and y are obtained. The transactions threshold y determines the sales rate s , and both moving and transaction thresholds x and y determine the moving rate n . These then determine transactions and listings, and thus the stock of houses for sale. Throughout, the focus is on the case of perfect foresight with respect to the parameters of the model (no changes in these parameters are anticipated).

4.1 The moving and transactions thresholds

The analysis assumes a case where the idiosyncratic shock is large enough to induce a homeowner with match quality y (a marginal homebuyer) to move, that is, $\delta y < x$. This is true when the parameters of the model satisfy the condition in equation (4.8) below.

When $\delta y < x$, it follows from the homeowner's value function (3.1) that the value for a marginal homebuyer satisfies:

$$(r + a)H(y) = \xi y + aW. \quad [4.1]$$

Using equation (3.1) again, the value for a marginal homeowner (in the sense of being indifferent

²¹There is an analogy with Ss models of price adjustment where assumptions on the distribution of idiosyncratic shocks are often made so that the general shape of the distribution of prices is preserved after the truncations following price changes. See Gertler and Leahy (2008) for a recent example using the uniform distribution.

between remaining a homeowner or moving) satisfies:

$$(r + a)H(x) = \xi x + aW. \quad [4.2]$$

These two values are related as follows using the definitions of the moving and transaction thresholds in (3.2) and (3.5):

$$H(y) = H(x) + C. \quad [4.3]$$

Equations (4.1)–(4.3) together imply that:

$$y - x = \frac{(r + a)C}{\xi}, \quad [4.4]$$

which is the first equilibrium condition linking the moving and transaction thresholds x and y .

A second equilibrium condition connecting x and y is obtained by deriving the combined buyer and seller value W as a function of the moving and transactions thresholds. First, from the definition of the moving threshold x , equations (3.2) and (4.2) together imply that:

$$H(x) = W = \frac{x\xi}{r}. \quad [4.5]$$

Second, the value W can be obtained directly from the flow value equation (3.6) by computing the surplus from a match. The expected surplus from a new match is shown in appendix A.3 to be given by:

$$\int_y (H(\epsilon) - W - C)dG(\epsilon) = \frac{\xi \left(y^{1-\lambda} + \frac{a\delta^\lambda}{r+a(1-\delta^\lambda)} x^{1-\lambda} \right)}{(r + a)(\lambda - 1)}. \quad [4.6]$$

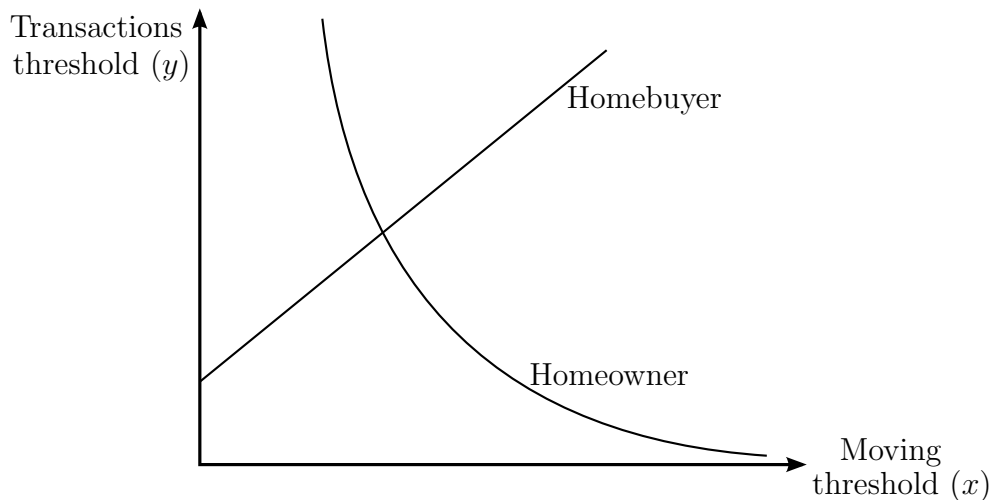
Allowing for moving decisions means that the expected surplus of a new match depends not only on the transactions threshold y but also on the moving threshold x . Combining this equation with (3.6) and (4.5) yields the second equilibrium condition linking x and y :

$$x = \frac{v \left(y^{1-\lambda} + \frac{a\delta^\lambda}{r+a(1-\delta^\lambda)} x^{1-\lambda} \right)}{(r + a)(\lambda - 1)} - \frac{F}{\xi}. \quad [4.7]$$

Together, equations (4.4) and (4.7) can be jointly solved for the thresholds x and y without reference to state variables such as the number of houses for sale or the distribution of existing match quality. Figure 5 depicts the determination of the moving and transaction thresholds as the intersection between an upward-sloping equation (4.4) and a downward-sloping equation (4.7). Intuitively, the upward-sloping line ties the value of a marginal homebuyer to that of a marginal homeowner together with the transaction cost (which is sunk for someone who has decided to become a buyer, but not for an existing homeowner who can choose to stay). This line is referred to as the ‘homebuyer’ curve. The downward-sloping curve ties the value of the marginal homeowner to the

expected value of becoming a buyer. This line is referred to as the ‘homeowner’ curve.

Figure 5: *Determination of the moving (x) and transactions (y) thresholds*



Notes: The homebuyer and homeowner curves represent equations (4.4) and (4.7) respectively.

In (x, y) space, these two curves pin down the equilibrium values of x and y . If an equilibrium exists, it must be unique. It is shown in [appendix A.3](#) that an equilibrium satisfying the conditions $y > 1$ and $\delta y < x$ exists if and only if:

$$\max \left\{ 1, \frac{(r+a)C}{(1-\delta)\xi} \right\}^{1-\lambda} + \frac{a\delta^\lambda}{r+a(1-\delta^\lambda)} \left(\max \left\{ 1, \frac{(r+a)C}{(1-\delta)\xi} \right\} - \frac{(r+a)C}{\xi} \right)^{1-\lambda} - \frac{(\lambda-1)(r+a)}{v} \left(\max \left\{ 1, \frac{(r+a)C}{(1-\delta)\xi} \right\} - \frac{(r+a)C}{\xi} + \frac{F}{\xi} \right) > 0. \quad [4.8]$$

4.2 Efficiency

The equilibrium of a search-and-matching model is often Pareto inefficient owing to the presence of externalities. For example, a ‘congestion externality’ occurs when individuals do not take account of the extra difficulty in finding a match faced by others when they enter the market. Furthermore, there is typically a ‘hold-up’ problem whereby one party is able to extract surplus from another after sunk costs of search have been incurred, which when anticipated reduces the incentive of the other to enter the market.

It turns out that the equilibrium of this model is Pareto efficient. The equilibrium is the solution of the following social planner’s problem with objective function

$$\Omega_T = \int_{t=T}^{\infty} e^{-r(t-T)} (\xi(1-u_t)Q_t - Cs_tu_t - Fu_t - M) dt, \quad [4.9]$$

where Q_t , s_t , and u_t are the average match quality, sales rate, and stock of unsold houses resulting from the planner’s choice of the moving and transaction thresholds. It is shown in [appendix A.6](#)

that maximizing this objective function subject to the laws of motion derived earlier leads to exactly the same moving and transaction thresholds as the equilibrium of the model.

Intuitively, the usual congestion externality is not present here because homeowners who decide to move enter the market simultaneously on both sides as a buyer and as a seller. Owing to the constant-returns meeting function, entry has no effect on the likelihood of any other participant in the market meeting a buyer or a seller. Furthermore, the hold-up problem is also absent, again because homeowners enter on both sides of the market. If participants on one side of the market are able to extract surplus from participants on the other side then homeowners entering the market knows that they will face hold up, but will also be able to hold up others. Ex ante, when moving decisions are made, these two effects are expected to cancel out. Private moving and transaction decisions thus result in a socially efficient allocation.

This analysis implicitly assumes that the costs associated with moving and search are resource costs rather than costs imposed by tax policy. In practice, some countries impose taxes on property transactions. The model can be used to assess the welfare costs of raising revenue through such taxes, an issue which cannot be satisfactorily addressed in a model of exogenous moving. An illustrative calculation of deadweight losses is provided in [appendix A.7](#).

4.3 Steady state

Taking as given the moving and transaction thresholds x and y , there exists a unique steady state for all stocks and flows. This steady state naturally has $\dot{u}_t = 0$, but also the distribution of existing match quality must have converged to its ergodic limit, which in practice requires that both u_t and n_t are constant over time.

First, the transaction threshold y directly pins down the sales rate s using equation (3.11):

$$s = vy^{-\lambda}. \quad [4.10]$$

The steady-state moving rate can be derived from (3.10) and (3.12) using $\dot{u}_t = 0$ and $\dot{n}_t = 0$:

$$n = \frac{a}{1 + \frac{\delta^\lambda}{1-\delta^\lambda} \left(\frac{y}{x}\right)^\lambda}. \quad [4.11]$$

Note that the term in the denominator can be expressed as

$$1 + \frac{\delta^\lambda}{1-\delta^\lambda} \left(\frac{y}{x}\right)^\lambda = 1 + \left(\frac{\delta y}{x}\right)^\lambda + \left(\frac{\delta^2 y}{x}\right)^\lambda + \dots, \quad [4.12]$$

which is equal to the sum of the conditional survival probabilities (starting from $\epsilon > y$) after receiving k shocks, summing over $k = 0, 1, 2, \dots$. When no shocks have been received, the match is of quality $y > x$, so the survival probability is 1. After $k \geq 1$ shocks, the conditional survival probability is $(\delta^k y/x)^\lambda$.

Given the steady-state sales and moving rates s and n , the steady state for houses for sale follows

immediately from (3.10):

$$u = \frac{n}{s + n}. \quad [4.13]$$

Average match quality in the steady state is obtained from equation (3.13):

$$Q = \frac{\lambda}{\lambda - 1} \left(\frac{n}{a} y + \left(1 - \frac{n}{a} \right) x \right), \quad [4.14]$$

which is related to a weighted average of the transaction and moving thresholds y and x , with the weight on x depending on the degree to which moving is endogenous (that is, how far the moving rate n is below the arrival rate a of idiosyncratic shocks). The average transaction price P is:

$$P = C_v - \frac{M}{r} + \omega \left(\frac{1}{r} + \frac{y^\lambda}{v} \right) (\xi x + F). \quad [4.15]$$

4.4 Transitional dynamics and overshooting

Following a change in the moving and/or transaction thresholds, the housing market will begin a process of convergence to the new steady state for the volume of transactions, the moving rate, and the stock of houses for sale. There are two facets of these transitional dynamics. First, there is convergence in the stock of houses for sale given the inflow and outflow rates, which is a common feature of most search models. Second, endogenous moving together with persistence in existing match quality gives rise to a novel source of transitional dynamics as the distribution of match quality converges to its ergodic limit.

First, abstracting from any transitions in the match-quality distribution, if the moving threshold is constant then the moving rate will also be constant. Given constant sales and moving rates s and n , the dynamics of houses for sale can be described as follows using the law of motion (3.10) and the steady-state equation (4.13):

$$\dot{u}_t = -(s + n)(u_t - u). \quad [4.16]$$

The gap between u_t and u is closed over time at rate $s + n$. Since time-to-sell (the reciprocal of s) is fairly short on average (a few months), the speed of convergence to the steady state is sufficiently rapid that these dynamics are of limited interest (as is also the case for unemployment in the labour-market analogue of this model).

The second source of transitional dynamics can be isolated using the following method. Denote by u_t^* the hypothetical level of houses for sale if the first source of transitional dynamics is ignored:

$$u_t^* = \frac{n_t^*}{s_t + n_t^*},$$

where n_t^* is the moving rate implied by (3.12) when $u_t = u_t^*$. Associated with u_t^* and n_t^* is the volume of transactions and listings $S_t^* = N_t^* = s u_t^* = n_t^* (1 - u_t^*)$. It is shown in [appendix A.8](#) that

the transitional dynamics of these variables are given by:

$$\frac{\dot{S}_t^*}{S_t^* - S} = \frac{\dot{N}_t^*}{N_t^* - N} = \frac{\dot{u}_t^*}{u_t^* - u} = -a(1 - \delta^\lambda) \left(\frac{a}{n}\right) \left(\frac{s+n}{s+a}\right), \quad \text{and}$$

$$\frac{\dot{n}_t^*}{n_t^* - n} = -a(1 - \delta^\lambda) \left(\frac{a}{n}\right) \left(\frac{s+n_t^*}{s+a}\right).$$

Even ignoring the inflow-outflow dynamics affecting houses for sale, the housing market would still not reach its steady state immediately. The equations above show that S_t^* , N_t^* , and u_t^* converge monotonically to the steady state at a common rate. For n_t^* , the differential equation is not linear, but qualitatively, the pattern of convergence is the same as the other variables. Quantitatively, the rate of convergence is largely determined by a , and also the ratio of a/n (the final term in parentheses is close to one because s is large relative to a and n). Since moving is infrequent (homeowners live in their houses for more than a decade on average), the arrival rate a of the idiosyncratic shock cannot be too large, and therefore convergence in the match quality distribution is relatively slow.

It is also shown in [appendix A.8](#) that starting from a steady state, the moving rate n_t^* immediately following a change in x (with y held constant) is

$$n_{t_+}^* = \frac{a - \frac{\delta^\lambda}{1-\delta^\lambda} \left(\frac{y}{x}\right)^\lambda s u_{t_-}^*}{1 + \frac{\delta^\lambda}{1-\delta^\lambda} \left(\frac{y}{x}\right)^\lambda u_{t_-}^*},$$

where $n_{t_+}^*$ denotes the value of n_t^* on impact and $u_{t_-}^*$ denotes the value of u_t^* prior to the change. Consider a case where the moving threshold x rises, which increases the steady-state moving rate so that $n > n_{t_-}^*$. The appendix shows $n_{t_+}^* > n > n_{t_-}^*$, so there is overshooting of the moving rate on impact, and this overshooting gradually declines according to transitional dynamics characterized earlier. Intuitively, a higher moving threshold x cleanses the distribution of match quality. As this process takes place, there is more moving in the short term, but the subsequent improvement in the match quality distribution means the long-term effect of the moving threshold on the moving rate is smaller.

4.5 The role of persistence in match quality

The endogenous moving decision here is analogous to the endogenous job-separation decision introduced in [Mortensen and Pissarides \(1994\)](#) for labour markets, but there is an important difference in the nature of the arrival process of new match quality. There, when an existing match is subject to an idiosyncratic shock, a new match quality is drawn independently of the match quality before the shock, that is, the stochastic process for match quality is ‘memory-less’. Here, idiosyncratic shocks degrade match quality, but an initially higher-quality match remains of a higher quality than a lower-quality match hit by the same shock. In other words, match quality is persistent.

This difference matters because it turns out that when match quality is persistent, the moving rate is affected by the transaction threshold as well as the moving threshold. More importantly, persistence of match quality makes the modelling of moving closer to an investment decision that

is influenced by a predetermined stock of existing match quality. This means aggregate moving rates can display high volatility for similar reasons that capital investment rates do. Endogenous moving is also present in [Guren \(2014\)](#), though the focus there is on how the existence of a concave demand curve can amplify price insensitivity in housing market, helping to account for the positive autocorrelation of house-price changes (momentum). Endogenous moving is modelled there by assuming homeowners face idiosyncratic shocks to the cost of moving from their current houses. Like [Mortensen and Pissarides \(1994\)](#), the moving decision is effectively ‘memory-less’, so the focus is mainly on how moving decisions react to short-run expectations of price changes.

4.6 Exogenous moving model

The general model embeds an exogenous moving model as a special case when $\delta = 0$. In this case any homeowner will move house after an idiosyncratic shock because match quality will drop to zero. Thus, the moving rate is the same as the exogenous arrival rate a of the idiosyncratic shock. By substituting equation (4.4) into (4.7) and setting $\delta = 0$, the transaction threshold y is the solution of the equation:

$$\frac{vy^{1-\lambda}}{(r+a)(\lambda-1)} = \left(y + \frac{F - (r+a)C}{\xi} \right), \quad [4.17]$$

where the first term is the expected surplus from a new match when future moving occurs at an exogenous rate a . This changes the effective discount rate to $a+r$, which is applied to the expected flow surplus $vy^{1-\lambda}/(\lambda-1)$ from a new match. The inflow rate n is now simply a , whereas the outflow rate s is the same as in (4.10).

4.7 The importance of transaction costs

In the special case of zero transactions costs, the model has the surprising feature that its steady-state equilibrium is isomorphic to the exogenous moving model with the parameter a redefined as $a(1-\delta^\lambda)$. The logic behind this is that equation (4.4) implies $y = x$ when $C = 0$. From (4.11), this means that $n = a(1-\delta^\lambda)$, so the moving rate is independent of the equilibrium moving and transactions thresholds. Hence, only those parameters directly related to the shocks received by homeowners affect the moving rate. The equilibrium value of y is determined by replacing x by y in equation (4.7) and simplifying to:

$$\frac{vy^{1-\lambda}}{(r+a(1-\delta^\lambda))(\lambda-1)} = y + \frac{F}{\xi}.$$

This equation is identical to (4.17) for the exogenous moving model with $a(1-\delta^\lambda)$ replacing a . Therefore, all steady-state predictions of the two models would be the same if $C = 0$.

5 The 1995–2004 housing-market boom

This section presents an application of the model to housing-market boom between 1995 and 2004. The housing-market crash of 2007 has been the focus of much commentary, but [Figure 2](#) reveals that the decade 1995–2004 was also a time of dramatic change. That period was characterized by a high level of housing-market activity: houses were selling faster, more houses were sold, and at the same time, more houses were put up for sale.

Transactions rose by 52%, while the sales rate increased by 22%. Despite the rise in the sales rate, the stock of houses for sale did not fall, and in fact increased by 30% while the fraction of houses for sale increased by 12%.²² The time series of listings plays a key role in reconciling the behaviour of transactions, the sales rate, and houses for sale. During this period, the volume of listings rose by 55% while the listing rate increased by 37%. Not only were houses selling faster (the rise in the sales rate), but at the same time homeowners decided to move more frequently. This increase in listings generated a rise in the stock of houses for sale, which also boosted transactions. Interestingly, the rise in the listing rate mirrors the 33% rise in the own-to-own moving rate found by [Bachmann and Cooper \(2014\)](#) using household-level data from the PSID.

It is well known that there was a boom in construction and a rise in the homeownership rate during the period in question. As explained in [section 2.2](#), both factors are captured by the increase in the owner-occupied housing stock series. Equation (2.3) shows that changes in the housing stock have an approximately proportional effect on transactions, which is seen in the 18% rise in the housing stock (the grey line in [Figure 2](#)) and the 18% contribution of the housing stock to transactions (the green line in [Figure 3](#)). Thus, net of the contribution from the changing housing stock, transactions rose by 34% and the number of listings increased by 37%. There remains a substantial rise in transactions even after accounting for changes in the owner-occupied housing stock. Finally, note that real house prices increased by 45% during the period in question according to the purchase-only price index from the Federal Housing Finance Agency (FHFA) deflated by the personal consumption expenditure (PCE) price index.

There are at least three features of the economic environment during the period 1995–2004 that have implications for moving decisions according to the model and which are consistent with the rise in listings. These are the increase in productivity growth, the adoption of internet technology, and cheaper and more easily accessible credit. It is explained in [appendix A.9](#) why changes in productivity and market interest rates can be interpreted as changes in the preference parameters ξ and r in the model. An increase in productivity raises incomes and increases the demand for housing ξ . The adoption of internet technology reduces search frictions in arranging viewings by distributing information about available houses and their general characteristics more widely among potential buyers. This raises the meeting rate v implied by the meeting function. Finally, lower mortgage rates reduce the opportunity cost of capital and thus lower the discount rate r in the model. Easier access to credit such as a fall in the fixed cost of obtaining a mortgage can be interpreted as a

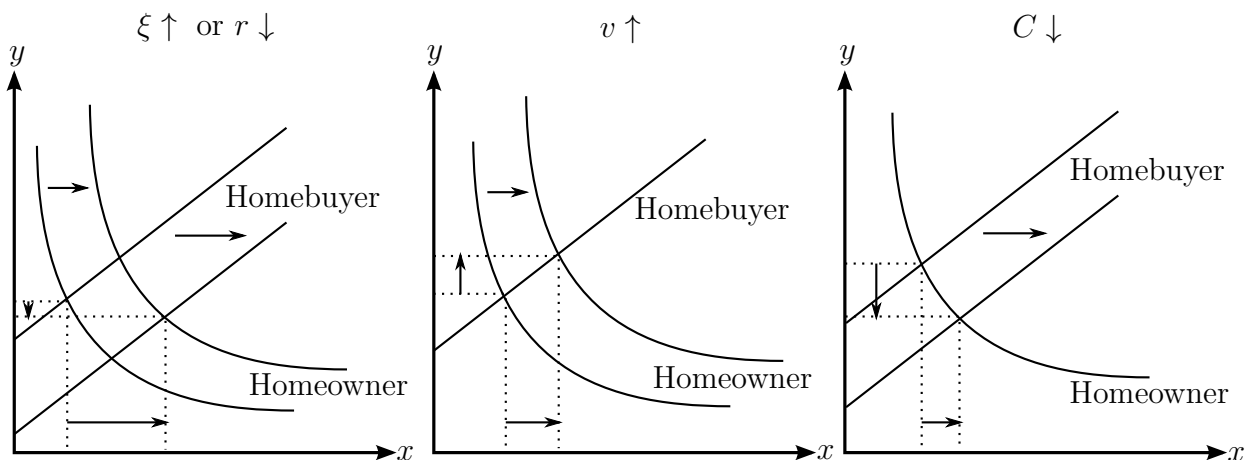
²²The percentage changes referred to in this section are the percentage changes of variables between the 1994 average and the 2004 average.

reduction in total transaction costs C (buyers' transaction costs C_b are lower). Another relevant factor that effectively lowered transaction costs C during this period is the Taxpayer Relief Act of 1997, which reduced the tax payable on moving for some existing homeowners (lower transaction costs C_s for sellers).²³

Using Figure 5, which depicts equations (4.4) and (4.7), both a rise in ξ and a fall in r imply the two curves shift to the right, as shown in the left panel of Figure 6 below. A rise in v implies the curve representing (4.7) shifts to the right (as shown in the middle panel). Last, a fall in C implies a downward shift of the line representing (4.4) (as shown in the right panel). In all cases, the moving threshold x increases, and increases proportionately more than y . Using equation (4.11), a rise in x/y leads to an unambiguous increase in the moving rate n . The sales rate unambiguously rises when C falls, but the effect is ambiguous in the other three cases.

The intuition for the effects on the moving threshold is the following. Take the case of lower mortgage rates r . This increases the present discounted value of flows of housing services, so it increases the incentive to invest in match quality, reducing the tolerance for low current match quality (higher moving threshold x), resulting in more frequent moves. However, there are two offsetting effects on transactions decisions. On the one hand, buyers are more keen to make a purchase to receive the higher discounted sum of flow values, so they become less picky (lower transaction threshold y). On the other hand, owing to the reduced tolerance for low quality matches as a homeowner, the expected duration of a match is shortened, which makes buyers more picky (higher y). The intuition is essentially the same for the effects of an increase in ξ . In the case of the higher viewing rate v , the effect is to increase the expected surplus from searching. This increases the incentive to search both for existing homeowners and homebuyers, making both more picky (higher moving and transaction thresholds x and y). Finally, a lower transaction cost C shrinks the gap between the least acceptable current match and the least acceptable new match, resulting in more moving and more transactions.

Figure 6: Comparative statics of moving and transaction thresholds



²³Shan (2011) and Heuson and Painter (2014) present evidence showing that this policy change led to an increase in mobility and transactions.

Quantifying the predictions of the model requires a calibration of the parameters. This is the goal of the next section.

5.1 Calibration

The model contains a total of 11 parameters $\{a, \delta, \lambda, v, C, F, M, \omega, \kappa, r, \xi\}$. Some parameters are directly matched to the data, while others are determined indirectly by choosing values that make the predictions of the model consistent with some empirical targets. For the parameter ω , a value of 0.5 is directly imposed to give buyers and sellers equal bargaining power. The (annual) discount rate r is set to 5.7% ($r = 0.057$), which is the 1994 average of the HP-filtered 30-year real mortgage rate series (subtracting PCE inflation from the nominal mortgage rate).

The parameters C , F , M , and κ are calibrated to match the costs of owning a house and the costs involved in buying and selling houses, and how those costs are distributed across buyers and sellers. Let $c = C/P$, $f = F/P$, and $m = M/P$ denote the costs C , F , and M relative to the average house price P in the steady state of the model. The data provide information on costs relative to price, so calibration targets for c , f , and m are adopted that will determine C , F , and M indirectly. As shown in [appendix A.10](#), the cost-to-price ratios predicted by the model are:

$$c = \frac{\frac{C}{\xi}}{\kappa \frac{C}{\xi} - \frac{M}{r\xi} + \omega \left(\frac{1}{r} + \frac{y^\lambda}{v} \right) \left(x + \frac{F}{\xi} \right)}; \quad [5.1a]$$

$$f = \frac{\frac{F}{\xi}}{\kappa \frac{C}{\xi} - \frac{M}{r\xi} + \omega \left(\frac{1}{r} + \frac{y^\lambda}{v} \right) \left(x + \frac{F}{\xi} \right)}; \quad [5.1b]$$

$$m = \frac{\frac{M}{\xi}}{\kappa \frac{C}{\xi} - \frac{M}{r\xi} + \omega \left(\frac{1}{r} + \frac{y^\lambda}{v} \right) \left(x + \frac{F}{\xi} \right)}. \quad [5.1c]$$

Observe that C , F , and M appear only as ratios to ξ , so the value of ξ can be normalized to 1.

Following [Poterba \(1991\)](#), the flow cost M of owning a house is set so that in equilibrium it is 4.5% of the average house price ($m = 0.045$). This cost is made up of a 2.5% maintenance cost and a 2% property tax. The maintenance cost is interpreted as the cost required perpetually to maintain a house in the same physical condition as when it was first purchased.

The costs incurred in buying and selling houses comprise the one-off transactions cost C and the flow costs of search F . For transaction costs, [Quigley \(2002\)](#) estimates the total costs as being in the range 6–12% of price in the U.S., with about 3–6% being the realtor’s fee paid by the seller. [Ghent \(2012\)](#) summarizes recent research and uses a total transaction cost of 13.1%, where 5.1% is the realtor’s fee borne by the seller. In light of these findings, the total transaction cost C is set so that it is 10% of the price ($c = 0.1$), and the share κ of these costs borne by the seller is set to be $1/3$.

For the flow cost parameter F , unfortunately there are almost no estimates of the flow costs of searching. The approach taken here is to base an estimate of F on the opportunity cost of the time spent searching. Assuming one house viewing entails the loss of a day’s income, the value of F can

be calibrated by adding up the costs of making the expected number of viewings. In the model, time-to-buy is equal to time-to-sell, so buyers will incur search costs $T_s F$ per housing transaction on average, where T_s denotes time-to-sell. With viewings-per-sale equal to the average number of viewings made by a buyer, the total search cost should be equated to $V_s Y/365$, where V_s denotes average viewings-per-sale and Y denotes average annual income. Thus, the calibration assumes $T_s F = V_s Y/365$, and by dividing both sides by $P T_s$, this implies an equation for $f \equiv F/P$:

$$f = \frac{1}{365} \frac{Y V_s}{P T_s}.$$

Using a house-price to income ratio of 2 as a reasonable average value (Case and Shiller, 2003) together with the values of $T_s = 6.5/12$ and $V_s = 10$ discussed below, the ratio of the flow cost of search to the average price is calibrated to be 2.5% ($f = 0.025$). Note that 2.5% should be interpreted as the hypothetical cost of spending a whole year searching.

While the data described above provide information about the ratios of the parameters C , F , and M to the average house price P , since determination of the price P depends in general on all the other parameters, the calibration must be done jointly with that for the remaining parameters $\{a, \delta, \lambda, v\}$. These four parameters are calibrated using four additional empirical targets: the average time to sell a house, the average number of viewings per sale, the expected tenure (expected duration of new matches), and the average years of ownership (the average time existing homeowners have spent in their homes).

The average time to sell is the reciprocal of the average sales rate obtained using data from NAR on transactions and inventories (for existing single-family homes), as described in section 2.2.²⁴ Average time-to-sell over the period 1991–2013 is 6.5 months.

Previous research on housing markets has used a variety of sources for data on time-to-sell, and there is a considerable dispersion in these estimates. Using the ‘Profile of Buyers and Sellers’ survey collected by NAR, Genesove and Han (2012) report that for the time period 1987–2008, the average time-to-sell is 7.6 weeks, the average time-to-buy is 8.1 weeks, and the average number of homes visited by buyers is 9.9. They also discuss other surveys that have reported similar findings.

However, the estimates of time-to-sell and time-to-buy derived from survey data are likely to be an underestimate of the actual time a new buyer or seller would expect to spend in the housing market. The reason is that the survey data include only those buyers and sellers who have successfully completed a house purchase or sale, while the proportion of buyers or sellers who withdraw from the market (at least for some time) without a completed transaction is substantial. Genesove and Mayer (1997) estimate the fraction of withdrawals at 50%, and Levitt and Syverson (2008) report a withdrawal rate of 22%. A high withdrawal rate is also found by Anenberg and Laufer (2016) using the MLS database between 2008–2012 for nine large MSAs. In comparing the efficiency of different platforms for selling properties, Hendel, Nevo and Ortalo-Magné (2009) explicitly control for withdrawals and report a time-to-sell of 15 weeks (using the Multiple Listing Service for the city

²⁴Time-to-sell is highly correlated with the ‘months supply’ variable reported by NAR, which is defined as inventories divided by transactions.

of Madison).²⁵

An alternative approach to estimating time-to-sell that does not face the problem of withdrawals is to look at the average duration for which a home is vacant using data from the American Housing Survey. In the years 2001–2005, the mean duration of a vacancy was 7–8 months. However, that number is likely to be an overestimate of the expected time-to-sell because it is based on houses that are ‘vacant for sale’. Houses that are for sale but currently occupied would not be counted in this calculation of average duration. Another approach that avoids the problem of withdrawals is to look at the average time taken to sell newly built houses. [Díaz and Jerez \(2013\)](#) use the Census Bureau ‘New Residential Sales’ report to find that the median number of months taken to sell a newly built house is 5.9 (for the period 1991–2012). This is only slightly shorter than the average of the time-to-sell number constructed using NAR data on existing single-family homes, but there is reason to believe that newly built homes should sell faster than existing homes owing to greater advertising expenditure and differences in the target groups of buyers.

In summary, most studies find that average time-to-sell is less than three months in cases where there is a potential withdrawal bias that is not controlled for. Most studies that are not subject to this bias, or attempt to control for it, find times-to-sell of more than four months. Since the predictions of the model will be compared to variables constructed from the NAR transactions and inventories data, a measure of time-to-sell consistent with this data is used. The calibration target is a time-to-sell of 6.5 months, hence $T_s = 6.5/12$. The calibration target for viewings per sale is set to 10 ($V_s = 10$) on the basis of the studies discussed above. In the model, average time-to-sell is the reciprocal of the sales rate in (4.10), and average viewings per sale is the reciprocal of the probability π that a viewing leads to a sale:

$$T_s = \frac{1}{vy^{-\lambda}}, \quad \text{and} \quad V_s = \frac{1}{y^{-\lambda}}. \quad [5.2]$$

The remaining calibration targets are for the number of years a buyer expects to remain in the same house (expected tenure, denoted T_n), and the average number of years existing homeowners have lived in their current houses (average years of ownership, denoted T_h). Note that these two numbers are not necessarily the same when the hazard rate of moving is not independent of the time already spent in a house. An estimate of both expected tenure and average years of ownership can be derived from the data in Table 2.9 (Year Householder Moved into Unit) of the American Housing Survey, which gives a frequency distribution for the time since owners moved into their homes. The data are supplied in 5-year bins for durations of less than 40 years, and in 10-year bins for longer durations.²⁶ In calculating the expected tenure and the average years of ownership, the frequency

²⁵For the U.K., [Merlo and Ortalo-Magné \(2004\)](#) obtain data from four real estate agencies that contain 780 completed transaction histories between 1995–1998 for Greater London and for South Yorkshire. They report an average time-to-sell of 11 weeks, but this number does not control for withdrawals, which they find occur at a rate of 25% in their data. They also report an average of 9.5 viewings per transaction for a sub-sample of 199 properties in their data.

²⁶The first bin requires special treatment because it covers a five-year interval that does not generally coincide with the survey year, and because the survey itself is conducted in the middle of the year (between mid-April and mid-September during a survey year). For example, in 2005, the first bin starts in the survey year, so this bin effectively

in each bin is assumed to be equally distributed within the bin. Elderly owners (over 65 years) are removed from the data because such individuals are less likely to consider moving. Using the 2005 survey, the average years of ownership is found to be 11 years ($T_h = 11$).

The expected tenure is found from the same data by calculating the hazard function for moving house consistent with the frequency distribution of the years of ownership (this assumes that the empirical distribution is the stationary distribution implied by the hazard function). The method leads to an estimate of expected tenure of 12.2 years ($T_n = 12.2$). That the expected tenure is longer than the average years of ownership is consistent with the model's prediction of a hazard rate for moving that is increasing in time spent in a house. It is shown in [appendix A.5](#) that the model implies expected tenure T_n and average years of ownership T_h are given by:

$$T_n = \frac{1}{a} \left(1 + \frac{\delta^\lambda}{1 - \delta^\lambda} \left(\frac{y}{x} \right)^\lambda \right), \quad \text{and} \quad T_h = \frac{\frac{1}{a} \left(1 + \frac{\delta^\lambda}{1 - \delta^\lambda} \left(1 + \frac{1}{1 - \delta^\lambda} \right) \left(\frac{y}{x} \right)^\lambda \right)}{1 + \frac{\delta^\lambda}{1 - \delta^\lambda} \left(\frac{y}{x} \right)^\lambda}. \quad [5.3]$$

The seven calibration targets used to determine the parameters $\{a, \delta, \lambda, v, C, F, M\}$ are listed in [Table 1](#). Intuitively, expected tenure and average years of ownership provide information about the arrival rate a of idiosyncratic shocks and the size of those shocks (the parameter δ). Both a lower arrival rate and smaller idiosyncratic shocks would lead to longer expected tenure and greater average years of ownership. The two parameters can be separately identified because having data on both T_n and T_h provides information not only about the average hazard rate of moving, but also its dependence on duration. Furthermore, the parameters a and δ have very different effects on the hazard function. A decrease in the arrival rate a of shocks uniformly decreases the hazard rate for all durations, while a decrease in the size of the shocks also tilts the hazard function so that its slope increases. The reason is that with very large idiosyncratic shocks, the moving decision would essentially depend only on receiving one shock. With smaller idiosyncratic shocks, homeowners who start with a high match quality would require more than one shock to persuade them to move, making moving more likely for longer-duration homeowners who have had time to receive multiple shocks than for those who have moved more recently.

There is also an intuitive connection between the parameter λ and the calibration target time-to-sell. The value of λ determines the amount of dispersion in the distribution of potential match quality, and thus the incentive to continue searching. A low value of λ indicates a high degree of dispersion, in which case families will be willing to spend longer searching for an ideal house. For the final parameter v , the average time between viewings can be found by dividing time-to-sell by viewings-per-sale, which directly provides information about the arrival rate v of viewings, as can be seen from equation (5.2).

A simple method for exactly matching the seven parameters $\{a, \delta, \lambda, v, C, F, M\}$ to the seven empirical targets in [Table 1](#) is described in [appendix A.10](#). The parameters matching the targets and those directly calibrated are all shown in [Table 2](#).

covers only one tenth of the time spanned by the other bins. The frequency in the first bin is scaled up accordingly.

Table 1: *Targets used to calibrate parameters*

Target description	Notation	Value
Time to sell (time to buy)	T_s	6.5/12
Viewings per sale (viewings per purchase)	V_s	10
Expected tenure of homeowners	T_n	12.2
Average years of homeownership	T_h	11
Ratio of transaction cost to average price	c	0.10
Ratio of flow search costs to average price	f	0.025
Ratio of flow maintenance costs to average price	m	0.045

Notes: The data sources for these empirical targets are discussed in [section 5.1](#).

5.2 Quantitative results

This section presents a quantitative analysis of the three developments discussed earlier for the period 1995–2004: the productivity boom, the rise of internet-based property search, and the improvement in credit conditions.

5.2.1 Baseline results

A simple measure of productivity growth is the increase in real GDP per person, which grew by a total of 25% over the decade. This is identical to the growth in the HP-filter trend line. A rise in income naturally leads to an increase in housing demand (the parameter ξ in the model), the extent of the increase also depending on the income-elasticity of housing, which is assumed to be unity here.²⁷

The rise of internet-based property search would be expected to improve the efficiency of search as captured by the meeting function (the parameter v in the model). Since $v = T_s/V_s$, data on time-to-sell and viewings-per-sale can be used to infer the rise in v . Using data from [Genesove and Han \(2012\)](#), the maximum rise in T_s/V_s over the period in question is 33%, and this is taken as an upper bound on the efficiency gains.

Mortgage rates (30-year conventional) declined from 8.4% in 1995 to 5.8% in 2004, while inflation (PCE) increased from 2.1% to 2.4%.²⁸ To abstract from transitory movements in interest rates, the focus is on the HP-filter trend fitted to the real mortgage rate. This trend real mortgage rate fell from 5.7% to 3.5%, which is a 39% drop.

The quantitative effects of each of these changes individually and taken together are shown in [Table 3](#). The assumption is that all changes are expected to be permanent. The combined effects are large: the calibrated model shows that macroeconomic variables can have a large impact on moving and buying decisions. As discussed earlier, it is changes in moving rates that are the main driver

²⁷[Harmon \(1988\)](#) finds an income elasticity of housing demand in the range 0.7–1.

²⁸The 10-year Treasury rate declined by a very similar amount, and inflation expectations as measured by the Michigan survey showed almost no change.

Table 2: *Calibrated parameters*

Parameter description	Notation	Value
<i>Parameters matching calibration targets</i>		
Arrival rate of shocks	a	0.13
Size of shocks	δ	0.86
Steady-state distribution of match quality	λ	13.9
Arrival rate of viewings	v	18.5
Total transaction cost	C	0.63
Flow search costs	F	0.16
Flow maintenance costs	M	0.28
<i>Directly measured parameters</i>		
Share of total transaction cost directly borne by seller	κ	1/3
Discount rate	r	0.057
<i>Imposed parameters</i>		
Bargaining power of seller	ω	1/2
Common component of homeowner flow value (normalization)	ξ	1

Notes: The parameters are chosen to match exactly the calibration targets in [Table 1](#).

of transactions in the longer term. The model is thus consistent with large changes in transactions precisely because it is able to explain large changes in moving rates.

The analysis assumes the observed change in the HP-filter trend of the real mortgage rate is permanent, which provides an upper bound for the effects of lower interest rates. It is debatable whether individuals at the time expected the decline in mortgage rates to be permanent (the HP-filter trend is estimated using data from 1971 to 2015, which has the benefit of hindsight). If mortgage rates were expected to be mean reverting, it would not be correct to take the observed change as permanent in the model.²⁹ For this reason, [Table 3](#) also reports the combined effects excluding the change in mortgage rates, which provides a lower bound for the combined effects taking account of possible mean reversion in mortgage rates. Excluding the effects coming from mortgage rates has a moderate impact on transactions and the moving rate, but has a much larger impact on prices and the sales rate. The predictions for the sales rate are worse compared to the data, but the predictions for house prices are much closer to the data.

As discussed earlier, easier access to credit might also be interpreted as a reduction in buyers' transaction costs C_b . This is more difficult to quantify. A 50% reduction is taken as an illustrative example and the results are reported in [appendix A.11](#). This change alone can account for a substantial increase in both the sales and moving rates (and consequently, transactions too), but its impact on price is muted.

Overall, the model does a fairly good job in explaining a significant fraction of the rise in the

²⁹[Glaeser, Gottlieb and Gyourko \(2010\)](#) argue that accounting for mean reversion in interest rates means that cheap credit explains only a small proportion of the boom in house prices.

Table 3: *Baseline results*

Factor	Transactions	Listings	Houses for sale	Sales rate	Moving rate	Prices
Productivity boom ($\xi \uparrow 25\%$)						
<i>Long run</i>	10%	10%	4%	6%	10%	41%
<i>Short run</i>	6%	12%	0%	6%	12%	41%
Internet search ($v \uparrow 33\%$)						
<i>Long run</i>	1%	1%	0%	1%	1%	3%
<i>Short run</i>	1%	15%	0%	1%	15%	3%
Mortgage rates ($r \downarrow 39\%$)						
<i>Long run</i>	6%	6%	18%	-10%	7%	64%
<i>Short run</i>	-10%	14%	0%	-10%	14%	64%
Combined effect						
<i>Long run</i>	14%	14%	22%	-6%	15%	140%
<i>Short run</i>	-6%	31%	0%	-6%	31%	140%
Excluding mortgage rates						
<i>Long run</i>	11%	11%	4%	6%	11%	46%
<i>Short run</i>	6%	24%	0%	6%	24%	46%
Data (1995-2004)	34%	37%	12%	22%	37%	45%

Notes: The combined effects are not the sum of the individual effects because the model is not linear.

moving rate through incentives for homeowners to invest in improving match quality (the responses of average match quality to ξ , v , and r are 1%, 2%, and 2% respectively, and 4% in total). The model generates substantial movements in house prices because productivity and mortgage rates have a large direct impact. This is especially true for mortgage rates, where the predicted changes in house prices are far in excess of what was observed, perhaps indicating the decline in mortgage rates was not expected to be permanent.

As discussed in [section 4.4](#), the model predicts overshooting in the moving rate due to the cleansing effect on the distribution of existing match quality. As seen in [Table 3](#), short-run (on impact) effects on moving rates and listings volume are more than double the long-run (steady-state) effects, so overshooting is quantitatively significant. Moreover, convergence to the new steady state is slow. Using the speed of convergence formulas from [section 4.4](#), it takes 5.8 years to go halfway to the new steady state. Note that the short-run effect on transactions is small because the stock of houses for sale does not immediately adjust. However, transactions quickly adjust in line with the short-run moving rate (because the new steady state for the stock of houses for sale is almost reached within one year). Consequently, transactions volume rises significantly in the medium term, overshooting its long-run level.

5.2.2 The role of endogenous moving

The results show that the endogenous moving model does a good job in accounting for the housing boom, but it is natural to ask what is its value added compared to a model where moving is exogenous. As explained in [section 4.6](#), exogenous moving is a special case of the model where $\delta = 0$.³⁰

The first two rows in [Table 4](#) show the combined effects across the endogenous and exogenous moving models (excluding the change in mortgage rates because of uncertainty about whether mean reversion was expected). The first row is the same as the combined effects reported in [Table 3](#), while the second row reports the results for the exogenous moving model. As in the endogenous moving model, house prices rise due to the direct effect of higher ξ . The sales rate actually falls in the exogenous moving model. But the key failure is in accounting for the rise in transactions in the absence of any change in the moving rate. The exogenous moving model essentially explains none of the change in transactions.

This analysis confirms the basic point that changes in the moving rate are necessary to explain the boom in transactions. However, it would be possible to have a model where the moving rate changes exogenously (by varying the arrival rate a of idiosyncratic shocks, which is identical to the moving rate in the exogenous moving model). The results are shown in the third row of [Table 4](#), where the size of the shock is set to match the observed change in transactions. By raising the moving rate significantly (almost matching the data), the exogenous moving model can replicate quantities very well. This is not surprising given the basic idea of this paper. However, the moving rate shock implies a decline in house prices because the effective discount rate $r + a$ increases. The exogenous moving model therefore cannot account for the developments in the housing market during this period without considering additional factors that would push up house prices. In any case, the endogenous moving model has shown that factors pushing up house prices can also explain the rise in the moving rate. In a similar vein, the advantages of the endogenous moving model are also apparent during the housing-market bust (because the same factors that push down house prices also imply a lower moving rate). A simple quantitative analysis of the bust period is presented in [section A.12](#).

The findings of [Table 4](#) confirm the claim that changes in the moving rate are essential to understand the boom and bust in housing market activity. Moreover, they show that simply imposing a moving rate shock on an exogenous model generates a negative co-movement between prices and transactions that is contrary to the data.

6 Conclusions

This paper presents evidence that aggregate housing-market dynamics are largely explained by changes in the frequency at which houses are put up for sale rather than changes in the length of

³⁰The exogenous moving model has the feature that average years of homeownership and the expected tenure of homeowners are identical. The calibration method is therefore adjusted so that this common number matches the average of the two targets reported in [Table 1](#). All other aspects of the calibration method are unchanged.

Table 4: *The role of endogenous moving*

Model	Transactions	Listings	Houses for sale	Sales rate	Moving rate	Prices
Endogenous moving						
<i>Long run</i>	11%	11%	4%	6%	11%	46%
<i>Short run</i>	6%	24%	0%	6%	24%	46%
Exogenous moving (I)						
<i>Long run</i>	0%	0%	1%	-1%	0%	46%
<i>Short run</i>	-1%	0%	0%	-1%	0%	46%
Exogenous moving (II)						
<i>Long run</i>	34%	34%	13%	19%	35%	-6%
<i>Short run</i>	35%	35%	0%	19%	35%	-6%
Data (1995-2004)	34%	37%	12%	22%	37%	45%

Notes: ‘Endogenous moving’ is the combined effect (excluding mortgage rates) given in Table 3. ‘Exogenous moving (I)’ is the combined effect when $\delta = 0$. ‘Exogenous moving (II)’ shows the effect of an increase in the moving rate a that matches the long-run increase in transactions.

time taken to sell them. Except for a relatively short transitional period (less than one year), even large changes in the sales rate have very little impact on transactions.

The paper builds a tractable model to analyse moving house where a homeowner’s decision to move is an investment in housing match quality. Since moving house is an investment with upfront costs and potentially long-lasting benefits, the model predicts that the aggregate moving rate depends on macroeconomic variables. The endogeneity of moving means that those who move come from the bottom of the existing match quality distribution, and the non-random selection of movers gives rise to a cleansing effect that leads to overshooting of housing-market variables. The calibrated model can successfully account for the key aggregate housing-market dynamics during the 1995-2004 boom.

References

- ALBRECHT, J., ANDERSON, A., SMITH, E. AND VROMAN, S. (2007), “[Opportunistic matching in the housing market](#)”, *International Economic Review*, **48(2)**:641–664 (May). 4
- ANENBERG, E. AND BAYER, P. (2013), “[Endogenous sources of volatility in housing markets: The joint buyer-seller problem](#)”, working paper 18980, NBER. 4
- ANENBERG, E. AND LAUFER, S. (2016), “A more timely house price index”, working paper, Federal Reserve Board. 28, 39
- BACHMANN, R. AND COOPER, D. (2014), “[The ins and arounds in the U.S. housing market](#)”, working paper 14–3, Federal Reserve Bank of Boston. 3, 8, 13, 25, 40

- CAPLIN, A. AND LEAHY, J. (2011), “Trading frictions and house price dynamics”, *Journal of Money, Credit and Banking*, **43(s2)**:283–303 (October). 4
- CASE, K. E. AND SHILLER, R. J. (2003), “Is there a bubble in the housing market?”, *Brookings Papers on Economic Activity*, **2003(2)**:299–342. 28
- COLES, M. G. AND SMITH, E. (1998), “Marketplaces and matching”, *International Economic Review*, **39(1)**:239–254 (February). 4
- DAVIS, M. A. AND VAN NIEUWERBURGH, S. (2014), “Housing, finance and the macroeconomy”, in G. Duranton, J. V. Henderson and W. C. Strange (eds.), *Handbook of Regional and Urban Economics*, vol. 5, forthcoming. 4
- DÍAZ, A. AND JEREZ, B. (2013), “House prices, sales, and time on the market: A search-theoretic framework”, *International Economic Review*, **54(3)**:837–872 (August). 4, 29
- FERREIRA, F., GYOURKO, J. AND TRACY, J. (2010), “Housing busts and household mobility”, *Journal of Urban Economics*, **68(1)**:34–45 (July). 1
- GENESOVE, D. AND HAN, L. (2012), “Search and matching in the housing market”, *Journal of Urban Economics*, **72(1)**:31–45 (July). 11, 12, 16, 28, 31
- GENESOVE, D. AND MAYER, C. J. (1997), “Equity and time to sell in the real estate market”, *American Economic Review*, **87(3)**:255–269 (June). 28, 39
- GERTLER, M. AND LEAHY, J. (2008), “A Phillips curve with an Ss foundation”, *Journal of Political Economy*, **116(3)**:533–572. 18
- GHENT, A. (2012), “Infrequent housing adjustment, limited participation, and monetary policy”, *Journal of Money, Credit and Banking*, **44(5)**:931–955 (August). 27
- GLAESER, E. L., GOTTLIEB, J. D. AND GYOURKO, J. (2010), “Can cheap credit explain the housing boom?”, working paper 16230, NBER. 32
- GLAESER, E. L. AND GYOURKO, J. (2007), “Arbitrage in housing markets”, working paper 13704, NBER. 13
- GUREN, A. M. (2014), “The causes and consequences of house price momentum”, working paper, Boston University. 4, 24
- HAN, L. AND STRANGE, W. C. (2014), “The microstructure of housing markets: Search, bargaining, and brokerage”, in G. Duranton, J. V. Henderson and W. C. Strange (eds.), *Handbook of Regional And Urban Economics*, vol. 5, forthcoming. 4
- HARMON, O. R. (1988), “The income elasticity of demand for single-family owner-occupied housing: An empirical reconciliation”, *Journal of Urban Economics*, **24(2)**:173–185 (September). 31
- HEAD, A., LLOYD-ELLIS, H. AND SUN, H. (2014), “Search, liquidity, and the dynamics of house prices and construction”, *American Economic Review*, **104(4)**:1172–1210 (April). 4
- HEDLUND, A. (2013), “Illiquidity and its discontents: Trading delays and foreclosures in the housing market”, working paper, University of Missouri. 4
- HENDEL, I., NEVO, A. AND ORTALO-MAGNÉ, F. (2009), “The relative performance of real estate marketing platforms: MLS versus FSBOMadison.com”, *American Economic Review*, **99(5)**:1878–1898 (December). 28

- HEUSON, A. J. AND PAINTER, G. (2014), “The impact of the Taxpayer Relief Act of 1997 on housing turnover in the U.S. single-family residential market”, *Real Estate Economics*, **42(4)**:869–899 (Winter). 26
- JOVANOVIC, B. (1979), “Job matching and the theory of turnover”, *Journal of Political Economy*, **87(5)**:972–990 (October). 15
- KARAHAN, F. AND RHEE, S. (2013), “Geographical reallocation and unemployment during the Great Recession: The role of the housing bust”, Staff report 605, Federal Reserve Bank of New York. 4
- KRAINER, J. (2001), “A theory of liquidity in residential real estate markets”, *Journal of Urban Economics*, **49(1)**:32–53 (January). 4
- LEVITT, S. D. AND SYVERSON, C. (2008), “Market distortions when agents are better informed: The value of information in real estate transactions”, *Review of Economics and Statistics*, **90(4)**:599–611 (November). 28, 39
- MERLO, A. AND ORTALO-MAGNÉ, F. (2004), “Bargaining over residential real estate: evidence from England”, *Journal of Urban Economics*, **56(2)**:192–216 (September). 29
- MOEN, E., NENOV, P. AND SNIKERS, F. (2014), “Buying first or selling first? Buyer-seller decisions and housing market volatility”, working paper, Norwegian Business School. 4
- MORTENSEN, D. T. AND PISSARIDES, C. A. (1994), “Job creation and job destruction in the theory of unemployment”, *Review of Economic Studies*, **61(3)**:397–415 (July). 23, 24
- NGAI, L. R. AND TENREYRO, S. (2014), “Hot and cold seasons in the housing market”, *American Economic Review*, **104(12)**:3991–4026 (December). 4
- NOVY-MARX, R. (2009), “Hot and cold markets”, *Real Estate Economics*, **37(1)**:1–22 (Spring). 4, 15
- PIAZZESI, M. AND SCHNEIDER, M. (2009), “Momentum traders in the housing market: Survey evidence and a search model”, *American Economic Review*, **99(2)**:406–411 (May). 4
- PIAZZESI, M., SCHNEIDER, M. AND STROEBEL, J. (2015), “Segmented housing search”, working paper 20823, NBER. 4
- PISSARIDES, C. A. (1985), “Short-run equilibrium dynamics of unemployment, vacancies and real wages”, *American Economic Review*, **75(4)**:676–690 (September). 15
- POTERBA, J. M. (1991), “House price dynamics: The role of tax policy and demography”, *Brookings Papers on Economic Activity*, **1991(2)**:143–203. 27
- QUIGLEY, J. M. (1987), “Interest rate variations, mortgage prepayments and household mobility”, *Review of Economics and Statistics*, **69(4)**:636–643 (November). 1
- (2002), “Transaction costs and housing markets”, in T. O’Sullivan and K. Gibb (eds.), *Housing Economics and Public Policy*, Blackwell, chap. 4, pp. 56–64. 27
- SHAN, H. (2011), “The effect of capital gains taxation on home sales: Evidence from the Taxpayer Relief Act of 1997”, *Journal of Public Economics*, **95(1–2)**:177–188 (February). 26

- WHEATON, W. C. (1990), “Vacancy, search, and prices in a housing market matching model”, *Journal of Political Economy*, **98(6)**:1270–1292 (December). 4
- WHEATON, W. C. AND LEE, N. J. (2009), “The co-movement of housing sales and housing prices: Empirics and theory”, working paper, MIT. 13

A Appendices

A.1 Listing and moving

This section addresses the concerns that listings N_t as measured by (2.4) do not perfectly correspond to moving because unsold houses might be withdrawn from the stock of houses for sale, or because transactions S_t and inventories I_t include non-owner-occupied houses.

Withdrawals

The effects of changes in the stock of owner-occupied houses have already been addressed in [section 2.2](#). To focus on the effects of withdrawals, this section assumed a fixed housing stock. Withdrawals can be explicitly introduced into the stock-flow accounting identity (2.1) as follows:

$$\dot{u}_t = n(1 - u_t) - (s + w)u_t,$$

where w is the rate at which houses are withdrawn from the stock of houses for sale because they fail to sell. Given s , n , g , and w , there is a steady state for the fraction of houses for sale:

$$u = \frac{n}{n + s + w},$$

and transactions S_t when u_t is at its steady-state value is:

$$S_t = \frac{sn}{s + n + w}.$$

The total derivative of transactions S_t is:

$$\frac{dS_t}{S_t} = \frac{s + w}{s + n + w} \frac{dn}{n} + \frac{n + w}{s + n + w} \frac{ds}{s} - \frac{w}{s + n + w} \frac{dw}{w}. \quad [\text{A.1.1}]$$

The relationship between the listings, transactions, and withdrawals in the steady state is:

$$S_t = N_t - W_t,$$

where W_t is the number of houses withdrawn from the market.

If the withdrawal rate were constant, its main effect is to change the average moving rate implied by the data, but this would have little impact on the changes over time seen in the measured moving rate. If the withdrawal rate were not constant over time then this would have an impact on the counterfactual exercise in [section 2.2](#) because a part of the measured increase in listings could actually be due to a decline in the withdrawal rate. As shown in equation (A.1.1), the contribution of changes in the withdrawal rate w to changes in transactions depends on the ratio $w/(s + n + w)$. The size of this ratio essentially depends on the size of w relative to s because n is small compared to s .

There is no consensus in the literature on how long it takes on average for a house to be withdrawn from the stock for sale if it is not sold. Using the MLS database between 2008–2012 for nine large MSAs, [Anenberg and Laufer \(2016\)](#) find that “the median property spends about eight weeks on the market before being delisted. Of those properties that are delisted, approximately half of them result in transactions. Many of the delistings that do not result in transactions are relisted soon after delisting which may be due to sales agreements that fall through because mortgage contingency or home inspection fails.” In other words, the withdrawal rate is unlikely to be larger than s , suggesting a maximum value of one for w/s . This is consistent with the fraction of withdrawals being between 22% and 50% according to the earlier findings of [Genesove and Mayer \(1997\)](#) and [Levitt and Syverson \(2008\)](#) using a smaller set of data.

Though the coefficient $w/(s + n + w)$ on changes in the withdrawal rate may not be insignificant, the contribution of withdrawals to changes in transactions depends crucially on how much the withdrawal rate has itself changed over time. It is not possible to obtain direct evidence on changes in w , but the direction of any potential bias is clear. Specifically, the contribution of the moving rate to changes in transactions

is overstated if the withdrawal rate was decreasing (increasing) during a period when transactions were increasing (decreasing).

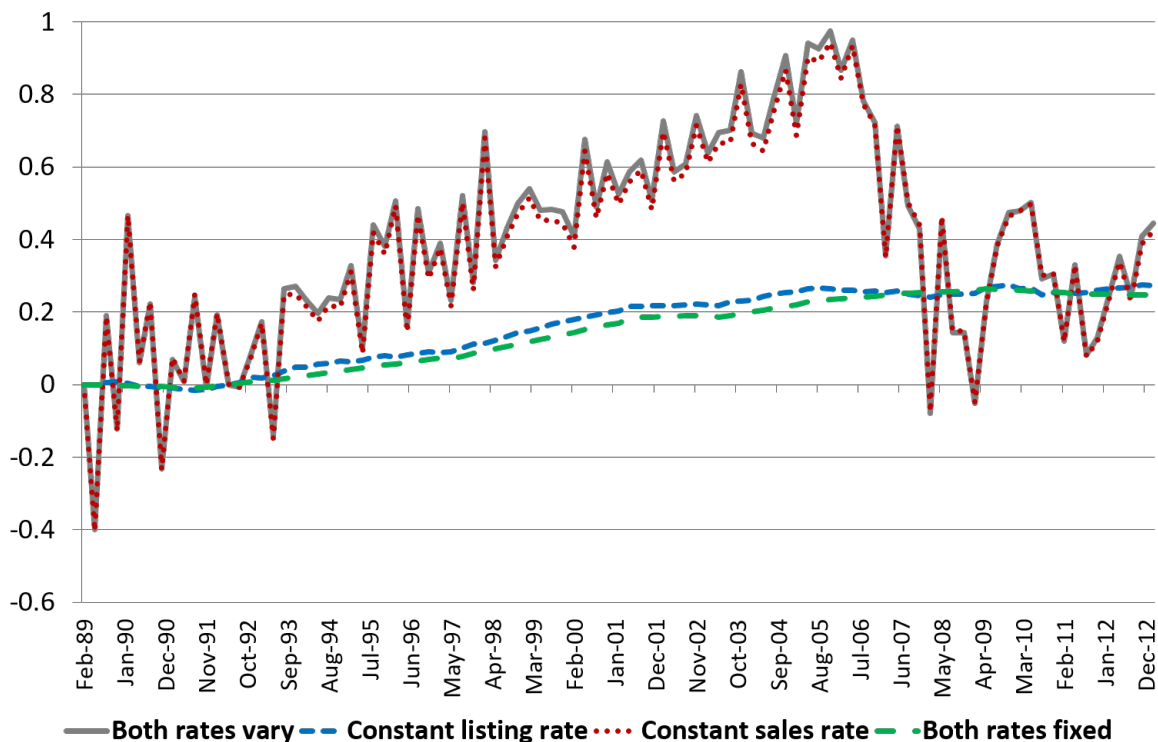
The analysis in [section 2.2](#) found that the listing rate increased by 37% during the boom period of 1995–2004. This implicitly assumed the withdrawal rate was constant. However, the finding is very close to the direct evidence from [Bachmann and Cooper \(2014\)](#) that the own-to-own moving rate increased by 33%, suggesting that any fall in the withdrawal rate during this period played only a limited role.

Measurement of transactions and inventories

The transactions and inventories data from NAR includes all existing single-family homes, so homes that are rented out are counted in this data. An estimate of the fraction of single-family homes that are not rented out can be computed from the AHS. This fraction is around 78% on average over the period 1989–2013. If the fraction were constant over time, the counterfactuals presented in [section 2.2](#) would be unaffected and the only change would be to the average level of the listing rate.

However, the data show some changes over time in the fraction of homes that are not rented out. The fraction rises from 77% to 80% during the boom period, and then falls to 75% by 2013. A simple robustness check is to scale the NAR data on transactions and inventories by the fraction of non-rented homes and then recompute the counterfactuals. The results are shown in [Figure 7](#), which are almost identical to those in [Figure 3](#).

Figure 7: Actual and counterfactual transactions (adjusted for rented homes)



Notes: The series are reported as log differences relative to their initial values.

A.2 Counterfactuals out of steady state

The counterfactuals in [section 2.2](#) assumed that the fraction of houses for sale was always at its steady-state level. While convergence to the steady state occurs at a fairly rapid rate (taking around a year), this section

repeats the counterfactual exercise without requiring that any variable remain at its steady state.

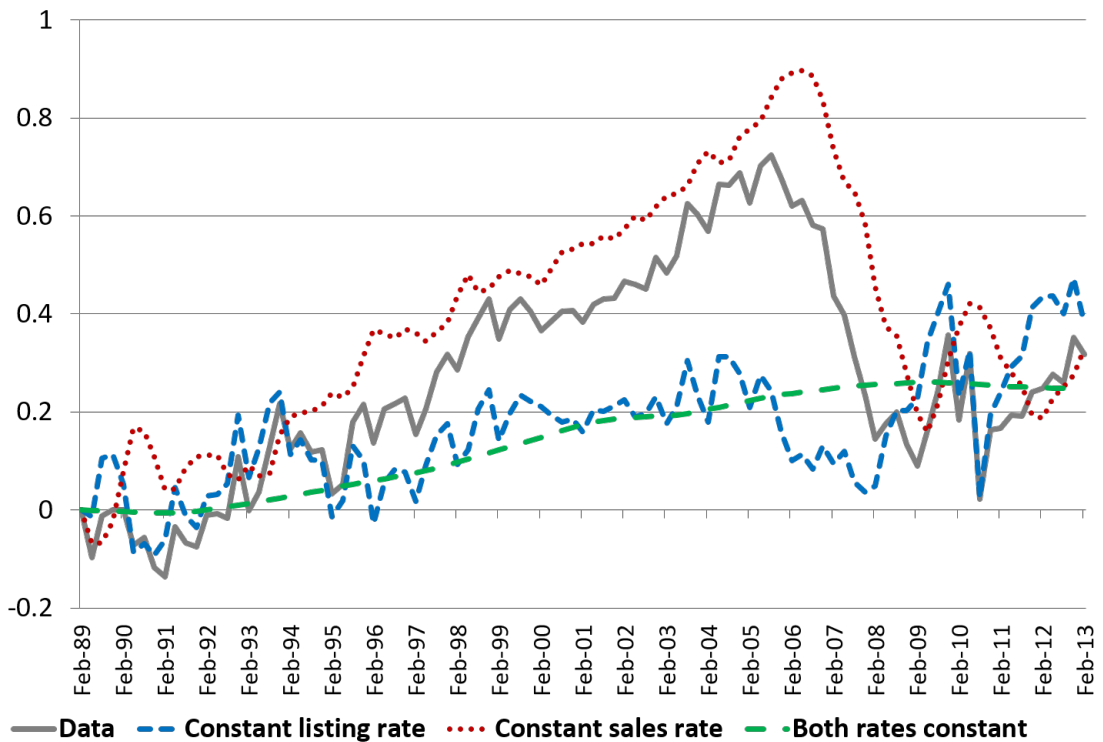
Note that equations (2.4) and (2.5) and the definitions of the sales and listing rates imply the following identity:

$$I_{t+1} = \frac{(1 - \frac{s_t+n_t}{2}) I_t + n_t K_t}{1 + \frac{s_t+n_t}{2}}. \quad [\text{A.2.1}]$$

Given time series for the sales rate s_t , the listing rate n_t , and the total housing stock K_t , this equation can be applied recursively to generate a series for inventories I_t starting from an initial value I_1 . The initial value of inventories is assumed to be at its steady state, that is, $I_1 = n_1 K_1 / (s_1 + n_1 + g_1)$, though for subsequent dates t there is no such requirement.

Two counterfactuals are generated using equation (A.2.1). The first holds the listing rate constant at its sample average ($n_t = \bar{n}$) while s_t varies as in the data, and the second holds the sales rate constant at its sample average ($s_t = \bar{s}$) while n_t varies as in the data. The equation is used to construct a hypothetical inventories series I_t given the assumed sales and listing rates. With this series, houses for sale U_t can be calculated using (2.5), which yields a counterfactual series for transactions using $S_t = s_t U_t$. The actual transactions series and the two counterfactuals are shown in Figure 8. The constant listing-rate counterfactual is largely unrelated to the actual transactions series. On the other hand, the counterfactual that completely ignores all variation in the sales rate is still able to reproduce most of the variation seen in the actual transactions series.

Figure 8: Actual and counterfactual transactions (out of steady state)



Notes: The series are plotted as log differences relative to their initial values.

A.3 Value functions and thresholds

Moving and transaction thresholds

The value functions $H_t(\epsilon)$ and W_t and the thresholds x_t and y_t satisfy the equations (3.1), (3.2), (3.5), and (3.6). No other variables appear in these equations. Given constant parameters, there is a time-invariant solution $H_t(\epsilon) = H(\epsilon)$, $W_t = W$, $x_t = x$, and $y_t = y$. The time-invariant equations are:

$$rH(\epsilon) = \epsilon\xi - M + a(\max\{H(\delta\epsilon), W\} - H(\epsilon)); \quad [\text{A.3.1}]$$

$$H(x) = W; \quad [\text{A.3.2}]$$

$$rW = -F - M + v \int_y^\infty (H(\epsilon) - W - C) dG(\epsilon); \quad [\text{A.3.3}]$$

$$H(y) = W + C. \quad [\text{A.3.4}]$$

Attention is restricted to parameters where the solution will satisfy $\delta y < x$.

Evaluating (A.3.1) at $\epsilon = x$, noting that $\delta < 1$ and $H(\epsilon)$ is increasing in ϵ :

$$rH(x) = \xi x - M + a(W - H(x)).$$

Since $H(x) = W$ (equation A.3.2), it follows that:

$$W = H(x) = \frac{\xi x - M}{r}. \quad [\text{A.3.5}]$$

Next, evaluate (A.3.1) at $\epsilon = y$. With the restriction $\delta y < x$, it follows that $H(\delta y) < H(x) = W$, and hence:

$$rH(y) = \xi y - M + a(W - H(y)).$$

Collecting terms in $H(y)$ on one side and substituting the expression for W from (A.3.5):

$$(r + a)H(y) = \xi y - M + \frac{a}{r}(\xi x - M) = \xi(y - x) + \left(1 + \frac{a}{r}\right)(\xi x - M),$$

and thus $H(y)$ is given by:

$$H(y) = \frac{\xi x - M}{r} + \frac{\xi(y - x)}{r + a}. \quad [\text{A.3.6}]$$

Combining the equation above with (A.3.4) and (A.3.5), it can be seen that the thresholds y and x must be related as follows:

$$y - x = \frac{(r + a)C}{\xi}. \quad [\text{A.3.7}]$$

Using the expression for the Pareto distribution function (3.3) and using (A.3.4) to note $H(\epsilon) - W - C = H(\epsilon) - H(y)$, the Bellman equation (A.3.3) can be written as:

$$rW = -F - M + v y^{-\lambda} \int_{\epsilon=y}^\infty \frac{\lambda}{y} \left(\frac{\epsilon}{y}\right)^{-(\lambda+1)} (H(\epsilon) - H(y)) d\epsilon, \quad [\text{A.3.8}]$$

which assumes $y > 1$. In solving this equation it is helpful to define the following function $\Psi(z)$ for all $z \leq y$:

$$\Psi(z) \equiv \int_{\epsilon=z}^\infty \frac{\lambda}{z} \left(\frac{\epsilon}{z}\right)^{-(\lambda+1)} (H(\epsilon) - H(z)) d\epsilon. \quad [\text{A.3.9}]$$

Since $\delta y < x$ is assumed and $z \leq y$, it follows that $\delta z < x$, and thus $H(\delta z) < H(x) = W$. Equation (A.3.1) evaluated at $\epsilon = z$ therefore implies:

$$rH(z) = \xi z - M + a(W - H(z)).$$

Subtracting this equation from (A.3.1) evaluated at a general value of ϵ leads to:

$$\begin{aligned} r(H(\epsilon) - H(z)) &= \xi(\epsilon - z) + a(\max\{H(\delta\epsilon), W\} - H(\epsilon)) - a(W - H(z)) \\ &= \xi(\epsilon - z) - a(H(\epsilon) - H(z)) + a\max\{H(\delta\epsilon) - W, 0\}. \end{aligned}$$

Noting that $W = H(x)$ and solving for $H(\epsilon) - H(z)$:

$$H(\epsilon) - H(z) = \frac{\xi}{r+a}(\epsilon - z) + \frac{a}{r+a}\max\{H(\delta\epsilon) - H(x), 0\}. \quad [\text{A.3.10}]$$

The equation above can be substituted into (A.3.9) to deduce:

$$\Psi(z) = \frac{\xi}{r+a} \int_{\epsilon=z}^{\infty} \frac{\lambda}{z} \left(\frac{\epsilon}{z}\right)^{-(\lambda+1)} (\epsilon - z) d\epsilon + \frac{a}{r+a} \int_{\epsilon=z}^{\infty} \frac{\lambda}{z} \left(\frac{\epsilon}{z}\right)^{-(\lambda+1)} \max\{H(\delta\epsilon) - H(x), 0\} d\epsilon. \quad [\text{A.3.11}]$$

First, observe that:

$$\int_{\epsilon=z}^{\infty} \frac{\lambda}{z} \left(\frac{\epsilon}{z}\right)^{-(\lambda+1)} (\epsilon - z) d\epsilon = \frac{z}{\lambda - 1}. \quad [\text{A.3.12}]$$

Next, make the change of variable $\epsilon' = \delta\epsilon$ in the second integral in (A.3.11) to deduce:

$$\begin{aligned} \int_{\epsilon=z}^{\infty} \frac{\lambda}{z} \left(\frac{\epsilon}{z}\right)^{-(\lambda+1)} \max\{H(\delta\epsilon) - H(x), 0\} d\epsilon &= \int_{\epsilon'=\delta z}^{\infty} \frac{\lambda}{\delta z} \left(\frac{\epsilon'}{\delta z}\right)^{-(\lambda+1)} \max\{H(\epsilon') - H(x), 0\} d\epsilon' \\ &= \int_{\epsilon'=\delta z}^x \frac{\lambda}{\delta z} \left(\frac{\epsilon'}{\delta z}\right)^{-(\lambda+1)} 0 d\epsilon' + \int_{\epsilon'=x}^{\infty} \frac{\lambda}{\delta z} \left(\frac{\epsilon'}{\delta z}\right)^{-(\lambda+1)} (H(\epsilon') - H(x)) d\epsilon' \\ &= \left(\frac{\delta z}{x}\right)^{\lambda} \int_{\epsilon=x}^{\infty} \frac{\lambda}{x} \left(\frac{\epsilon}{x}\right)^{-(\lambda+1)} (H(\epsilon) - H(x)) d\epsilon = \left(\frac{\delta z}{x}\right)^{\lambda} \Psi(x), \end{aligned}$$

where the second line uses $\delta z < x$ (as $z \leq y$ and $\delta y < x$) and $H(\epsilon') < H(x)$ for $\epsilon' < x$, and the final line uses the definition (A.3.9). Putting the equation above together with (A.3.11) and (A.3.12) yields the following for all $z \leq y$:

$$\Psi(z) = \frac{\xi z}{(r+a)(\lambda-1)} + \frac{a}{r+a} \left(\frac{\delta z}{x}\right)^{\lambda} \Psi(x). \quad [\text{A.3.13}]$$

Evaluating this expression at $z = x$ (with $x < y$):

$$\Psi(x) = \frac{\xi x}{(r+a)(\lambda-1)} + \frac{a}{r+a} \delta^{\lambda} \Psi(x),$$

and hence $\Psi(x)$ is given by:

$$\Psi(x) = \frac{\xi x}{(r+a(1-\delta^{\lambda}))(\lambda-1)}. \quad [\text{A.3.14}]$$

Next, evaluating (A.3.13) at $z = y$ and using (A.3.14) to substitute for $\Psi(x)$:

$$\Psi(y) = \frac{\xi y}{(r+a)(\lambda-1)} + \frac{a}{r+a} \left(\frac{\delta z}{x}\right)^{\lambda} \left(\frac{\xi x}{(r+a(1-\delta^{\lambda}))(\lambda-1)}\right),$$

and simplifying this equation yields the following expression for $\Psi(y)$:

$$\Psi(y) = \frac{\xi}{(r+a)(\lambda-1)} \left(y + \frac{a\delta^{\lambda}y^{\lambda}x^{1-\lambda}}{r+a(1-\delta^{\lambda})}\right). \quad [\text{A.3.15}]$$

Using the definition (A.3.9), equation (A.3.8) can be written in terms of $\Psi(y)$:

$$rW = -F - M + vy^{-\lambda}\Psi(y),$$

and substituting from (A.3.5) and (A.3.15) yields:

$$\xi x - M = -F - M + vy^{-\lambda} \left(\frac{\xi}{(r+a)(\lambda-1)} \left(y + \frac{a\delta^\lambda y^\lambda x^{1-\lambda}}{r+a(1-\delta^\lambda)} \right) \right).$$

This equation can be simplified as follows:

$$x + \frac{F}{\xi} = \frac{v}{(\lambda-1)(r+a)} \left(y^{1-\lambda} + \frac{a\delta^\lambda}{r+a(1-\delta^\lambda)} x^{1-\lambda} \right). \quad [\text{A.3.16}]$$

The two equations (A.3.7) and (A.3.16) confirm (4.4) and (4.7) given in the main text. These can be solved for the thresholds x and y .

Existence and uniqueness

By using equation (A.3.7) to replace x with a linear function of y , the equilibrium threshold y is the solution of the equation:

$$\mathcal{I}(y) \equiv \frac{v}{(\lambda-1)(r+a)} \left(y^{1-\lambda} + \frac{a\delta^\lambda}{r+a(1-\delta^\lambda)} \left(y - \frac{(r+a)C}{\xi} \right)^{1-\lambda} \right) - y + \frac{(r+a)C}{\xi} - \frac{F}{\xi} = 0. \quad [\text{A.3.17}]$$

It can be seen immediately (since $\lambda > 1$) that $\mathcal{I}'(y) < 0$, so any solution that exists is unique. A valid solution must satisfy $x > 0$, $y > 1$, and $\delta y < x$. Using equation (A.3.7), the inequality $\delta y < x$ is equivalent to:

$$\delta y < y - \frac{(r+a)C}{\xi},$$

which is in turn equivalent to:

$$y > \frac{(r+a)C}{(1-\delta)\xi}.$$

Thus, to satisfy $y > 1$ and $\delta y < x$, the equilibrium must feature:

$$y > \max \left\{ 1, \frac{(r+a)C}{(1-\delta)\xi} \right\}. \quad [\text{A.3.18}]$$

Observe that $\lim_{y \rightarrow \infty} \mathcal{I}(y) = -\infty$ (using A.3.17 and $\lambda > 1$), so an equilibrium satisfying (A.3.18) exists if and only if:

$$\mathcal{I} \left(\max \left\{ 1, \frac{(r+a)C}{(1-\delta)\xi} \right\} \right) > 0. \quad [\text{A.3.19}]$$

If the condition (A.3.18) is satisfied then by using (A.3.7):

$$x > \max \left\{ 1, \frac{(r+a)C}{(1-\delta)\xi} \right\} - \frac{(r+a)C}{\xi} > \frac{(r+a)C}{(1-\delta)\xi} - \frac{(r+a)C}{\xi} = \frac{\delta(r+a)C}{(1-\delta)\xi} > 0,$$

confirming that $x > 0$ must hold. Therefore, (A.3.19) is necessary and sufficient for the existence of a unique equilibrium satisfying all the required conditions. Using equation (A.3.17), (A.3.19) is equivalent to the condition in (4.8).

Surplus and selling rate

Given x and y , the value functions W , $H(x)$, and $H(y)$ can be obtained from (A.3.5) and (A.3.6). The average surplus can be found by combining (A.3.5) and (A.3.8) to deduce:

$$\int_{\epsilon=y}^{\infty} \frac{\lambda}{y} \left(\frac{\epsilon}{y}\right)^{-(\lambda+1)} (H(\epsilon) - H(y)) d\epsilon = \frac{y^\lambda}{v} (\xi x + F). \quad [\text{A.3.20}]$$

Given x and y , the probability π that a viewing leads to a sale, and the expected number of viewings before a sale $V_s = 1/\pi$ are:

$$\pi = y^{-\lambda}, \quad \text{and} \quad V_s = y^\lambda. \quad [\text{A.3.21}]$$

The selling rate s and the expected time-to-sell $T_s = 1/s$ are given by:

$$s = v y^{-\lambda}, \quad \text{and} \quad T_s = \frac{y^\lambda}{v}. \quad [\text{A.3.22}]$$

A.4 Prices

Nash bargaining

The price $p_t(\epsilon)$ is determined by combining the Nash bargaining solution $\omega \Sigma_{b,t}(\epsilon) = (1 - \omega) \Sigma_{u,t}(\epsilon)$ with the expressions for the buyer and seller surpluses in (3.7):

$$\omega(H_t(\epsilon) - p_t(\epsilon) - (1 - \kappa)C - B_t) = (1 - \omega)(p_t(\epsilon) - \kappa C - U_t),$$

from which it follows that:

$$p_t(\epsilon) = \omega H_t(\epsilon) + (\kappa - \omega)C + ((1 - \omega)U_t - \omega B_t). \quad [\text{A.4.1}]$$

The surplus-splitting condition implies $\Sigma_{b,t}(\epsilon) = (1 - \omega) \Sigma_t(\epsilon)$ and $\Sigma_{u,t}(\epsilon) = \omega \Sigma_t(\epsilon)$, with $\Sigma_t(\epsilon) = \Sigma_{b,t}(\epsilon) + \Sigma_{u,t}(\epsilon)$ being the total surplus from (4.6). The Bellman equations in (3.8) can thus be written as:

$$rB_t = -F + (1 - \omega)v \int_{y_t} \Sigma_t(\epsilon) dG(\epsilon) + \dot{B}_t, \quad \text{and} \quad rU_t = -M + \omega v \int_{y_t} \Sigma_t(\epsilon) dG(\epsilon) + \dot{U}_t,$$

and a multiple ω of the first equation can be subtracted from a multiple $1 - \omega$ of the second equation to deduce:

$$r((1 - \omega)U_t - \omega B_t) = \omega F - (1 - \omega)M + ((1 - \omega)\dot{U}_t - \omega\dot{B}_t).$$

The stationary solution of this equation is:

$$(1 - \omega)U_t - \omega B_t = \frac{\omega F - (1 - \omega)M}{r},$$

and by substituting this into (A.4.1):

$$p_t(\epsilon) = \omega H_t(\epsilon) + (\kappa - \omega)C + \frac{\omega F - (1 - \omega)M}{r}. \quad [\text{A.4.2}]$$

Integrating this equation over the distribution of new match quality yields equation (3.9) for the average transaction price.

Average transactions price

In an equilibrium where the moving and transactions thresholds x_t and y_t are constant over time, the value function $H_t(\epsilon)$ is equal to the time-invariant function $H(\epsilon)$. This means that prices $p_t(\epsilon) = p(\epsilon)$ are also

time invariant. Using the Pareto distribution function (3.3) and equation (3.9), the average price is:

$$P = \omega \int_y \frac{\lambda}{y} \left(\frac{\epsilon}{y} \right)^\lambda H(\epsilon) d\epsilon + (\kappa - \omega)C + \frac{\omega F - (1 - \omega)M}{r}.$$

By using the expression for $H(y)$ in (A.3.6), the above can be written as:

$$P = \omega \int_y \frac{\lambda}{y} \left(\frac{\epsilon}{y} \right)^\lambda (H(\epsilon) - H(y)) d\epsilon + \omega \left(\frac{\xi x - M}{r} + \frac{\xi(y - x)}{r + a} \right) + (\kappa - \omega)C + \frac{\omega F - (1 - \omega)M}{r},$$

and substituting from (A.3.7) and (A.3.20) yields:

$$P = \omega \frac{y^\lambda}{v} (\xi x + F) + \omega C + \frac{\omega \xi x}{r} + (\kappa - \omega)C + \frac{\omega F - M}{r}.$$

Therefore, the following expression for the average price is obtained:

$$P = \kappa C - \frac{M}{r} + \omega \left(\frac{1}{r} + \frac{y^\lambda}{v} \right) (\xi x + F). \quad [\text{A.4.3}]$$

This leads to expressions for the ratios of costs (search, transactions, and maintenance) to the average price:

$$f = \frac{\frac{F}{\xi}}{\kappa \frac{C}{\xi} - \frac{M}{r\xi} + \omega \left(\frac{1}{r} + \frac{y^\lambda}{v} \right) \left(x + \frac{F}{\xi} \right)}; \quad [\text{A.4.4a}]$$

$$c = \frac{\frac{C}{\xi}}{\kappa \frac{C}{\xi} - \frac{M}{r\xi} + \omega \left(\frac{1}{r} + \frac{y^\lambda}{v} \right) \left(x + \frac{F}{\xi} \right)}; \quad [\text{A.4.4b}]$$

$$m = \frac{\frac{M}{\xi}}{\kappa \frac{C}{\xi} - \frac{M}{r\xi} + \omega \left(\frac{1}{r} + \frac{y^\lambda}{v} \right) \left(x + \frac{F}{\xi} \right)}. \quad [\text{A.4.4c}]$$

A.5 Stocks and flows

The moving rate

The formula (3.12) for the moving rate can also be given in terms of inflows $N_t = n_t(1 - u_t)$, where u_t is the stock of unsold houses:

$$N_t = a(1 - u_t) - a\delta^\lambda x_t^{-\lambda} v \int_{\tau \rightarrow -\infty}^{\infty} e^{-a(1-\delta^\lambda)(t-\tau)} u_\tau d\tau. \quad [\text{A.5.1}]$$

The first term $a(1 - u_t)$ is the quantity of existing matches that receive a shock (arrival rate a). The second term is the quantity of existing matches that receive a shock now, but decide not to move. The difference between these two numbers (under the assumption that only those who receive a shock make a moving decision) gives inflows N_t .

Now consider the derivation of the second term in (A.5.1). The distribution of existing matches (measure $1 - u_t$) can be partitioned into vintages τ (when matches formed) and the number k of previous shocks that have been received. At time τ , a quantity u_τ of houses were for sale, and viewings arrived at rate v . Viewings were draws of match quality ϵ from a Pareto(1, λ) distribution, and those draws with $\epsilon \geq y_\tau$ formed new matches, truncating the distribution at y_τ . In the interval between τ and t , those matches that have received k shocks now have match quality $\delta^k \epsilon$. Some of these matches will have been destroyed as a result of these shocks, truncating the distribution of surviving match quality. Because the distribution of initial match quality is a Pareto distribution, these truncations also result in Pareto distributions with the same shape parameter λ .

Consider the matches of vintage τ . All of these were originally from a Pareto distribution truncated at $\epsilon \geq y_\tau$. Subsequently, depending on the arrival of idiosyncratic shocks (both timing and number), this distribution may have been truncated further. Let z denote the last truncation point in terms of the original match quality ϵ (at the time of the viewing). This is $z = y_\tau$ if no shocks have been received, or $z = \delta^{-k}x_T$ if k shocks have been received and the last one occurred at time T when the moving threshold was x_T . Conditional on this last truncation point z , it is shown below that the measure of surviving matches is $z^{-\lambda}vu_\tau$. Furthermore, the original match quality of these surviving matches must be a Pareto(z, λ) distribution.

Now consider the distribution of the number of previous shocks k between τ and t . Given the Poisson arrival rate a , k has a Poisson distribution, so the probability of k is $e^{-a(t-\tau)}(a(t-\tau))^k/k!$. If a shock arrives at time t , matches of current quality greater than x_t survive. If these have received k shocks earlier, this means the truncation threshold in terms of original match quality ϵ is $\epsilon \geq \delta^{-(k+1)}x_t$. Of these matches that have accumulated k earlier shocks, suppose last relevant truncation threshold (in terms of original match quality) was z (this will vary over those matches even with the same number of shocks because the timing might be different), so the distribution of surviving matches in terms of their original match quality is Pareto(z, λ). The probability that these matches then survive the shock at time t is given by $(\delta^{-(k+1)}x_t/z)^{-\lambda}$, and multiplying this by $z^{-\lambda}vu_\tau$ gives the number that survive:

$$(\delta^{-(k+1)}x_t/z)^{-\lambda}z^{-\lambda}vu_\tau = (\delta^\lambda)^{k+1}x_t^{-\lambda}vu_\tau,$$

noting that the terms in z cancel out. This is conditional on z , k , and τ , but since z does not appear above, the distribution of the past truncation thresholds is not needed. Averaging over the distribution of k yields:

$$\begin{aligned} \sum_{k=0}^{\infty} e^{-a(t-\tau)} \frac{(a(t-\tau))^k}{k!} (\delta^\lambda)^{k+1} x_t^{-\lambda} vu_\tau &= \delta^\lambda x_t^{-\lambda} vu_\tau e^{-a(t-\tau)} \sum_{k=0}^{\infty} \frac{(a\delta^\lambda(t-\tau))^k}{k!} \\ &= \delta^\lambda x_t^{-\lambda} vu_\tau e^{-a(t-\tau)} e^{a\delta^\lambda(t-\tau)} = \delta^\lambda x_t^{-\lambda} vu_\tau e^{-a(1-\delta^\lambda)(t-\tau)}, \end{aligned}$$

where the penultimate expression uses the Taylor series expansion of the exponential function $e^z = \sum_{k=0}^{\infty} z^k/k!$ (valid for all z). Next, integrating over all vintages τ before the current time t leads to:

$$\int_{\tau \rightarrow -\infty}^t \delta^\lambda x_t^{-\lambda} e^{-a(1-\delta^\lambda)(t-\tau)} d\tau = \delta^\lambda x_t^{-\lambda} \int_{\tau \rightarrow -\infty}^t e^{-a(1-\delta^\lambda)(t-\tau)} vu_\tau d\tau.$$

Multiplying this by the arrival rate a of the idiosyncratic shocks confirms the second term of the expression for N_t in (A.5.1).

This leaves only the claim that the measure of vintage- τ surviving matches with truncation point z (in terms of the original match quality distribution ϵ) is $z^{-\lambda}vu_\tau$. When these matches first form, they have measure $y_\tau^{-\lambda}vu_\tau$ and a Pareto(y_t, λ) distribution, so the formula is correct if no shocks have occurred and $z = y_\tau$. Now suppose the formula is valid for some z and truncation now occurs at a new point $w > z$ (in terms of original match quality). Since matches surviving truncation at z have distribution Pareto(z, λ), the proportion of these that survive the new truncation is $(w/z)^{-\lambda}$, and so the measure becomes $(w/z)^{-\lambda}z^{-\lambda}vu_\tau = w^{-\lambda}vu_\tau$ (with the term in z cancelling out), which confirms the claim.

The distribution of match quality

Now consider the derivation of the law of motion for average match quality Q_t in (3.13). Let total match quality across all families be denoted by \mathcal{E}_t (those not matched have match quality equal to zero), with $\mathcal{E}_t = (1 - u_t)Q_t$ by definition. Total match quality \mathcal{E}_t changes over time as new matches form, when matches are hit by shocks, and when moving decisions are made. With transaction threshold y_t and new match quality drawn from a Pareto(1; λ) distribution, new matches have average quality $(\lambda/(\lambda - 1))y_t$. The contribution to the rate of change of total match quality is that average multiplied by $s_t u_t$. Shocks to existing matches arrive randomly at rate a . If no shock is received then there is no change to match quality

and no moving decision. For those who receive a shock, let $\underline{\mathcal{E}}_t$ denote the total match quality of those matches that survive (with matches that dissolve counted as having zero match quality). The contribution of the shocks and moving decisions to the rate of change of total match quality is to subtract $a(\mathcal{E}_t - \underline{\mathcal{E}}_t)$. The differential equation for \mathcal{E}_t is therefore:

$$\dot{\mathcal{E}}_t = \frac{\lambda}{\lambda - 1} y_t s_t u_t - a(\mathcal{E}_t - \underline{\mathcal{E}}_t). \quad [\text{A.5.2}]$$

Using this formula requires an expression for $\underline{\mathcal{E}}_t$.

Consider the distribution of all matches that formed before time t , survived until time t , and now receive an idiosyncratic shock at time t , but one that is not sufficient to trigger moving. The distribution of surviving matches can be partitioned into vintages τ (when the match formed) and the number of shocks k that have been received previously (not counting the shock at time t). At time τ , a quantity u_τ of houses were for sale, and viewings arrived at rate v . Viewings were draws of match quality ϵ from a Pareto(1; λ) distribution, and those draws with $\epsilon \geq y_\tau$ formed new matches, truncating the distribution at y_τ . Subsequently, a number k of idiosyncratic shocks have occurred, with k having a Poisson($a(t - \tau)$) distribution, and these shocks resulting in the distribution of surviving match quality being truncated. With a shock now occurring at time t after k earlier shocks, match quality is now $\delta^{k+1}\epsilon$, and the distribution is truncated at x_t . In terms of the original match quality ϵ , survival requires $\epsilon \geq \delta^{-(k+1)}x_t$.

Consider matches of vintage τ that have previously accumulated k shocks for which the last truncation threshold was z in terms of original match quality (this threshold will depend on when the previous shocks occurred). Since the Pareto distribution is preserved after truncation with the same shape parameter, these matches have a Pareto(z ; λ) distribution in terms of their original match quality. It was shown above that the measure of surviving vintage- τ matches with truncation point z is $z^{-\lambda} v u_\tau$ (conditional on z , the number of shocks k is irrelevant, though the number of shocks may be related to the value of z). The measure that remain ($\epsilon \geq \delta^{-(k+1)}x_t$) after moving decisions are made at time t is:

$$\left(\delta^{-(k+1)}x_t/z\right)^{-\lambda} z^{-\lambda} v u_\tau = (\delta^\lambda)^{k+1} x_t^{-\lambda} v u_\tau,$$

noting that the terms in z cancel out. The probability of drawing k shocks in the interval between τ and t is $e^{-a(t-\tau)}(a(t-\tau))^k/k!$, and hence averaging over the distribution of k for vintage- τ matches implies that the surviving measure is:

$$\sum_{k=0}^{\infty} e^{-a(t-\tau)} \frac{(a(t-\tau))^k}{k!} (\delta^{k+1})^\lambda x_t^{-\lambda} v u_\tau = \delta^\lambda x_t^{-\lambda} v u_\tau e^{-a(1-\delta^\lambda)(t-\tau)},$$

which is confirmed by following the same steps as in the derivation of the moving rate above. Integrating these surviving measures over all cohorts:

$$\int_{\tau \rightarrow -\infty}^t \delta^\lambda x_t^{-\lambda} v u_\tau e^{-a(1-\delta^\lambda)(t-\tau)} d\tau = v \delta^\lambda x_t^{-\lambda} \int_{\tau \rightarrow -\infty}^t e^{-a(1-\delta^\lambda)(t-\tau)} u_\tau d\tau,$$

and since the average match quality among the survivors after the shock at time t is $(\lambda/(\lambda - 1))x_t$ for all cohorts, it follows that:

$$\underline{\mathcal{E}}_t = \frac{v \delta^\lambda \lambda}{\lambda - 1} x_t^{1-\lambda} \int_{\tau \rightarrow -\infty}^t e^{-a(1-\delta^\lambda)(t-\tau)} u_\tau d\tau.$$

Substituting this and equation (3.11) into (A.5.2) implies:

$$\dot{\mathcal{E}}_t = \frac{v \lambda}{\lambda - 1} y_t^{1-\lambda} u_t - a \left(\mathcal{E}_t - \frac{v \delta^\lambda \lambda}{\lambda - 1} x_t^{1-\lambda} \int_{\tau \rightarrow -\infty}^t e^{-a(1-\delta^\lambda)(t-\tau)} u_\tau d\tau \right). \quad [\text{A.5.3}]$$

The integral can be eliminated by defining an additional variable Z_t :

$$Z_t = \int_{\tau \rightarrow -\infty}^t e^{-a(1-\delta^\lambda)(t-\tau)} u_\tau d\tau, \quad [\text{A.5.4}]$$

and hence (A.5.3) can be written as follows:

$$\dot{\mathcal{E}}_t = \frac{v\lambda}{\lambda-1} y_t^{1-\lambda} u_t - a\mathcal{E}_t + \frac{av\delta^\lambda \lambda}{\lambda-1} x_t^{1-\lambda} Z_t. \quad [\text{A.5.5}]$$

The evolution of the state variable u_t is determined by combining equations (3.10), (3.11), and (3.12):

$$\dot{u}_t = a(1-u_t) - av\delta^\lambda x_t^{-\lambda} \int_{\tau \rightarrow -\infty}^t e^{-a(1-\delta^\lambda)(t-\tau)} u_\tau d\tau - v y_t^{-\lambda} u_t,$$

where the integral can again be eliminated by writing the equation in terms of the new variable Z_t from (A.5.4):

$$\dot{u}_t = a(1-u_t) - av\delta^\lambda x_t^{-\lambda} Z_t - v y_t^{-\lambda} u_t. \quad [\text{A.5.6}]$$

Differentiating the integral in (A.5.4) shows that Z_t must satisfy the differential equation:

$$\dot{Z}_t = u_t - a(1-\delta^\lambda)Z_t. \quad [\text{A.5.7}]$$

These results can be used to obtain the differential equation for average match quality Q_t in (3.13). Since the definition implies $Q_t = \mathcal{E}_t/(1-u_t)$, it follows that:

$$\dot{Q}_t = \frac{\dot{\mathcal{E}}_t}{1-u_t} + \frac{\mathcal{E}_t \dot{u}_t}{(1-u_t)^2} = \frac{\dot{\mathcal{E}}_t}{1-u_t} + Q_t \frac{\dot{u}_t}{1-u_t}.$$

Substituting from the differential equations (A.5.5) and (A.5.6) leads to:

$$\dot{Q}_t = \left(\frac{v\lambda}{\lambda-1} y_t^{1-\lambda} \frac{u_t}{1-u_t} - aQ_t + \frac{av\delta^\lambda \lambda}{\lambda-1} x_t^{1-\lambda} \frac{Z_t}{1-u_t} \right) + Q_t \left(a - av\delta^\lambda x_t^{-\lambda} \frac{Z_t}{1-u_t} - v y_t^{-\lambda} \frac{u_t}{1-u_t} \right),$$

noting that the terms in Q_t on the right-hand side cancel out, so \dot{Q}_t can be written as:

$$\dot{Q}_t = v y_t^{-\lambda} \left(\frac{\lambda}{\lambda-1} y_t - Q_t \right) \frac{u_t}{1-u_t} - \frac{av\delta^\lambda x_t^{-\lambda} Z_t}{1-u_t} \left(Q_t - \frac{\lambda}{\lambda-1} x_t \right).$$

Comparison with equations (3.11), (3.12), and the definition of Z_t in (A.5.4) confirms the differential equation for Q_t in (3.13).

The distribution of time spent in a house

Now consider an equilibrium where parameters are expected to remain constant. In this case, the moving and transaction thresholds x and y are constant over time. Let $\psi(\tau)$ denote the survival function for new matches, in the sense of the fraction of matches forming at time t that survive until at least $t + \tau$. Each cohort starts with a match quality distribution $\epsilon \sim \text{Pareto}(y; \lambda)$ at $\tau = 0$. Now consider some $\tau > 0$. Moving occurs only if the value of ϵ after shocks have occurred (ϵ') is such that $\epsilon' < x$. Shocks arrive at a Poisson rate a , so the number k of shocks that would occur to a match over an interval of time τ has a $\text{Poisson}(a\tau)$ distribution, which means the probability that k shocks occur is $e^{-a\tau} (a\tau)^k / k!$. If no shocks occur, $\epsilon' = \epsilon$, so no moving occurs. If $k \geq 1$ shocks have occurred then $\epsilon' = \delta^k \epsilon$, where ϵ is the initial draw of match quality. These matches survive only if $\epsilon' \geq x$, that is, $\epsilon \geq x/\delta^k$. Since the original values of ϵ are drawn from a Pareto distribution truncated at $\epsilon = y$ with shape parameter λ , this probability is $((x/\delta^k)/y)^{-\lambda}$ (this expression is valid for all $k \geq 1$ since $\delta y < x$). Therefore, the survival function is given

by:

$$\psi(\tau) = e^{-a\tau} + \sum_{k=1}^{\infty} e^{-a\tau} \frac{(a\tau)^k}{k!} \left(\frac{x/\delta^k}{y}\right)^{-\lambda} = e^{-a\tau} + \left(\frac{y}{x}\right)^{\lambda} e^{-a\tau} \sum_{k=1}^{\infty} \frac{(a\delta^{\lambda}\tau)^k}{k!} = e^{-a\tau} + \left(\frac{y}{x}\right)^{\lambda} e^{-a\tau} e^{a\delta^{\lambda}\tau},$$

where the final equality uses the (globally convergent) series expansion of the exponential function. The survival function is thus:

$$\psi(\tau) = \left(1 - \left(\frac{y}{x}\right)^{\lambda}\right) e^{-a\tau} + \left(\frac{y}{x}\right)^{\lambda} e^{-a(1-\delta^{\lambda})\tau}, \quad [\text{A.5.8}]$$

observing that $\psi(0) = 1$.

Given the survival function $\psi(\tau)$, the hazard function $\phi(\tau)$ for moving is defined by $\phi(\tau) = -\psi'(\tau)/\psi(\tau)$. Using equation (A.5.8):

$$\phi(\tau) = -\frac{d}{d\tau} \log e^{-a\tau} \left(1 + \left(\frac{y}{x}\right)^{\lambda} (e^{a\delta^{\lambda}\tau} - 1)\right) = a - \frac{a\delta^{\lambda} \left(\frac{y}{x}\right)^{\lambda} e^{a\delta^{\lambda}\tau}}{1 + \left(\frac{y}{x}\right)^{\lambda} (e^{a\delta^{\lambda}\tau} - 1)}.$$

Therefore, the hazard function is given by:

$$\phi(\tau) = a \left(1 - \frac{\delta^{\lambda} \left(\frac{y}{x}\right)^{\lambda}}{\left(\frac{y}{x}\right)^{\lambda} + \left(1 - \left(\frac{y}{x}\right)^{\lambda}\right) e^{-a\delta^{\lambda}\tau}}\right), \quad [\text{A.5.9}]$$

which is increasing in τ .

For new matches, the distribution $\mu(\tau)$ of the time τ until the next move is obtained from the survival function $\psi(\tau)$ using $\mu(\tau) = -\psi'(\tau)$. Hence, by using (A.5.8):

$$\mu(\tau) = a \left(1 - \left(\frac{y}{x}\right)^{\lambda}\right) e^{-a\tau} + a(1 - \delta^{\lambda}) \left(\frac{y}{x}\right)^{\lambda} e^{-a(1-\delta^{\lambda})\tau}. \quad [\text{A.5.10}]$$

The expected time T_n until the next move for a new match (expected tenure) can be derived from this distribution:

$$\begin{aligned} T_n &= \int_{\tau=0}^{\infty} \tau \mu(\tau) d\tau = \left(1 - \left(\frac{y}{x}\right)^{\lambda}\right) \int_{\tau=0}^{\infty} a\tau e^{-a\tau} d\tau + \left(\frac{y}{x}\right)^{\lambda} \int_{\tau=0}^{\infty} a(1 - \delta^{\lambda})\tau e^{-a(1-\delta^{\lambda})\tau} d\tau \\ &= \left(1 - \left(\frac{y}{x}\right)^{\lambda}\right) \frac{1}{a} + \left(\frac{y}{x}\right)^{\lambda} \frac{1}{a(1 - \delta^{\lambda})} = \frac{1}{a} \left(1 - \left(\frac{y}{x}\right)^{\lambda} + \frac{1}{1 - \delta^{\lambda}} \left(\frac{y}{x}\right)^{\lambda}\right). \end{aligned}$$

Thus, an expression for expected tenure is:

$$T_n = \frac{1}{a} \left(1 + \frac{\delta^{\lambda}}{1 - \delta^{\lambda}} \left(\frac{y}{x}\right)^{\lambda}\right). \quad [\text{A.5.11}]$$

The stationary age distribution $\theta(\tau)$ in the cross-section of surviving matches is proportional to the survival function $\psi(\tau)$:

$$\theta(\tau) = \frac{\psi(\tau)}{\int_{\tau=0}^{\infty} \psi(\tau) d\tau}. \quad [\text{A.5.12}]$$

The expression for $\psi(\tau)$ in (A.5.8) can be used to deduce that:

$$\int_{\tau=0}^{\infty} \psi(\tau) d\tau = \left(1 - \left(\frac{y}{x}\right)^{\lambda}\right) \frac{1}{a} + \left(\frac{y}{x}\right)^{\lambda} \frac{1}{a(1 - \delta^{\lambda})} = \frac{1}{a} \left(1 + \frac{\delta^{\lambda}}{1 - \delta^{\lambda}} \left(\frac{y}{x}\right)^{\lambda}\right). \quad [\text{A.5.13}]$$

Combining equations (A.5.12) and (A.5.13), the stationary age distribution is:

$$\theta(\tau) = \frac{a \left(1 - \left(\frac{y}{x}\right)^\lambda\right) e^{-a\tau} + a \left(\frac{y}{x}\right)^\lambda e^{-a(1-\delta^\lambda)\tau}}{1 + \frac{\delta^\lambda}{1-\delta^\lambda} \left(\frac{y}{x}\right)^\lambda}. \quad [\text{A.5.14}]$$

This distribution can be used to calculate the average years of ownership T_h of existing homeowners:

$$\begin{aligned} T_h &= \int_{\tau=0}^{\infty} \tau \theta(\tau) d\tau = \frac{\left(1 - \left(\frac{y}{x}\right)^\lambda\right) \int_{\tau=0}^{\infty} a\tau e^{-a\tau} d\tau + \frac{1}{1-\delta^\lambda} \left(\frac{y}{x}\right)^\lambda \int_{\tau=0}^{\infty} a(1-\delta^\lambda)\tau e^{-a(1-\delta^\lambda)\tau} d\tau}{1 + \frac{\delta^\lambda}{1-\delta^\lambda} \left(\frac{y}{x}\right)^\lambda} \\ &= \frac{\left(1 - \left(\frac{y}{x}\right)^\lambda\right) \frac{1}{a} + \frac{1}{1-\delta^\lambda} \left(\frac{y}{x}\right)^\lambda \frac{1}{a(1-\delta^\lambda)}}{1 + \frac{\delta^\lambda}{1-\delta^\lambda} \left(\frac{y}{x}\right)^\lambda} = \frac{\frac{1}{a} \left(1 - \left(\frac{y}{x}\right)^\lambda + \frac{1}{(1-\delta^\lambda)^2} \left(\frac{y}{x}\right)^\lambda\right)}{1 + \frac{\delta^\lambda}{1-\delta^\lambda} \left(\frac{y}{x}\right)^\lambda} = \frac{\frac{1}{a} \left(1 + \left(\frac{(1-\delta^\lambda)^2 - 1}{(1-\delta^\lambda)^2}\right) \left(\frac{y}{x}\right)^\lambda\right)}{1 + \frac{\delta^\lambda}{1-\delta^\lambda} \left(\frac{y}{x}\right)^\lambda}. \end{aligned}$$

Simplifying leads to the following formula for T_h :

$$T_h = \frac{\frac{1}{a} \left(1 + \frac{\delta^\lambda}{1-\delta^\lambda} \left(1 + \frac{1}{1-\delta^\lambda}\right) \left(\frac{y}{x}\right)^\lambda\right)}{1 + \frac{\delta^\lambda}{1-\delta^\lambda} \left(\frac{y}{x}\right)^\lambda}. \quad [\text{A.5.15}]$$

The average moving rate n can be calculated from the hazard function $\phi(\tau)$ and the age distribution $\theta(\tau)$:

$$n = \int_{\tau=0}^{\infty} \phi(\tau) \theta(\tau) d\tau = \int_{\tau=0}^{\infty} \left(-\frac{\psi'(\tau)}{\psi(\tau)}\right) (\theta(0)\psi(\tau)) d\tau = \theta(0) \int_{\tau=0}^{\infty} (-\psi'(\tau)) d\tau = \theta(0),$$

where the second equality uses the definition $\phi(\tau) = -\psi'(\tau)/\psi(\tau)$, and $\theta(\tau) = \theta(0)\psi(\tau)$, which follows from (A.5.12) noting $\psi(0) = 1$. Evaluating (A.5.14) at $\tau = 0$ implies the following expression for n :

$$n = \frac{a}{1 + \frac{\delta^\lambda}{1-\delta^\lambda} \left(\frac{y}{x}\right)^\lambda}, \quad [\text{A.5.16}]$$

which is the reciprocal of expected tenure ($T_n = 1/n$), and thus consistent with equation (A.5.11).

Given the moving rate n and the sales rate s , the steady-state stock of houses for sale is:

$$u = \frac{n}{s+n}. \quad [\text{A.5.17}]$$

The expression for n given in (A.5.16) is consistent with the formula (3.12) in the steady state:

$$n = a - a\delta^\lambda x^{-\lambda} v \frac{u}{1-u} \int_{\tau=0}^{\infty} e^{-a(1-\delta^\lambda)\tau} d\tau = a - a\delta^\lambda \left(\frac{y}{x}\right)^\lambda v y^{-\lambda} \frac{n}{s} \frac{1}{a(1-\delta^\lambda)},$$

where the final equality uses $u/(1-u) = n/s$, as implied by (A.5.17). Since $s = v y^{-\lambda}$ according to (A.3.22), the equation above becomes:

$$n = a - \frac{\delta^\lambda}{1-\delta^\lambda} \left(\frac{y}{x}\right)^\lambda n,$$

which yields the same solution for n as (A.5.16).

A.6 Efficiency

The social planner's objective function from (4.9) can be written in terms of total match quality \mathcal{E}_t , the transaction threshold y_t , and houses for sale u_t by substituting $\mathcal{E}_t = (1 - u_t)Q_t$ and using equation (3.11):

$$\Omega_T = \int_{t=T}^{\infty} e^{-r(t-T)} \left(\xi \mathcal{E}_t - C v y_t^{-\lambda} u_t - F u_t - M \right) dt. \quad [\text{A.6.1}]$$

This is maximized by choosing x_t , y_t , \mathcal{E}_t , u_t , and Z_t subject to the differential equations for \mathcal{E}_t , u_t , and Z_t in (A.5.5), (A.5.6), and (A.5.7) (the variable Z_t defined in A.5.4 is introduced because the differential equations A.5.5 and A.5.6 are written in terms of Z_t). The problem is solved by introducing the (current-value) Hamiltonian:

$$\begin{aligned} \mathcal{J}_t = & \xi \mathcal{E}_t - C v y_t^{-\lambda} u_t - F u_t - M + \varphi_t \left(\frac{v\lambda}{\lambda-1} y_t^{1-\lambda} u_t - a \mathcal{E}_t + \frac{av\delta^\lambda \lambda}{\lambda-1} x_t^{1-\lambda} Z_t \right) \\ & + \vartheta_t \left(a(1 - u_t) - av\delta^\lambda x_t^{-\lambda} Z_t - v y_t^{-\lambda} u_t \right) + \gamma_t \left(u_t - a(1 - \delta^\lambda) Z_t \right), \end{aligned} \quad [\text{A.6.2}]$$

where φ_t , ϑ_t , and γ_t are the co-state variables associated with \mathcal{E}_t , u_t , and Z_t . The first-order conditions with respect to x_t and y_t are:

$$\frac{\partial \mathcal{J}_t}{\partial x_t} = av\delta^\lambda \lambda x_t^{-\lambda-1} Z_t \vartheta_t - av\delta^\lambda \lambda x_t^{-\lambda} Z_t \varphi_t = 0; \quad [\text{A.6.3a}]$$

$$\frac{\partial \mathcal{J}_t}{\partial y_t} = v\lambda C y_t^{-\lambda-1} u_t - v\lambda y_t^{-\lambda} u_t \varphi_t + v\lambda y_t^{-\lambda-1} u_t \vartheta_t = 0, \quad [\text{A.6.3b}]$$

and the first-order conditions with respect to the state variables \mathcal{E}_t , u_t , and Z_t are:

$$\frac{\partial \mathcal{J}_t}{\partial \mathcal{E}_t} = \xi - a\varphi_t = r\varphi_t - \dot{\varphi}_t; \quad [\text{A.6.3c}]$$

$$\frac{\partial \mathcal{J}_t}{\partial u_t} = -C v y_t^{-\lambda} - F + \frac{v\lambda}{\lambda-1} y_t^{1-\lambda} \varphi_t - (a + v y_t^{-\lambda}) \vartheta_t + \gamma_t = r\vartheta_t - \dot{\vartheta}_t; \quad [\text{A.6.3d}]$$

$$\frac{\partial \mathcal{J}_t}{\partial Z_t} = \frac{av\delta^\lambda \lambda}{\lambda-1} x_t^{1-\lambda} \varphi_t - av\delta^\lambda x_t^{-\lambda} \vartheta_t - a(1 - \delta^\lambda) \gamma_t = r\gamma_t - \dot{\gamma}_t. \quad [\text{A.6.3e}]$$

By cancelling common terms from (A.6.3a), the following link between the moving threshold x_t and the co-states φ_t and ϑ_t can be deduced:

$$\varphi_t = \frac{\vartheta_t}{x_t}. \quad [\text{A.6.4}]$$

Similarly, cancelling common terms from (A.6.3b) implies a link between the transaction threshold y_t and φ_t and ϑ_t :

$$\frac{C}{y_t} + \frac{\vartheta_t}{y_t} = \varphi_t. \quad [\text{A.6.5}]$$

The differential equation for φ_t in (A.6.3c) is:

$$\dot{\varphi}_t = (r + a)\varphi_t - \xi,$$

and since $r + a > 0$, the only solution satisfying the transversality condition is the following constant solution:

$$\varphi_t = \frac{\xi}{r + a}. \quad [\text{A.6.6}]$$

With this solution for φ_t , equation (A.6.5) implies that ϑ_t is proportional to the moving threshold x_t :

$$\vartheta_t = \frac{\xi}{r+a} x_t. \quad [\text{A.6.7}]$$

Eliminating both φ_t and ϑ_t from (A.6.5) by substituting from (A.6.6) and (A.6.7) implies that y_t and x_t must satisfy:

$$y_t - x_t = \frac{(r+a)C}{\xi}. \quad [\text{A.6.8}]$$

Using (A.6.3d) to write a differential equation for ϑ_t and substituting the solution for φ_t from (A.6.6):

$$\dot{\vartheta}_t = (r+a+vy_t^{-\lambda})\vartheta_t - \gamma_t + F + Cvy_t^{-\lambda} - \frac{\xi}{r+a} \frac{v\lambda}{\lambda-1} y_t^{1-\lambda}. \quad [\text{A.6.9}]$$

Similarly, (A.6.3e) implies a differential equation for γ_t , from which φ_t can be eliminated using (A.6.6):

$$\dot{\gamma}_t = (r+a(1-\delta^\lambda))\gamma_t + av\delta^\lambda x_t^{-\lambda} \left(\frac{\xi}{r+a} x_t \right) - \frac{av\delta^\lambda \lambda}{\lambda-1} x_t^{1-\lambda} \left(\frac{\xi}{r+a} \right),$$

which can be simplified as follows:

$$\dot{\gamma}_t = (r+a(1-\delta^\lambda))\gamma_t - \frac{\xi}{r+a} \frac{av\delta^\lambda}{\lambda-1} x_t^{1-\lambda}. \quad [\text{A.6.10}]$$

It is now shown that there is a solution of the constrained maximization problem where the co-states ϑ_t and γ_t are constant over time. In this case, equations (A.6.7) and (A.6.8) require that x_t and y_t are constant over time and related as follows:

$$y - x = \frac{(r+a)C}{\xi}. \quad [\text{A.6.11}]$$

With $\dot{\vartheta}_t = 0$ and $\dot{\gamma}_t = 0$, (A.6.9) and (A.6.10) imply the following pair of equations:

$$(r+a+vy^{-\lambda})\vartheta - \gamma + F + Cvy^{-\lambda} - \frac{\xi}{r+a} \frac{v\lambda}{\lambda-1} y^{1-\lambda} = 0; \quad [\text{A.6.12}]$$

$$(r+a(1-\delta^\lambda))\gamma - \frac{\xi}{r+a} \frac{av\delta^\lambda}{\lambda-1} x^{1-\lambda} = 0. \quad [\text{A.6.13}]$$

Equation (A.6.13) yields the following expression for γ in terms of x :

$$\gamma = \frac{\xi av\delta^\lambda}{(\lambda-1)(r+a)(r+a(1-\delta^\lambda))} x^{1-\lambda},$$

and substituting this and (A.6.7) into (A.6.12) leads to:

$$\frac{\xi(r+a+vy^{-\lambda})}{r+a} x - \frac{\xi av\delta^\lambda}{(\lambda-1)(r+a)(r+a(1-\delta^\lambda))} x^{1-\lambda} + F + Cvy^{-\lambda} - \frac{\xi v\lambda}{(\lambda-1)(r+a)} y^{1-\lambda} = 0.$$

Since $(r+a)C = \xi(y-x)$ according to (A.6.11), multiplying the equation above by $(r+a)$ and substituting for $(r+a)C$ implies:

$$\xi(r+a+vy^{-\lambda})x - \frac{\xi av\delta^\lambda}{(\lambda-1)(r+a(1-\delta^\lambda))} x^{1-\lambda} + (r+a)F + \xi v(y-x)y^{-\lambda} - \frac{\xi v\lambda}{(\lambda-1)} y^{1-\lambda} = 0.$$

Dividing both sides by ξ and grouping terms in $(r + a)$ on the left-hand side:

$$(r + a) \left(x + \frac{F}{\xi} \right) = \frac{v\lambda}{\lambda - 1} y^{1-\lambda} - v y^{1-\lambda} + \frac{av\delta^\lambda}{(\lambda - 1)(r + a(1 - \delta^\lambda))} x^{1-\lambda},$$

and dividing both sides by $r + a$ and simplifying the terms involving $y^{1-\lambda}$ leads to:

$$x + \frac{F}{\xi} = \frac{v}{(\lambda - 1)(r + a)} \left(y^{1-\lambda} + \frac{a\delta^\lambda}{r + a(1 - \delta^\lambda)} x^{1-\lambda} \right). \quad [\text{A.6.14}]$$

The pair of equations (A.6.11) and (A.6.14) for x and y are identical to the equations (4.4) and (4.7) characterizing the equilibrium values of x and y . The equilibrium is therefore the same as the solution to the social planner's problem, establishing that it is efficient.

A.7 Implications of transaction taxes

The welfare consequences of taxes on housing-market transactions can be analysed using the sum of all families' utilities Ω_t from (4.9). The steady-state value of Ω_t is:

$$\Omega = \frac{1}{r} (\xi(1 - u)Q - Csu - Fu - M),$$

where the values of Q , s , and u are obtained from (4.10), (4.13), and (4.14).

A simple way of modelling transaction taxes is to add a tax component C_T to the total transaction cost $C = C_O + C_T$, where C_O is the original non-tax transaction cost. The amount of revenue raised in steady state is C_Tsu , and social welfare is given by $\Omega + C_Tsu$.

As an example, consider imposing a transactions tax equal to 3% of the average house price. Using the calibration from section 5.1, this implies that transactions S fall by 15%, eroding the amount of revenue collected by the same amount. More importantly, the deadweight loss is 57% of the revenue actually collected, so the tax has a significantly distortionary effect. If moving were exogenous (and adjusting the calibration accordingly), transactions would fall by less than 0.1% and the deadweight loss would only be 6% of the tax collected.

A.8 Transitional dynamics and overshooting

Transitional dynamics

If the moving and selling rates n_t and s_t were equal to constants n and s , the stock of houses for sale evolves according to the differential equation:

$$\dot{u}_t = n(1 - u_t) - su_t = -(s + n)(u_t - u), \quad \text{where } u = \frac{n}{s + n}.$$

Using $s = 1/T_s$ and $n = 1/T_n$, the rate of convergence to the steady state is determined by:

$$\dot{u}_t = - \left(\frac{1}{T_s} + \frac{1}{T_n} \right) (u_t - u).$$

Now suppose the moving and transaction thresholds are constant over time at x and y . This means the sales rate is constant at $s = vy^{-\lambda}$. Let u_t^* , n_t^* , S_t^* , and N_t^* denote houses for sale, the moving rate, and the volumes of transactions and listings, ignoring transitional dynamics in houses for sale. This means that the number of houses for sale satisfies:

$$u_t^* = \frac{n_t^*}{s + n_t^*}. \quad [\text{A.8.1}]$$

Given u_t^* , the listing rate n_t^* can be obtained using the formula in (3.12):

$$n_t^* = a - \frac{a\delta^\lambda vx^{-\lambda}}{1 - u_t^*} \int_{\tau \rightarrow -\infty}^t e^{-a(1-\delta^\lambda)(t-\tau)} u_\tau^* d\tau. \quad [\text{A.8.2}]$$

The volumes of transactions and listings are:

$$S_t^* = su_t^*, \quad \text{and} \quad N_t^* = n_t^*(1 - u_t^*), \quad \text{with} \quad S_t^* = N_t^*, \quad [\text{A.8.3}]$$

where the latter claim follows from the definition of u_t^* in (A.8.1). Multiplying both sides of (A.8.2) by $1 - u_t^*$ leads to an equation for N_t^* :

$$N_t^* = a(1 - u_t^*) - a\delta^\lambda vx^{-\lambda} \int_{\tau \rightarrow -\infty}^t e^{-a(1-\delta^\lambda)(t-\tau)} u_\tau^* d\tau, \quad [\text{A.8.4}]$$

and differentiating with respect to time:

$$\dot{N}_t^* = -a\dot{u}_t^* - a\delta^\lambda vx^{-\lambda} u_t^* + a(1 - \delta^\lambda) \left(a\delta^\lambda vx^{-\lambda} \int_{\tau \rightarrow -\infty}^t e^{-a(1-\delta^\lambda)(t-\tau)} u_\tau^* d\tau \right).$$

Using (A.8.4) to substitute for the integral above:

$$\dot{N}_t^* = -a\dot{u}_t^* - a\delta^\lambda vx^{-\lambda} u_t^* + a(1 - \delta^\lambda)(a(1 - u_t^*) - N_t^*),$$

and since (A.8.3) implies $u_t^* = N_t^*/s$ for all t for which the sales rate s is constant (and thus $\dot{u}_t^* = \dot{N}_t^*/s$), the differential equation above can be written solely in terms of N_t^* :

$$\dot{N}_t^* = -\frac{a}{s}\dot{N}_t^* - \frac{a}{s}\delta^\lambda vx^{-\lambda} N_t^* + a(1 - \delta^\lambda) \left(a \left(1 - \frac{N_t^*}{s} \right) - N_t^* \right).$$

Collecting terms in \dot{N}_t^* on the left-hand side and grouping terms in N_t^* on the right-hand side:

$$\left(\frac{a+s}{s} \right) \dot{N}_t^* = a(1 - \delta^\lambda)a - a(1 - \delta^\lambda) \left(\frac{a+s}{s} + \frac{\delta^\lambda}{1-\delta^\lambda} \frac{vx^{-\lambda}}{s} \right) N_t^*,$$

and using $s = vy^{-\lambda}$ it follows that:

$$\dot{N}_t^* = a(1 - \delta^\lambda) \left(\frac{as}{a+s} - \left(1 + \frac{\delta^\lambda}{1-\delta^\lambda} \left(\frac{y}{x} \right)^\lambda \frac{s}{a+s} \right) N_t^* \right). \quad [\text{A.8.5}]$$

Now observe that:

$$\frac{\frac{as}{a+s}}{1 + \frac{\delta^\lambda}{1-\delta^\lambda} \left(\frac{y}{x} \right)^\lambda \frac{s}{a+s}} = \frac{a}{\frac{a+s}{s} + \frac{\delta^\lambda}{1-\delta^\lambda} \left(\frac{y}{x} \right)^\lambda} = \frac{a}{\frac{a}{s} + \left(1 + \frac{\delta^\lambda}{1-\delta^\lambda} \left(\frac{y}{x} \right)^\lambda \right)} = \frac{a}{\frac{a}{s} + \frac{a}{n}} = \frac{sn}{s+n} = N,$$

which uses the expression for n from (A.5.16), hence the differential equation (A.8.5) can be written as:

$$\dot{N}_t^* = -a(1 - \delta^\lambda) \left(1 + \frac{\delta^\lambda}{1-\delta^\lambda} \left(\frac{y}{x} \right)^\lambda \frac{s}{a+s} \right) (N_t^* - N). \quad [\text{A.8.6}]$$

The coefficient of $N_t^* - N$ gives the rate of convergence to the long-run steady state. Since $S_t^* = N_t^*$ and

$u_t^* = N_t^*/s$, it follows that the rate of convergence is the same for S_t^* and u_t^* :

$$\begin{aligned}\dot{S}_t^* &= -a(1 - \delta^\lambda) \left(1 + \frac{\delta^\lambda}{1 - \delta^\lambda} \left(\frac{y}{x} \right)^\lambda \frac{s}{a + s} \right) (S_t^* - S); \\ \dot{u}_t^* &= -a(1 - \delta^\lambda) \left(1 + \frac{\delta^\lambda}{1 - \delta^\lambda} \left(\frac{y}{x} \right)^\lambda \frac{s}{a + s} \right) (u_t^* - u).\end{aligned}$$

The result is similar for the moving rate n_t^* , though this is not a linear function of the other variables:

$$\dot{n}_t^* = -a(1 - \delta^\lambda) \left(1 + \frac{\delta^\lambda}{1 - \delta^\lambda} \left(\frac{y}{x} \right)^\lambda \frac{s}{a + s} \right) \left(\frac{s + n_t^*}{s + n} \right) (n_t^* - n).$$

Overshooting

Now consider the effect of a change in the moving threshold x at time t while the transaction threshold y is held constant, starting from a steady state. In what follows, the subscripts t_- and t_+ respectively denote the values of a variable immediately before and after the change in the moving threshold at time t . Beginning in a steady state implies

$$\int_{\tau \rightarrow -\infty}^t e^{-a(1-\delta^\lambda)(\tau-t)} u_\tau^* d\tau = \frac{u_{t_-}^*}{a(1-\delta^\lambda)},$$

and substituting this expression into equation (A.8.2) shows that $n_{t_+}^*$ must satisfy:

$$n_{t_+}^* = a - \frac{a\delta^\lambda vx^{-\lambda}}{a(1-\delta^\lambda)} \frac{u_{t_-}^*}{1-u_{t_+}^*} = a - \frac{\delta^\lambda}{1-\delta^\lambda} \frac{vx^{-\lambda}}{s} (s+n_{t_+}^*) u_{t_-}^*,$$

where the second equality uses $1 - u_t^* = s/(s + n_t^*)$ implied by (A.8.1). Noting that $s = vy^{-\lambda}$, the equation becomes:

$$n_{t_+}^* = a - \frac{\delta^\lambda}{1-\delta^\lambda} \left(\frac{y}{x} \right)^\lambda (s+n_{t_+}^*) u_{t_-}^*,$$

which can be solved for $n_{t_+}^*$:

$$n_{t_+}^* = \frac{a - \frac{\delta^\lambda}{1-\delta^\lambda} \left(\frac{y}{x} \right)^\lambda s u_{t_-}^*}{1 + \frac{\delta^\lambda}{1-\delta^\lambda} \left(\frac{y}{x} \right)^\lambda u_{t_-}^*}.$$

This confirms the equation given in the text. Equation (4.11) implies that the new steady-state moving rate n satisfies:

$$\frac{\delta^\lambda}{1-\delta^\lambda} \left(\frac{y}{x} \right)^\lambda = \frac{a}{n} - 1,$$

which can be substituted into the formula for $n_{t_+}^*$ above to obtain:

$$n_{t_+}^* = \frac{a - \left(\frac{a}{n} - 1 \right) s u_{t_-}^*}{1 + \left(\frac{a}{n} - 1 \right) u_{t_-}^*}.$$

Note that $n_{t_+}^* > n$ is equivalent to:

$$a - \left(\frac{a}{n} - 1 \right) s u_{t_-}^* > \left(1 + \left(\frac{a}{n} - 1 \right) u_{t_-}^* \right) n,$$

and dividing both sides by n and factorizing leads to:

$$\left(\frac{a}{n} - 1\right) \left(1 - \frac{u_{t-}^*}{u}\right) > 0.$$

Since $a > n$, this can hold only if $u > u_{t-}^*$. With $u = n/(s+n)$ and $u_{t-}^* = n_{t-}^*/(s+n_{t-}^*)$, this occurs when $n > n_{t-}^*$, which confirms the claim that there is overshooting.

A.9 Productivity and interest rates

Suppose that a family's flow utility is $C_t^{1-\alpha} \mathcal{H}_t^\alpha$, where C_t denotes consumption and \mathcal{H}_t denotes housing, and where α indicates the importance of housing in the utility function ($0 < \alpha < 1$). This adds non-housing goods to the model and replaces the flow utility $\xi\epsilon$ assumed earlier. The form of the flow utility function assumes complementarity between consumption and housing services. The housing variable \mathcal{H}_t that enters the utility function is equal to the match quality ϵ of a family with its house, and the evolution of this variable in response to idiosyncratic shocks and moving and transaction decisions is the same as before. The discount rate for future utility flows is the rate of pure time preference ρ . The lifetime utility function from time T onwards is therefore:

$$\mathcal{U}_T = \int_{t=T}^{\infty} e^{-\rho(t-T)} C_t^{1-\alpha} \mathcal{H}_t^\alpha dt. \quad [\text{A.9.1}]$$

Suppose there are complete financial markets for securities with consumption payoffs contingent on any state of the world, and suppose all families receive the same real income (with no aggregate risk) and initially all have equal financial wealth. Note that only state-contingent consumption, not housing services, can be traded in these markets. With complete financial markets there is full consumption insurance of idiosyncratic risk coming from shocks to match quality and the uncertainties in the search process, implying that the marginal utility of consumption must be equalized across all families. The marginal utility of consumption is $z_t^{-\alpha}$, where $z_t = C_t/\mathcal{H}_t$ is the ratio of consumption to housing match quality. If r is the real interest rate (in terms of consumption goods) then maximization of utility (A.9.1) subject to the lifetime budget constraint requires that the following consumption Euler equation holds:

$$\alpha \frac{\dot{z}_t}{z_t} = r - \rho. \quad [\text{A.9.2}]$$

In equilibrium, the sum of consumption C_t across all families must be equal to aggregate real income Y_t , which is assumed to be an exogenous endowment growing at rate g over time. Given equalization of $z_t = C_t/\mathcal{H}_t$ across all families at a point in time and given a stationary distribution of match quality $\mathcal{H}_t = \epsilon$ across all families, it follows that all families have a value of z_t proportional to aggregate real income Y_t at all times:

$$z_t = \varkappa Y_t, \quad \text{where } \varkappa = \frac{1}{(1-u)Q}. \quad [\text{A.9.3}]$$

The constant \varkappa is the reciprocal of total match quality $(1-u)Q$ in steady state (noting that unsatisfied owners receive no housing utility flows). Substituting this into the consumption Euler equation (A.9.2) implies that the equilibrium real interest rate is:

$$r = \rho + \alpha g. \quad [\text{A.9.4}]$$

Since (A.9.3) implies $C_t = \varkappa Y_t \mathcal{H}_t$, it follows that lifetime utility (A.9.1) can be expressed as follows:

$$\mathcal{U}_T = \varkappa^{1-\alpha} \int_{t=T}^{\infty} e^{-\rho(t-T)} Y_t^{1-\alpha} \mathcal{H}_t dt.$$

With Y_t growing at rate g , income at time t can be written as $Y_t = e^{g(t-T)}Y_T$. By substituting this into the lifetime utility function and using the expression for the real interest rate r in (A.9.4):

$$\mathcal{U}_T = \varkappa^{1-\alpha} Y_T^{1-\alpha} \int_{t=T}^{\infty} e^{-(r-g)(t-T)} \mathcal{H}_t dt. \quad [\text{A.9.5}]$$

Lifetime utility is therefore a discounted sum of match quality $\mathcal{H}_t = \epsilon$. The coefficient of match quality (this is the parameter ξ in the main text) is increasing in the current level of real income, and the discount rate (denoted r in the main text) is the difference between the market interest rate and the growth rate of real income. This provides a justification for interpreting a rise in real incomes as an increase in ξ and a fall in the market interest rate as a lower discount rate.

A.10 Calibration method

This section shows how the 10 parameters a , δ , λ , v , C , F , M , κ , ω , and r can be obtained from observables. Three of the parameters (κ , ω , and r) are set directly. The other seven are obtained indirectly from seven calibration targets. These are time-to-sell T_s , viewings per sale V_s , expected tenure T_n , average years of ownership T_h , the transaction cost to price ratio c , the flow search cost to price ratio f , and the flow maintenance cost to price ratio m . Note that the model contains one other parameter ξ , but in all equations determining observables, ξ enters only as a ratio to other parameters (this can be seen from equations 5.1a–5.1c). This parameter is therefore normalized to $\xi = 1$.

The calibration method begins by setting κ , ω , and r directly. Next, consider a guess for T_δ , the expected time until an idiosyncratic shock occurs. This conjecture determines the parameter a using:

$$a = \frac{1}{T_\delta}. \quad [\text{A.10.1}]$$

The admissible range for T_δ is $0 < T_\delta < T_n$.

Define the following variable ζ :

$$\zeta \equiv \frac{\delta^\lambda}{1 - \delta^\lambda} \left(\frac{y}{x} \right)^\lambda. \quad [\text{A.10.2}]$$

Using equations (A.10.1) and (A.10.2), the expressions for T_n and T_h in (A.5.11) and (A.5.15) can be written as:

$$T_n = (1 + \zeta)T_\delta, \quad \text{and} \quad T_h = \frac{\left(1 + \left(1 + \frac{1}{1 - \delta^\lambda}\right)\zeta\right) T_\delta}{1 + \zeta}. \quad [\text{A.10.3}]$$

This equation confirms it is necessary that $0 < T_\delta < T_n$ otherwise ζ would not be positive, as required in (A.10.2). Solving for ζ using the expression for T_n in (A.10.3):

$$\zeta = \frac{T_n - T_\delta}{T_\delta}. \quad [\text{A.10.4}]$$

Equations (A.10.3) and (A.10.4) can be used to deduce:

$$\frac{T_n}{T_\delta} + \left(\frac{T_n - T_\delta}{T_\delta} \right) \frac{1}{1 - \delta^\lambda} = 1 + \left(1 + \frac{1}{1 - \delta^\lambda} \right) \left(\frac{T_n - T_\delta}{T_\delta} \right) = (1 + \zeta) \frac{T_h}{T_\delta} = \frac{T_n T_h}{T_\delta^2},$$

and multiplying both sides by T_δ/T_n and rearranging yields:

$$\left(\frac{T_n - T_\delta}{T_n} \right) \frac{1}{1 - \delta^\lambda} = \frac{T_h - T_\delta}{T_\delta}.$$

This leads to an expression for $\delta^\lambda/(1 - \delta^\lambda)$:

$$\frac{\delta^\lambda}{1 - \delta^\lambda} = \frac{1}{1 - \delta^\lambda} - 1 = \frac{(T_h - T_\delta)T_n}{(T_n - T_\delta)T_\delta} - 1, \quad [\text{A.10.5}]$$

and using this in conjunction with (A.10.2) and (A.10.4):

$$\left(\frac{y}{x}\right)^\lambda = \frac{\frac{T_n - T_\delta}{T_\delta}}{\frac{(T_h - T_\delta)T_n}{(T_n - T_\delta)T_\delta} - 1}. \quad [\text{A.10.6}]$$

Now take equation (A.4.3) for the average price and divide both sides by P (recalling the normalization $\xi = 1$):

$$\kappa c - \frac{m}{r} + \omega \left(\frac{1}{r} + \frac{y^\lambda}{v} \right) \left(\frac{x}{P} + f \right) = 1.$$

Noting the expression for T_s in (A.3.22), the equation above can be solved for x/P as follows:

$$\frac{x}{P} = \frac{1 - \kappa c + \frac{m}{r}}{\omega \left(\frac{1}{r} + T_s \right)} - f. \quad [\text{A.10.7}]$$

Now take the linear equation (A.3.7) involving the thresholds x and y and divide both sides by P (again, recalling $\xi = 1$):

$$\frac{y}{P} = \frac{x}{P} + (r + a)c,$$

and then dividing both sides by x/P and using (A.10.7):

$$\frac{y}{x} = \frac{y/P}{x/P} = 1 + \frac{(r + a)c}{\frac{1 - \kappa c + \frac{m}{r}}{\omega \left(\frac{1}{r} + T_s \right)} - f}. \quad [\text{A.10.8}]$$

With formulas for both $(y/x)^\lambda$ from (A.10.6) and y/x from (A.10.8), the value of λ can be deduced from the identity $\log(y/x)^\lambda = \lambda \log(y/x)$:

$$\lambda = \frac{\log \left(\frac{\frac{T_n - T_\delta}{T_\delta}}{\frac{(T_h - T_\delta)T_n}{(T_n - T_\delta)T_\delta} - 1} \right)}{\log \left(1 + \frac{(r + a)c}{\frac{1 - \kappa c + \frac{m}{r}}{\omega \left(\frac{1}{r} + T_s \right)} - f} \right)}. \quad [\text{A.10.9}]$$

Given λ , the transactions and moving thresholds y and x can be obtained from viewings per sale V_s using (A.3.21) and (A.10.8):

$$y = V_s^{\frac{1}{\lambda}}, \quad \text{and} \quad x = \frac{V_s^{\frac{1}{\lambda}}}{1 + \frac{(r + a)c}{\frac{1 - \kappa c + \frac{m}{r}}{\omega \left(\frac{1}{r} + T_s \right)} - f}}. \quad [\text{A.10.10}]$$

Using (A.3.21) and (A.3.22), the ratio of viewings per sale V_s and time to sell T_s determines the meeting rate v :

$$v = \frac{V_s}{T_s}. \quad [\text{A.10.11}]$$

Combining equations (A.10.7) and (A.10.10) leads to the following expression for P :

$$P = \frac{V_s^{\frac{1}{\lambda}}}{\frac{1-\kappa c + \frac{m}{r}}{\omega(\frac{1}{r} + T_s)} + (r+a)c - f},$$

and this can be used to obtain the parameters C , F , and M using $C = cP$, $F = fP$, and $M = mP$. The parameter δ is derived from (A.10.5) and the value of λ in (A.10.9):

$$\delta = \left(1 - \frac{(T_n - T_\delta)T_\delta}{(T_h - T_\delta)T_n}\right)^{\frac{1}{\lambda}}.$$

Finally, equation (A.3.16) must also hold, which requires:

$$x + \frac{F}{\xi} = \frac{v}{(\lambda - 1)(r + a)} \left(y^{1-\lambda} + \frac{a\delta^\lambda}{r + a(1 - \delta^\lambda)} x^{1-\lambda} \right),$$

and this is used to verify the initial conjecture for T_δ .

A.11 The effects of easier credit

Table 5 reports the results in the case of a 50% reduction in buyers' transaction costs C_b . The effects are shown in isolation and in combination with the other factors.

Table 5: *Improvement in credit conditions*

Factor	Transactions	Listings	Houses for sale	Sales rate	Moving rate	Prices
$C_b \downarrow 50\%$	16%	16%	2%	14%	16%	3%
$C_b \downarrow 50\%$, $\xi \uparrow 25\%$, $\nu \uparrow 33\%$	22%	22%	5%	16%	22%	49%
$C_b \downarrow 50\%$, $\xi \uparrow 25\%$, $\nu \uparrow 33\%$, $r \downarrow 39\%$	23%	23%	21%	2%	25%	145%
Data (1995-2004)	34%	37%	12%	22%	37%	45%

A.12 The bust period

The advantages of the endogenous moving model are also apparent during the housing market bust. There was a collapse in transactions and listings (both volumes and rates) starting in 2006, which was largely complete by 2009. The size of the declines in these variables was of a similar magnitude to the preceding decade-long boom.

Suppose that the driving force for the bust is modelled as a decrease in housing demand (a fall in ξ). The size of this shock is chosen so that the endogenous moving model matches the decline in transactions seen in the data. The effects of the demand shock in the endogenous and exogenous moving models are reported in the first two rows of Table 6. The endogenous moving model does a good job in matching the decline in the moving rate and the volume of listings while, as expected, the exogenous moving model cannot account for any of the drop in transactions given that it predicts no change in the moving rate. The third row of the table reports the results when the exogenous moving model is subject to an exogenous

moving rate shock that generates a decline in transactions matching the data. While this version of the model does well in predicting declines in the sales rate and moving rate, it actually predicts that prices would rise.

Table 6: *Housing bust, 2006–2009*

Model	Transactions	Listings	Houses for sale	Sales rate	Moving rate	Prices
Endogenous moving ($\xi \downarrow 48\%$)	–50%	–50%	–21%	–37%	–50%	–76%
Exogenous moving (I) ($\xi \downarrow 48\%$)	0%	0%	–5%	5%	0%	–79%
Exogenous moving (II) (<i>a</i> shock, match transactions)	–50%	–50%	–30%	–29%	–51%	11%
Data (2006-2009)	–50%	–68%	13%	–62%	–66%	–15%