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Stephen P. Jenkins

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Pareto models, top incomes, and recent trends in UK income inequality

Stephen P. Jenkins (LSE, ISER (University of Essex), and IZA)

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Abstract

I determine UK income inequality levels and trends by combining inequality estimates from tax return data (for the 'rich') and household survey data (for the 'non-rich'), taking advantage of the better coverage of top incomes in tax return data (which I demonstrate) and creating income variables in the survey data with the same definitions as in the tax data to enhance comparability. For top income recipients, I estimate inequality and mean income by fitting Pareto models to the tax data, examining specification issues in depth, notably whether to use Pareto I or Pareto II (generalised Pareto) models, and the choice of income threshold above which the Pareto models apply. The preferred specification is a Pareto II model with a threshold set at the 99th or 95th percentile (depending on year). Conclusions about aggregate UK inequality trends since the mid-1990s are robust to the way in which tax data are employed. The Gini coefficient for gross individual income rose by around 7% or 8% between 1996/97 and 2007/08, with most of the increase occurring after 2003/04. The corresponding estimate based wholly on the survey data is around –5%.

Keywords: inequality, top incomes, Pareto distribution, generalized Pareto distribution, survey under-coverage, HBAI, SPI

JEL Classifications: C46, C81, D31

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Correspondence: Stephen P. Jenkins, Department of Social Policy, London School of Economics, Houghton Street, London WC2A 2AE, UK. Email: s.jenkins@lse.ac.uk.

1. Introduction

There is a bifurcation in the literature on income inequality levels and trends. On the one hand, most official statistics and academic analysis utilise data from household surveys and report estimates of the inequality of family or household disposable income summarised using Gini coefficients and other inequality indices calculated using all incomes from poorest to richest. (See e.g. OECD 2008, 2011, 2015, on cross-national comparisons, and Belfield et al. 2015 and Department of Work and Pensions 2015 on UK trends.) On the other hand, there is the 'top incomes' literature that uses administrative record data on personal income tax returns, reporting estimates of top income shares – the share of total income received by the richest 1% or richest 10%, and so on. (See e.g. Alvaredo et al. 2013, Atkinson and Piketty 2007 on cross-national comparisons, and Atkinson 2005 on UK trends.)

The two literatures differ in their findings about recent inequality trends: estimates from tax return data show a substantial rise in inequality over the last two decades in both the UK and USA, for instance, whereas survey-based estimates of inequality show much less change. For the UK, for example, the share of total income held by the richest 1% increased by 29% between fiscal years 1996/97 and 2007/08 whereas the Gini coefficient increased by 7% (Alvaredo et al. 2015, Belfield et al. 2015). For the USA, the corresponding increases over the same period are 30% and 2% (Alvaredo et al. 2015, De-Nevas Walt and Proctor 2015).

The divergent findings about inequality trends from the two data sources arise partly because different inequality indices and income definitions are employed (more on this later). However, another important explanation is that household surveys do not capture top incomes very well, whereas tax data do a much better job of this.

In this paper, I determine UK income inequality levels and trends since the mid-1990s by combining estimates from tax return data (for the 'rich') and household survey data (for the 'non-rich'), taking advantage of the better coverage of top incomes in tax return data (which I demonstrate) and creating income variables in the survey data with the same definitions as in the tax data to enhance comparability. I also analyse how estimates of inequality trends differ by inequality index.

There are multiple sources of under-coverage of top incomes in survey data. The first is under-reporting among high-income respondents or top-coding of their responses by survey administrators. In these cases, survey data are right-censored. A second source of under-coverage is the sampling of high-income respondents per se. Respondents may provide

sparse coverage of the top income ranges and, in addition, there may be no respondents at all from the extreme right-hand tail, because the survey organisation does not target potential high income respondents by design, or it is unable to contact them, or there is contact but refusal to participate. In this case, the observed income data are a right-truncated sample of the 'true' distribution. Both types of under-coverage contribute downward bias to survey estimates of inequality for a given year because there is not enough income observed in the very top income ranges. A by-product of sparse coverage of the top income ranges is that the high-income observations present in the survey data have the characteristics of outliers (even if they are genuine rather than an error), and have substantial influence on the conventional non-parametric estimate of an inequality measure for a given year: see Cowell and Victoria-Feser (1996, 2007) and Cowell and Flachaire (2007). This sensitivity can also introduce spurious volatility in a time series of inequality estimates.

There are three approaches to estimating inequality measures that address these under-coverage problems: see Figure 1 for a schematic summary. Approach A is based entirely on survey data. It derives an inequality estimate for the poorest p% using non-parametric methods applied to survey unit-record data, and derives an inequality estimate from the richest (1-p)% by fitting a Pareto Type I distribution to the top income observations from the same source. The estimate of total inequality, mostly summarised using the Gini coefficient, is calculated by adding together three components: inequality within the top group, inequality within the non-top group, and between-group inequality.

<Figure 1 near here>

Cowell and Flachaire (2007) provide a thorough examination of the properties of Approach A motivated by, and focusing on, the problem of sparse coverage of top income ranges. Their headline conclusion is that such 'use of appropriate semiparametric methods for modelling the upper tail can greatly improve the performance of those inequality indices that are normally considered particularly sensitive to extreme values' (2007: 1044). Alfons et al. (2013) also motivate their application of Approach A, using EU-SILC survey data for Austria and Belgium, with reference to sensitivity issues. Neither article refers to under-coverage per se. By contrast, Ruiz and Woloszko motivate their application to survey data for OECD countries in terms of 'correcting household survey data for underreporting in the upper-tail of income distributions' (2015: 6). Burkhauser et al. (2012) use Approach A to adjust for the systematic under-coverage of high incomes in public use Current Population Survey datasets introduced by US Census Bureau top-coding. In both applications, the idea is that the upper

tail to the income distribution implied by the parametric model estimates will capture more income than non-parametric estimates.

There is evidence that Approach A's ability to address survey under-coverage at the top is limited. For example, survey-based estimates of the share of total income held by the top 1% are several percentage points less than the estimates from tax return data according to the analysis of Atkinson et al. (2011) and Burkhauser (2012) for the USA. Put differently, fitting a parametric upper tail may obviate the sparsity problem (there is density mass at all points of the distribution's support, by assumption), but the estimate of the 'true' upper tail based on model-based extrapolation from the observed survey observations may not be reliable. This motivates the use of tax return data, as they have better coverage of the upper tail.

Approaches B and C both use tax return data but take different routes to addressing under-coverage issues. Approach B replaces the highest incomes in the survey with cell-mean imputations based on the corresponding observations in the tax return data. The 'SPI adjustment' to Family Resource Survey income data – used to derive the UK's official income distribution statistics since the early 1990s – is an example of this approach (see e.g. Department for Work and Pensions 2015). Burkhauser et al. (2016) apply Approach B in a more extensive and comprehensive manner and use World Top Incomes Database (Alvaredo et al. 2015) estimates of top income shares as a benchmark. Bach et al. (2009) is an application to Germany.

Approach C, used in this paper, *combines estimates* from the two types of data source rather than *combining data* per se as Approach B does. It is thus identical to Approach A except that it uses both survey and tax data rather than only the former; it is this feature that addresses the under-coverage problem. Approach C was developed by Atkinson (2007: 19–20) with an application to the USA by Atkinson et al. (2011), and extended by Alvaredo (2011) who also included applications to Argentina and the USA. Subsequent applications include those by Alvaredo and Londoño Vélez (2015) and Diaz-Bazan (2015) to Colombia, and by Lakner and Milanovic (2016) and Anand and Segal (2016) to global income inequality. Each of the applications cited uses a Pareto I model to describe the upper tail of the income distribution. In principle, researchers could employ non-parametric estimates of inequality indices for the top incomes in the tax data, but there is then the issue of whether these would be subject to the sensitivity problems mentioned earlier. The issue has not been studied before using tax data: I do so in this paper.

To perform well, Approaches B and C both rely on the researcher using the same 'income' definition in both data sources and ensuring that calculations refer to the same population. Otherwise, there is an 'apples + bananas' problem: non-comparability introduces bias. To avoid this, we may exploit a comparative advantage of survey data. The ability to change income definitions in tax return data is limited but, with access to unit record survey data, we can do a cross-walk from survey to tax data definitions. That is what I do in this paper, employing the same harmonized income variables for the survey and tax data as Burkhauser et al. (2016). For more details, see below.

This paper makes several contributions. First, there is the substantive application to UK inequality trends since the mid-1990s. How much income inequality has been growing is of much public interest. Second, related, there is question of whether Approaches C and B tell the same story about trends when applied to the same data sources. I contrast my Approach C estimates with the Approach B estimates provided by the official statistics (Department for Work and Pensions 2015; see also Belfield et al. 2015) and Burkhauser et al. (2016). Third, I provide new evidence about the extent to which there is under-coverage by survey data of the UK income distribution, using comparable tax data as the benchmark.

Fourth, I provide new analysis of issues that arise when fitting a Pareto model to the upper tail of the income distribution, and hence of direct relevance to researchers applying the semiparametric Approaches A and C. My findings are relevant to analysis of other heavy-tailed distributions such as wealth (Shorrocks et al. 2015, Vermeulen 2014), and city and firm size (Eeckhout 2004; Gabaix 2009, 2016). I use unit record tax return data rather than grouped (bracketed) data and so have flexibility to explore a number of econometric issues. (On estimation issues that arise with grouped tax return data – the only source available for deriving very long historical series – see Atkinson 2005, 2007 and references therein.) For instance, for the Pareto Type I model, I compare the performance of ordinary least squares, maximum likelihood, and maximum likelihood-robust estimators. I also address two implementation questions.

The first question is: what model should be fitted to top incomes? To date, researchers have invariably used the Pareto Type I model. This has a single shape parameter and there are simple formulae for calculating mean income and inequality indices from parameter estimates. There is also a widespread view that Pareto Type I models fit top income data well (Atkinson et al. 2014: 14). However, many of the goodness of fit checks that researchers have employed do not reliably distinguish Pareto distributions from other heavy-tailed distributions. In addition, most of the goodness of fit approaches used can only check whether

data are consistent with a distribution in the Pareto family, i.e. not with the Pareto Type I specifically (Cirillo 2013). I provide the first systematic comparison of the goodness of fit of Pareto Type I and Pareto Type II ('generalised Pareto') models to top income data, and show that the latter outperforms the former except at extremely high thresholds – thresholds that are well above those typically employed.

The second and related implementation question is: if we assume that incomes are described by a Pareto model above some threshold, what should that threshold be? In particular, when implementing Approaches C or A, what is the cut-off to use to distinguish between top incomes and non-top incomes? Is the top income group the top 10% (Ruiz and Woloszko 2015), or the top 5% (Atkinson 2016), or the top 1% (Alvaredo 2011)? There is some evidence that a higher cut-off decreases the estimate of the Pareto Type I shape parameter, i.e. increases inequality among top incomes, other things being equal (see e.g. Burkhauser 2012: Appendix A). However, the impact on total inequality estimated using Approach C of changing the threshold is unclear, because inequality and the mean among non-top incomes and between-group inequality also change.

Several criteria have been proposed for choosing Pareto thresholds (see e.g. Clauset et al. 2009, Coles 2001) and I employ them. However, I also argue that there is an additional issue to be taken into account when applying Approach C. That is, because non-coverage issues motivate the approach, it is important to ascertain precisely where along the top income range it is that survey non-coverage occurs. There is little evidence about this for the UK. I show that survey non-coverage is apparent from around the 99th percentile upwards in the mid- to late-1990s or from around the 95th percentile in the 2000s. I use the 99th and 95th percentiles as the Pareto threshold when deriving my inequality estimates, as well as the 90th percentile as a robustness check.

I introduce in Section 2 the UK tax return and survey data that I use, and explain the creation of income variables using harmonized definitions and hence on a comparable basis. Section 3 provides evidence about under-coverage of the survey data using the tax data as the benchmark. I analyse the fitting of Pareto models to top incomes in tax return data in Section 4, and present estimates of overall inequality levels and trends since the mid-1990s in Section 5. Section 6 provides a summary and conclusions. Applying Approach C, I show that choosing different Pareto models and different thresholds has noticeable impacts on estimates of inequality among the rich. However, my conclusions about overall inequality trends are broadly robust to the choice of Pareto model and percentile threshold, and there are similar results if upper tail inequality and mean income are estimated non-parametrically. The

estimated inequality trends from Approach C are also similar to those derived using Approach B (Burkhauser et al. 2016). For example, the Gini coefficient for gross individual income rose by around 7% or 8% between 1996/97 and 2007/08, with most of the increase occurring after 2003/04. The corresponding estimate based wholly on the survey data is around –5%.

2. Survey and tax data, and the definition of income

The income tax return data are from the public-release files of the *Survey of Personal Incomes* (SPI) for each year 1995/96 through 2010/11, with the exception of 2008/09 for which no data have been released. Atkinson (2005) uses these data, as well as published tabulations from the SPI and from supertax and surtax returns for earlier years, in his pioneering analysis of trends in UK top income shares since 1908. (See also Atkinson 2016 for Pareto I parameter estimates back to 1799.) The SPI data underlie the UK top income share estimates in the World Top Incomes Database (WTID) (Alvaredo et al. 2015). Each year's SPI is a stratified sample of the universe of tax returns. The number of individuals in the data has increased from around 57,000 individuals in 1995/96 to nearly 677,500 in 2010/11, corresponding to around 32 million taxpayers. For further details, see HM Revenue and Customs KAI Data, Policy and Co-ordination (2014) and Burkhauser et al. (2016). The data are comparable over time, except for a small discontinuity between 1995/96 and later years (the effect of which I show later). Self-assessment was introduced that year and there were changes to the SPI methodology (personal communication with HMRC). Hence, I use 1996/97 as the base year for analysis of inequality trends rather than 1995/96.

Throughout the period of my analysis (and since 1990), the unit of assessment in the UK income tax system has been the individual. For this reason, the SPI income variables are all individual-level variables, rather than referring to the incomes of families or households (as in the survey data and official income distribution statistics). The SPI income variable I use is *individual gross income* (total taxable income from the market plus taxable government transfers, and before the deduction of income tax), i.e. the same variable that the WTID and the top income shares literature focuses on.

In addition, and to further align my research with the WTID and top income shares literature, I restrict analysis to the population of individuals aged 15 years or more. Because the SPI does not cover all individuals in the UK population or all of their income, the WTID

uses external population and income control totals for each year, i.e. estimates of the total number of individuals aged 15 or more, and of the total income held by them. I use the WTID control totals throughout. In practice, I accomplish this by introducing some observations with zero income into each year's unit record data and adjusting the grossing-up weights supplied with the data.

The unit record survey data I employ come from the *Family Resources Survey* (FRS), and the accompanying subfiles of derived income variables called the *Households Below Average Income* (HBAI) dataset (Department for Work and Pensions 2013, Department for Work and Pensions et al. 2014). I use data for the same period as the SPI data, 1995/96–2010/11. The FRS is a large continuous cross-sectional survey with data released annually for around 20,000 respondent households and the individuals within them. The Department for Work and Pensions (DWP) administers the FRS, and DWP staff produce the HBAI subfiles that they use to derive the UK's official income distribution statistics published annually using a variant of Approach B, i.e. the 'SPI adjustment'. (Despite its label, the HBAI provides information about the income distribution as a whole.) In essence, the HBAI subfiles contain a set of FRS income variables that DWP statisticians have cleaned.

Because the DWP's focus is on family and household post-tax post-transfer income variables (reflecting the needs of official statistics), there is a definitional mismatch between the income variables in the HBAI and the SPI. As it happens, the DWP's public-use files do contain an individual-level gross income variable but only from 2005/06 onwards.

Burkhauser et al. (2016) create a complete time series for the period 1995/96–2010/11 (as for the SPI data) from FRS variables and show that their derived individual-level gross income variable is virtually identical to the DWP's for the years for which they can make comparisons. I use Burkhauser et al.'s individual gross income variables derived from the HBAI in this paper. (None of these variables are SPI-adjusted in the sense described earlier.) Burkhauser et al. (2016) go on to create a second set of individual-level income variables when implementing Approach B. These data reflect a more extensive 'SPI adjustment' procedure than employed by the DWP for the official statistics, and Burkhauser et al. (2016) label it 'SPI2' accordingly.

In sum, there are two main individual-level gross income data series employed in the paper to implement Approach C: that from the tax data ('SPI') and from the DWP's cleaned-up survey data ('HBAI'). In Section 5, I contrast my results for overall inequality based on the SPI and HBAI series (combining estimates) with those derived using Approach B (combining data). I refer to the DWP's (2015) inequality series as 'HBAI-SPI' and the

Burkhauser et al. (2016) series as 'HBAI-SPI2'.

To fully align the survey data with the tax return data, I restrict attention to individuals aged 15 years or more. I use the FRS weights in all calculations with the survey data and SPI weights with the tax data ones. All income variables (from tax and survey data) are expressed in pounds per year in 2012/13 prices.

3. Under-coverage of top incomes by household survey data

Ascertaining the point on the income range at which survey under-coverage of top incomes begins is an integral part of implementing Approaches A and C and of independent interest as well.

Table 1 shows estimates of percentiles *p*90, *p*95, *p*99, *p*99.5 and *p*99.9 derived from the survey and tax data as well as the ratio of each corresponding survey and tax data estimate (in %), by year. (For brevity, henceforth I refer to tax years 1995/96 as '1995', 1996/97 as '1996', and so on.) Real incomes at the top of the distribution generally rose over the period according to either source (look down each column of Table 1), except that there is fall in the uppermost percentiles after 2007, especially in the tax data estimates.

<Table 1 near here>

There are two explanations for the post-2007 fall in the uppermost percentiles. One is the recession at that time. The second, particularly relevant here, is the incentive for high income taxpayers to declare income in tax year 2009/10 rather than 2010/11 in order to avoid the increase in top marginal tax rate from 45% to 50% with effect from April 2010. The subsequent reintroduction of the 45% top marginal rate with effect from April 2013 provided an incentive to defer declaration of income. On these issues of 'forestalling' and 'reverse forestalling', see HM Revenue and Customs (2012). Because of these issues (and having no SPI data for 2008), although I provide annual estimates for the full period between 1995 and 2010, I mostly focus discussion on inequality trends through to 2007.

Table 1 provides clear evidence of under-coverage in top incomes and that its nature changed over the period. Survey estimates of the very top percentiles are more volatile over time than are the tax data estimates, which is indicative of the sparsity aspect of under-coverage. Regarding under-coverage per se, look at the 'ratio' columns: values less than 100% suggest under-coverage. Throughout the period, there is a broad correspondence between survey and tax incomes up to around *p*99. In the mid- to late-1990s, one might refer

to 'over-coverage' of the survey up to p95. However, in the 2000s, there is a substantial uplift in the very highest incomes shown by the tax data. This is not picked up by the survey data. Between 2000 and 2007, the ratio of survey p99 to the tax data p99 fell from around 100% to 82%. There is a similar decline in the corresponding ratio for p99.5 starting from around 1997 (when it was 100%), down to 78% in 2007. These changes in under-coverage over time suggest that it may be inappropriate to use the same percentile cut-off to define the top income group for all years. I return to this issue. This aside, the table also suggests that the optimal threshold for application of Approach C (or A) should not be lower than p95, because survey coverage is adequate up to this point.

Figure 2 provides a complementary perspective on the nature of survey under-coverage. It focuses on 1996 and 2007; the full series for all years is shown in Appendix A. I show densities derived from a histogram for the full distribution of log(income) in the survey data and for the tax data for each year. (I use the logarithmic scale in order to focus on the upper tail.) There are three plots for each year. The leftmost one shows densities plotted for log(income) greater than 10 (i.e. income > £22,026), and the vertical dotted lines mark p90, p95, p99, and p99.5 for the relevant year. The other two graphs provide more detailed views on the upper tail by plotting the same densities by plotted only for log(income) greater than 11 (i.e. income > £59,874; middle graph) and log(income) greater than 12 (i.e. income > £162,755; rightmost graph). Histogram areas reflect survivor function proportions, and so comparisons of areas provide information about under-coverage in the sense of how much of top income being captured by the survey data. The histograms also provide information about sparsity and 'outlierness' in top income ranges. Sensitivity issues are likely to be more important, the more that the histograms do not approximate a continuous function and show clumping of density mass.

<Figure 2 near here>

The leftmost plots suggest that the concentration of incomes in the tax and survey data is quite similar for most of the income range if one focuses on the top 5% to 10% of the distribution as a whole. Coverage, summarised by differences in histogram areas, is not so different – though it is clearly worse in 2007 than 1996. Both survey and tax densities appear quite smooth and continuous, though the tax data distribution has a long tail that is not present in the survey data, especially in 2007.

However, differences in income concentration across data sources are much more apparent if one focuses on the extreme top: look at the middle and rightmost plots. In 1996, both densities are discontinuous: extreme incomes are spread sparsely across the top income

range, and this range is much greater for tax data. There are greater proportions at the very top in the tax data than in the survey data (the total area of the dark bars is greater than the total area of the light bars). By 2007, and with the secular growth of incomes over the previous decade (Table 1), the survey data are even more clumpy and the proportion with extremely high incomes is more markedly less than for the tax data. In the tax data, the density is relatively continuous up to extremely high incomes.

Overall, Figure 2 and Appendix A suggests that, from the point of view of survey undercoverage of top incomes, the cut-off used to implement Approach C (or A) should lie at around p95 or higher, depending on the year. In addition, the sparse spread of incomes along the very top income range means that there are potentially 'high leverage' outliers (Cowell and Flachaire 2007) even in the tax data, and these could bias non-parametric estimates of inequality indices and also estimation of Pareto model parameters. I address these issues below.

4. Fitting Pareto models to top incomes

An integral part of inequality estimation using Approaches A and C is to fit a parametric model to top income data, but there are implementation issues concerning the choice of model and the top income range over which they are fitted. There is also a prior question of whether top incomes are described better by a model other than a Pareto one. This issue has rarely been addressed though one exception is Harrison (1979, 1981) who compares the fit to UK men's top earnings data of Pareto I, lognormal, and sech² distributions. Addressing all these issues is complicated by a chicken and egg problem: most methods for choosing the appropriate model are conditional on a given threshold; and most methods for choosing the threshold have been applied to a single model. One can use multiple models and thresholds but there can be an information overload, and this is and potentially worsened by having 15 years of data covering a period when the income distribution changed. What is appropriate for one year's data may not be appropriate for another. To address the implementation issues, I have had to make some judicious choices regarding empirical strategy and what I report. A full set of estimates is provided in appendices.

My analysis focuses on comparisons of Pareto I and Pareto II models fitted to SPI tax data. In this section, first I explain the model properties and different parameter estimation methods. (Important references on Pareto distributions include Arnold 2008, 2015, Coles

2001, Cowell 2011, 2015, and Kleiber and Kotz 2003.) Next, I report on tests checking whether Paretianity is an appropriate assumption, and whether answers depend on the income threshold used. Then I consider the relative goodness of fit of Pareto I and II models using two methods and multiple thresholds. Finally, I address the choice of threshold issue using both rule-of-thumb and more formal statistical methods. Overall, I demonstrate that the choice of model and threshold is not as clear cut as typical practice might suggest.

Pareto Type I and Type II models

If income x is characterised by a Pareto Type I model, the survivor function showing the fraction of the population with incomes greater than x, S(x), i.e. one minus the cumulative distribution function, F(x), is:

$$S(x) = 1 - F(x) = \left(\frac{x}{x_m}\right)^{-\alpha} \tag{1}$$

where $x \ge x_m > 0$, and $x_m > 0$ is the lower bound on incomes. Parameter α is the shape parameter ('tail index') describing the heaviness of the right tail of the distribution, with smaller values corresponding to greater tail heaviness. The k^{th} moment exists only if $k < \alpha$.

The survivor function for the Pareto Type II model is:

$$S(x) = \left[1 + \xi \left(\frac{x - \lambda}{\sigma}\right)\right]^{-\frac{1}{\xi}}, \xi > 0$$
 (2)

where $x > \lambda$ (a location parameter), and $\sigma > 0$ is a scale parameter. Parameter ξ is the shape parameter. In principle, ξ can take on any real value (including the limiting case of $\xi = 0$, which implies an exponential distribution), but the restriction $\xi > 0$ yields heavy-tailed distributions of the 'Pareto' kind. The k^{th} moment exists only if $k < 1/\xi$. The Pareto Type I and II models are equivalent when $\xi = 1/\alpha$, $\lambda = x_m$, and $\sigma = x_m/\alpha$. With one additional parameter, the Pareto Type II model has the potential to fit real-world top incomes better. But the improvement in goodness-of-fit may be negligible and this has be balanced against the greater simplicity of the Pareto I model.

To implement Approaches A and C, we need formulae for the mean and inequality for the top income group (those with incomes greater than x_m or, equivalently, λ) expressed in terms of the model parameters. I display the formulae for these statistics in Table 2, and clearly they are simpler for the Pareto I model.

<Table 2 near here>

Estimation

Estimation of the two Pareto models proceeds by assuming x_m or μ is a threshold prespecified by the researcher (not estimated) with its choice determined by a simple rule-of-thumb (such as the 95th or 99th percentile) or other means. I return to this issue below.

There are two methods commonly used to estimate the Pareto I shape parameter α . The first is an Ordinary Least Squares (OLS) regression of the log of empirical survivor function on the log of income and a constant term. The idea is that, if eq. (1) holds, then the Zipf plot – a plot of the log of the survivor function against logarithms of income (for incomes in ascending order and greater than x_m) – is a straight line with slope equal to $-\alpha$. Atkinson (2016) explains that α may be estimated by OLS in two other ways. (The Zipf approach uses data on income and the survivor function; the other two approaches utilize information about the total income received by income units.) I have estimated α using all three methods, but find that the Zipf method performed best, and so report only estimates from this in the main text. For the full set of estimates for all years, see Appendix B.

The OLS estimate of α is consistent (Quandt 1966) but the standard error is incorrect because no account is taken of the positive autocorrelation in the residuals introduced by the ranking of incomes. In contrast, the Maximum Likelihood (ML) estimator of α and its standard error is consistent, efficient, and asymptotically normal (Hill 1975, Quandt 1966). I implement the ML estimator using software by Jenkins and Van Kerm (2015). Both OLS and ML estimators are potentially biased in small samples, but the sample sizes in the tax return data employed in this paper are never 'small' – an advantage of using this source.

The ML estimator of α is susceptible to bias when there are a few high outlier incomes, the values of which may be potentially genuine or may reflect error and data contamination in the sense of Cowell and Victoria-Feser (1996, 2007) and Cowell and Flachaire (2007). The influence function for the ML estimator is unbounded in this situation. Figure 2 (and Appendix A) suggest that this issue may be relevant, even for tax data. I address this potential problem by using the ML 'Optimal b-robust estimator' (ML-OBRE) of Ronchetti and Victoria-Feser (1994). (The software implementation is by Van Kerm 2007.) The idea is to use the ML score function for most of the data (and exploit the efficiency of the ML estimator) but to place an upper limit c on the score function for high values in the interests of robustness. Ronchetti and Victoria-Feser (1994) show that, with 95% efficiency, the optimal value in the Pareto case is c = 3, and this is what I use. I use both ML and ML-OBRE estimators because only the former can be used for likelihood ratio tests of Pareto I

versus Pareto II models. Differences between their estimates are indicative of the empirical importance of the robustness problem.

There are several estimators of the Pareto Type II model: see e.g. Singh and Guo (2009) for a review. However, ML is the most commonly used and provides consistent, efficient and asymptotically normal estimates. The software implementation is by Roodman (2015); software for an ML-OBRE estimator is not available.

Are top incomes Pareto distributed?

Researchers commonly check for Pareto properties by inspecting whether Zipf plots are linear above some income threshold (while perhaps discounting apparent non-linearity in the very highest income range given the sparsity of observations there). However, Cirillo (2013) argues persuasively that we should not check Paretianity in this way: our eyes are unreliable detectors of linearity, and what we see as linearity is also consistent with non-Pareto distributions including lognormal distributions that do not have a heavy tail. As it happens, Zipf plots for each year of SPI data do appear roughly linear above a threshold (with the exception of 1995 – see below). However, given Cirillo's critique, I relegate these plots to Appendix C.

Mean excess plots are another tool used for checking Pareto properties. They plot mean income above a threshold against a series of thresholds. For Pareto distributions, the graph is a positively-sloped straight line above some minimum income; deviations from linearity are evidence of non-Paretianity. I show mean excess plots for selected years in Figure 3, using thresholds ranging from £10,000 per year to £600,000 per year. The graphs also show pointwise 95% confidence bands. The estimates for all years are shown in Appendix D.

<Figure 3 near here>

It is difficult to draw definitive conclusions from the mean excess plots. On the one hand, the plots are roughly linear at thresholds above approximately £50,000 per year though perhaps accompanied by some small decrease in slope at extremely high thresholds. On the other hand, in every plot, confidence intervals (CIs) become very wide as the income threshold increases (there are few observations at extremely high incomes), and so it is difficult to cite non-linearities with confidence. The plot for 1995 is an exception because non-linearity is much clearer. However, this is no doubt due to the SPI discontinuities cited in the previous section. The non-linearity in the 1996 plot arises at thresholds of £300,000 or more and hence relates to a tiny number of incomes.

Cirillo (2013: 5983) also points out that mean excess plots provide a reliable means of differentiating between Pareto distributions and lognormal distributions only if the number of observations is very large (he mentions 10,000). The most reliable conclusion that we can draw from the mean excess plots (and Zipf plots) is that there is no decisive rejection of Paretianity.

Zenga curves provide a much better means for discriminating between different types of model (Cirillo 2013). A Zenga curve, Z(u), is a transformation of the Lorenz curve:

$$Z(u) = \frac{u - L(u)}{u[1 - L(u)]}, 0 < u < 1,$$
(3)

where L(u) is the Lorenz curve for the distribution of incomes above a pre-specified threshold. For Pareto distributions, the Zenga curve is positively-sloped and rises as $u \to 1$ and, the higher the curve, the more heavy-tailed the distribution is. By contrast, for a lognormal distribution, the Zenga curve is horizontal. Figure 4 shows plots for 1996 and 2007 for thresholds of £60,000 and £120,000 (the higher threshold provides greater resolution over the top income range). See Appendix E for other years and thresholds.

The Zenga plots provide strong evidence in favour of Paretianity for all years (with the exception of 1995 for the reasons cited earlier.) At the same time, the location and precise shape of the curves changes over time and with threshold. This suggests that not only do Pareto tail indexes vary from year to year but also with the threshold chosen. I return to these issues below.

<Figure 4 near here>

Which distributional model for top incomes? Pareto I or Pareto II?

We cannot reliably differentiate between Pareto Type I and Type II models with these graphical checks. To do this, I use two approaches. The first is a straightforward likelihood ratio test. The second is comparisons of probability plots, specifically 'PP' plots graphing values of p = F(x) predicted from each model against the values of p in the data, with a different plot for each threshold. Plots that lie wholly along the 45° line from the origin indicate perfect goodness of fit. The better fitting model is the one with less deviation from the 45° line.

Figure 5 summarizes likelihood ratio test statistics – equal to twice the difference in estimated log-likelihoods of ML-estimated Pareto I and II models – for thresholds up to £300,000 for 1996, 2001, 2007, and 2010. I cap the test statistics at 100 for plotting purposes. The dotted lines show critical values of the $\chi^2(1)$ distribution at significance levels 0.05, 0.01,

and 0.001. (Plots for other years are in Appendix F.) Regardless of the critical value chosen, the findings are clear. Using a likelihood criterion, we should choose the Pareto I model over Pareto II only if the threshold used to fit the models is extremely high. For 1996, the balance in favour of Pareto II is at all thresholds below around £100,000, which lies between p99 and p99.5. For the other three years shown in Figure 5, the cut-off threshold is at the same high level or even higher, and hence above the income level at which survey non-coverage starts (Table 1, Figure 2). The plots for other years confirm this general finding.

<Figure 5 near here>

The PP plots shown in Figure 6 compare model goodness of fit over the full range of incomes above the pre-specified threshold. Plots for the Pareto I model are on the left and for the Pareto II model on the right. For brevity, I show results only for 2007 and thresholds of £60,000 and £80,000 (between p95 and p99 in 2007), with plots for other years and thresholds in Appendix G. The fit of each model is good: the curves shown are closer to the 45° line than most textbook illustrations of PP plots. However, there is evidence that the Pareto II model fits better than Pareto I at the lower of the two thresholds (consistent with the likelihood ratio test findings). Below the median of the left-truncated distribution, Pareto I under-predicts empirical probabilities. More evidence in favour of Pareto II is apparent for other years and thresholds (see Appendix G). Overall, probability plots provide evidence in favour of the Pareto II model over the Pareto I model, but the differences in goodness of fit are generally not large.

<Figure 6 near here>

The results from the two types of goodness of fit check suggest that the choice between Pareto models is threshold-contingent. What, then, is the optimal threshold?

What is the optimal high income threshold?

Clauset et al. (2009) and Coles (2001) review methods for determining the threshold. The most commonly-used approaches are reviews of Zipf plots or minimum excess plots, as discussed above. Another intuitively attractive approach is to plot estimated parameters against thresholds and to choose as optimal threshold, the minimum income above which the plot is horizontal. For the Pareto I model the plot is of fitted α against threshold t; for the Pareto II model, the plots are of fitted ξ and 'modified scale parameter' $\sigma^* = \sigma \xi - t$ against t (Coles 2001: 83).

Clauset et al. argue against these 'subjective' approaches and in favour of a 'more objective and principled approach based on minimizing the "distance" between the power-law model and the empirical data' (2009: 670). After reviewing alternatives, they favour measuring distance between fitted and empirical distributions using the Kolmogorov-Smirnov (KS) statistic, i.e. the maximum distance between their cumulative distribution functions, *D*:

$$D = \max_{x \ge x_m} [F(x) - P(x)] \tag{3}$$

where F(x) is the empirical CDF for incomes at the threshold x_m or above and P(x) is the model-predicted CDF over the same range. (D is thus a numerical summary of information shown in a PP plot.) The optimal threshold is the value of x_m that minimizes D.

Figure 7 displays plots of estimated parameters against thresholds for both models, for 1996 and 2007. (Plots for other years are in Appendix H.) The vertical dashed lines show, from left to right, the percentiles *p*90, *p*95, *p*99, and *p*99.5 in the SPI data.

The figure shows that the choice of estimator matters when fitting a Pareto I model. On the one hand, the OLS estimator produces estimates of α that are distinctly smaller than those derived from ML and ML-OBRE estimators, except at extremely high thresholds. On the other hand, the ML and ML-OBRE estimates are remarkably similar.

Regardless of estimator, the choice of threshold for the Pareto I model is not clear cut if the information in Figure 7 and Appendix H is used as the guide. The graphs are relatively flat only at extremely high thresholds, though the flattening out occurs at thresholds that are lower in later years – but they are very high nonetheless. The pattern for 2007 is also apparent from the start of the 2000s (Appendix H). Put differently, if we restrict the range of thresholds to between p95 and p99.5, i.e. in the range commonly used, then in 1996 the estimate of α varies between around 2.5 and 2. This is a wide range: it corresponds to Gini coefficients between 0.25 and 0.33 (according to the formula in Table 2). For 2007 and over the same range, the α estimates vary between 2.2 and 1.8, and hence Gini coefficients between 0.29 and 0.38.

In contrast, this sensitivity of parameter estimates is not apparent for the Pareto II model for thresholds in the range of *p*95 and *p*99.5. The curves are relatively flat and there is evidence for an optimal threshold lying between *p*95 and *p*99, with the precise range depending on the year.

Figure 8 displays optimal thresholds derived using the KS minimum distance criterion for both Pareto models. For the Pareto I case, the optimal thresholds are very similar for each year for ML and ML-OBRE estimators, with the exception of 1996 and 2004. It is striking that the optimal thresholds for the Pareto I model are typically much larger than those for the Pareto II model (except in 2007). For the Pareto I model, the optima are at around *p*99.5 or higher; for the Pareto II model, they are at about £50,000 which corresponds to around *p*99 in the mid- to late-1990s or *p*95 in 2000. Although there is variation in the estimated optimal threshold from year to year, there is much less variability in the optima derived for the Pareto II model than for those derived for the Pareto I model.

<Figure 8 near here>

The general lesson of this analysis is that Pareto I model estimates from top income data are sensitive to the choice of threshold, and perhaps more so than has been appreciated by researchers to date. Put differently, the range of thresholds for which the Pareto I model estimates are stable is well above the thresholds commonly used. Pareto II model estimates are more robust to the choice of threshold.

The specific lesson for applications of Approach C (and A) to determining total inequality is that estimates may be sensitive to choice of both the model of top incomes and the threshold. The criterion regarding threshold choice discussed earlier – that it should be in the income range at which survey under-coverage becomes apparent – further complicates matters. For the period considered here, this criterion implies a threshold somewhere between p95 and p99, with the former more appropriate in later years, the latter more appropriate in earlier years. This income range is broadly consistent with optimal thresholds derived for the Pareto II model but not those for the Pareto I model. In the light of these results, and in order to check the robustness of findings about overall inequality, my implementation of Approach C uses both Pareto models and multiple thresholds.

5. UK income inequality: estimates from combining estimates and combining trends

To implement Approaches C and A, we exploit the properties of inequality indices that are additively decomposable by population subgroup. For all such indices, we may write:

+ between-group inequality

where between-group inequality is the inequality that would arise if each individual is attributed the mean of his or her income group. Additively decomposable indices include all members of the generalized entropy class I_a , including the mean logarithmic deviation (I_0 or L'), the Theil index (I_1 , L'), and half the squared coefficient of variation (I_2 , HSCV), that were cited in Table 2. The larger that L' is, the more sensitive is L' to income differences at the top of the distribution compared to the bottom. HSCV is particularly top-sensitive. Because the incomes of the top income group and the non-top income group do not overlap (by construction), the Gini coefficient is also additively decomposable in this context. For further discussion of decomposable inequality indices, see inter alia, Cowell (1980) and Cowell and Kuga (1981).

The decomposition formula for the Gini coefficient, *G*, derived by Atkinson (2007) and Alvaredo (2011), is also set out clearly by Cowell (2013: 43):

$$G = P_R S_R G_R + P_N S_N G_N + G_B. (5)$$

 P_R is the proportion of the population in the top income group ('Rich') in a given year; $P_N = 1 - P_R$ is the proportion of the population in the non-rich group; $S_R = P_R \mu_R / \mu$ and $S_N = P_N \mu_N / \mu$ are the shares in total income of each group; μ_R and μ_N are the group mean incomes; and $\mu = P_R \mu_R + P_N \mu_N$ is the overall mean. Between-group inequality $G_B = S_R - P_R$.

Pareto I and Pareto II models fitted using the same threshold and data provide different estimates of total inequality G in a given year because they imply different estimates of G_R and μ_R . (G_R and μ_R may also be estimated non-parametrically: see below.) A higher estimate of μ_R from one model implies larger S_R and G_B . That model's estimate of G will be greater as well unless the higher μ_R coincides with a sufficiently lower value of G_R . For either model, what happens to estimates of G when one changes the threshold (and thence P_R) is less clear cut because there are changes in G_N and μ_N as well as in G_R and μ_R .

The researcher has to choose the value of P_R . In the light of the analysis in previous sections, I use three thresholds for each year, p99, p95, and p90, estimating them non-parametrically from the *survey* data. (Although p90 is substantially below the thresholds discussed earlier, I include it as a robustness check; it has been used by Ruiz and Woloszko 2015.) Because the survey estimates differ from their tax data counterparts (Table 1), P_R in the *tax* data is close to but not exactly equal to 1%, 5%, or 10% respectively (see Appendix I for the values for each year). I also estimate μ_N and G_N non-parametrically from the survey data, and μ_R and G_R , L_R , and T_R from the estimates of the two Pareto models using the

formulae shown in Table 1. (I report estimates for Pareto I derived using the ML-OBRE estimator.)

I calculate the combined estimate G using the formula in (5) and employ analogous steps to calculate estimates of L and T. I could not derive T for the Pareto II model (there were numerical integration problems) and I did not calculate HSCV because of its strong top-sensitivity and because the requisite moments of the fitted Pareto distribution do not always exist (Figure 7, Appendix H). Appendix I contains the estimates derived from the SPI data of the Pareto model parameters and their standard errors; μ_R , G_R , L_R , T_R and their standard errors (derived from the Pareto parameters using Table 2 formulae; and also calculated non-parametrically), plus μ_N and G_N , L_N , and T_N (derived non-parametrically from HBAI data). Appendix I also contains the combined estimates G, L and T, for all years, and for each of the three sets of estimates of mean income and inequality among the Rich. I focus discussion initially on the Pareto model-based estimates for the Gini coefficient, and later compare them with the fully non-parametric estimates, together with corresponding estimates for L and T.

Figure 9 charts the Pareto-based estimates of mean income among the Rich (μ_R), the share of total income held by the Rich (S_R), inequality among the Rich (G_R), and the overall combined estimate (G), for each of the three percentile thresholds. The Pareto I estimates are on the left; the Pareto II estimates are on the right.

The headline finding is that income inequality summarized by the Gini coefficient distinctly increased between the mid-1990s and 2007: see panel (a). It then fell back to late-1990s levels by 2010, though assessment of the fall is complicated by the forestalling issues mentioned earlier. Most of the inequality increase occurred between 2004 and 2007. These conclusions hold regardless of which Pareto model and threshold is used.

<Figure 9 near here>

Using a higher threshold leads to higher estimates of μ_R , S_R , and G_R in each year, for both Pareto models, and especially going from $P_R = 5\%$ to $P_R = 1\%$. The S_R estimates closely track those shown in the World Top Incomes Database for the UK (based exclusively on SPI data), though there are some differences in levels (the S_R depend also on survey data).

However, when looking at overall inequality summarised by G, the Pareto II estimates are less sensitive to the choice of threshold than are the Pareto I estimates: see panel (a). Each yearly Pareto II estimate of G differs by at most one percentage point across series for the three thresholds (in the mid-1990s), and the series for $P_R = 5\%$ and $P_R = 10\%$ are virtually identical up to 2006. For the Pareto I model, the corresponding range is larger, reaching a

maximum of around 2.5 percentage points (2009). Otherwise, again, the largest differences are between the series for $P_R = 1\%$ on the one hand, and $P_R = 5\%$ or 10% on the other hand. The variation in estimates relates back to the earlier findings regarding choice of the optimal threshold. The thresholds used in this section correspond to range of optimal thresholds for the Pareto II model, but well below those for the Pareto I model.

I now contrast my estimates of inequality trends derived using Approach C with estimates derived using other approaches. For brevity, I show only the results for $P_R = 5\%$: see Figure 10. Conclusions are largely insensitive to choice of threshold in any case: for the corresponding graphs for the other two thresholds, see Appendix I.

The three series of Approach C estimates ('HBAI & SPI' variants) differ according to whether top incomes are summarised using the Pareto I or Pareto II models or nonparametrically. There are two HBAI series showing trends in inequality for the poorest 95% and the poorest 100% of the survey data, i.e. not including any information from the tax data. The HBAI-SPI series uses the estimates in the UK official income statistics derived using a variant of Approach B (the DWP's SPI adjustment, cited earlier). It is important to note that the HBAI-SPI series uses a different income definition and refer to a different population than all of the other series shown in the figure. It refers to inequality of equivalized household net income among all individuals (adults and children) rather than to individual gross income among adults. Estimates of inequality levels based on HBAI-SPI definitions are smaller than estimates based on the tax data definition, but the differences in definitions have little effect on estimates of inequality trends (Burkhauser et al. 2016). The HBAI-SPI2 series is from Burkhauser et al. (2016) and uses a different variant of Approach B (see earlier). I summarise inequality not only using the Gini coefficient (panel a), but also using L and T (panels b and c). The DWP does not publish estimates for L or T: I derived them non-parametrically from public use HBAI unit record data.

<Figure 10 near here>

Figure 10 shows that if one restricts attention to the poorest 95% in the survey data each year, all three indices show a marked decline in inequality over the period as a whole. (These estimates are unlikely to be contaminated by the 'forestalling' issue.) Inequality also appears to be falling according to the series that uses 100% of the survey data observations (the Gini fell by around 5% between 1996 and 2007), but another distinctive feature of the series is its volatility. This is particularly acute for the Theil index, which is unsurprising because it is the most top-sensitive of the three indices. Thus Figure 10 illustrates well the sensitivity problems analysed by Cowell and Flachaire (2007) and also their conclusion that

in terms of performance in finite samples there is little to choose between the Gini coefficient and the mean logarithmic deviation (L). But what happens if one utilizes information about top incomes from tax data?

According to all three Approach C variants, and all three inequality indices, inequality increased between 1996 and 2007. The Gini coefficient increased by around 5% according to the Pareto I estimates, by around 8% according to the Pareto II estimates, and by around 7% according to the non-parametric ones. For *L*, the corresponding increases are 1%, 5%, and 4%. For *T*, the increase in the Pareto I estimate is 24% and 33% for the non-parametric estimate. These results indicate that using a Pareto II model for top incomes leads to larger estimates of the rise in inequality over this period than does a Pareto I model, not only according to the Gini coefficient (Figure 9) but also according to *L*. In addition, the Pareto II estimates of trends in *G* and *L* are quite similar to the non-parametric ones. This is reassuring evidence for analysts that the Pareto II model provides a parsimonious but good description of distributions of top incomes. Using a more top-sensitive index (*T* rather than *L*) leads to a greater estimated increase in inequality, reflecting the marked increase is top income shares over the period.

Figure 10 also shows how the three Approach C estimates of inequality trends compare with the two Approach B series. The Burkhauser et al. (2016) HBAI-SPI2 series is very similar to the Pareto I-based Approach C series for all three inequality indices.

By contrast, trends in the DWP's official statistics series (HBAI-SPI) appear at first sight to differ markedly from those of all three Approach C estimates and for all three inequality indices. However, closer inspection of the figure reveals that the differences in trends arise almost entirely between 1996 and 1998. The official series shows a sharp increase in inequality over those two years; trends are much more similar across series in subsequent years. It is difficult to explain the sub-period inconsistency across series. One possible source is the way in which the DWP's SPI adjustment derives the cell mean estimates for top income groups. According to Department for Work and Pensions (2015*a*: 11), values to be used in year *t* of the HBAI data are derived by HMRC statisticians by 'projections' from SPI data for year *t*-1 (because year *t*'s SPI data are not yet available). No further details of the projection method are given. By contrast, all my Approach C estimates and Burkhauser et al.'s (2016) Approach B estimates combine information HBAI data for year *t* and SPI data for year *t*. I conjecture that a larger than usual difference between projected cell-means and actual out-turns for 1996–1998 are the source of the inconsistency

observed for that period. The public-use SPI data do not contain the variables that would allow me to check if this is the case.

In sum, apart from the exceptional and short sub-period just discussed, there is substantial consistency across the different methods for combining survey data and tax data about top incomes. Compared to the estimates that are wholly survey-based, all show a rise in income inequality over the decade prior to the onset of the Great Recession, whereas the estimates that are wholly survey-based show no increase in inequality.

6. Summary and conclusions

Statistical agencies and other researchers typically estimate income inequality levels and trends from either survey data or tax return data, but rarely combine the information in the two types of data source. The result is that very different impressions about how inequality is changing over time may arise, as the examples for the UK and the USA in the Introduction show. Research users may reasonably ask what the 'true' picture of inequality trends is. There is a good case for providing them with answers using methods that combine information from survey and tax data in order to take advantage of the strengths of each source. In particular, tax return data provide better coverage of top incomes than do survey data; and survey data provide the ability to create income variables with the same definitions, so that combination is done on a like-for-like basis.

I have analysed income inequality levels and trends for the UK by combining inequality estimates from survey and tax data (Approach C), contrasting these estimates with those derived by combining data per se (Approach B). As part of this analysis, I have also provided new findings about survey under-coverage of top incomes in UK survey data (Section 3). The problem becomes apparent at around the 99th percentile in the 1990s but at around the 95th percentile in the 2000s.

I have found that that conclusions about aggregate UK inequality trends since the mid-1990s are broadly robust to the way in which tax data are employed in Approach C. One may conclude for example that the Gini coefficient for gross individual income rose by around 7% to 8% between 1996/97 and 2007/08, with most of the increase occurring after 2003/04. When I use only survey data, with tax data not exploited at all, the Gini coefficient is estimated to decrease by around 5% over the same period.

The result that combining information about top incomes from tax data with information about the rest of the distribution in survey data leads to an estimated increase in inequality is unsurprising given knowledge of survey under-coverage of top incomes and the marked rise in top income shares in the UK over the last two decades. But I have shown how we may go beyond the qualitative conjecture and provide specific quantitative estimates of inequality trends, and for a range of inequality indices.

The analysis highlights the continuing importance of normative judgements for inequality analysis. Different inequality indices incorporate different assumptions about how to evaluate income differences in different parts of the income distribution (Cowell 1977, 2011). A focus on the income share of the top 1% measure means that zero weight is placed on income differences among the poorest 99% or on differences between the rich and non-rich groups. This paper has considered inequality indices that give a non-zero weight to everyone. It is because of this, and because the rich are assumed to form such a small proportion of the population, that I estimate the increase in UK income inequality over the last two decades to be substantially smaller than the rise in the income share of the top 1% whether shown by the tax data alone or by the combined estimate (Figure 9).

The portfolio of inequality indices is also constrained by practical considerations: the indices used cannot be too top-sensitive. Application of the semiparametric Approach C is problematic if the distribution of top incomes is particularly heavy-tailed. Various moments of the fitted Pareto distributions do not exist in this case, and hence nor do many top-sensitive inequality indices (Figure 7; Appendix H). Cowell and Flachaire (2007) make this argument in the context of Approach A; I have shown that it also applies even if one uses tax data to describe top incomes. One might instead consider implementing Approach C using non-parametric estimates of top-sensitive inequality measures for the top income group, but I have found that such estimates are non-robust and volatile in the sense described in the Introduction, even using SPI tax data rather than HBAI survey data. (See the nonparametric estimates of the HSCV for the rich that are reported in Appendix I.)

In this paper, I have focused on inequality estimation issues related to data quality and ignored issues of statistical significance (as has virtually all previous work using Approaches B and C). It is relatively straightforward to estimate standard errors or the various elements in the inequality decomposition equation (1) using standard asymptotic formulae (these estimates are provided in Appendix I). However, there are non-trivial challenges to overcome in providing reliable inference for the overall inequality estimate. Cowell and Flachaire (2007, especially Section 3.3) discuss these issues with reference to generalised entropy

inequality indices. The case of the Gini coefficient appears not to have been discussed in the literature to date.

As part of deriving the substantive results about inequality levels and trends, this paper has also provided new evidence about which Pareto model to fit to the upper tail of a heavy-tailed distribution, and which threshold to use when doing this. Although the application has been to income, the analysis should be of broad interest because Pareto distributions are commonly used in many other contexts,. In his recent review of power laws in economics and finance, Gabaix argued that 'the Pareto law has survived the test of time: It fits still quite well. The extra degree of freedom allowed by a lognormal might be a distraction from the essence of the phenomenon' (2009: 285). He might have substituted 'Pareto II' for 'lognormal'. My analysis has shown that there is a good case for exploiting the extra degree of freedom provided by the Pareto II model, especially given the top income thresholds that are typically used (*p*99 or less). Put differently, the Pareto I model is as good as Pareto II only at extremely high incomes, beyond the range of thresholds usually considered. My conclusions refer to income rather than other variables such as wealth or city and firm size, and to the UK rather than to other countries, so checking the robustness of my findings in other contexts would be a useful topic for future research.

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Table 1. Percentiles of individual gross income (£ p.a., 2012/13 prices), survey and tax data estimates

Year		p90			p95			p99			p99.5	.
	HBAI	SPI	Ratio	HBAI	SPI	Ratio	HBAI	SPI	Ratio	HBAI	SPI	Ratio
1995	35,551	30,964	115	45,602	40,056	114	83,362	78,340	106	107,080	105,630	101
1996	37,028	31,209	119	47,623	41,043	116	85,141	80,869	105	109,948	113,469	97
1997	37,317	32,381	115	48,084	42,133	114	89,995	86,330	104	122,952	122,466	100
1998	38,285	33,595	114	50,485	44,541	113	95,853	92,694	103	127,830	131,499	97
1999	39,075	35,333	111	51,065	46,776	109	96,053	98,250	98	126,214	138,335	91
2000	40,371	37,273	108	53,048	49,786	107	106,413	105,722	101	142,586	150,871	95
2001	41,854	38,370	109	54,721	51,117	107	105,741	108,620	97	140,193	153,585	91
2002	41,360	38,498	107	54,401	51,370	106	103,532	108,742	95	136,152	153,379	89
2003	41,932	38,174	110	54,644	50,860	107	100,354	108,587	92	135,495	153,474	88
2004	42,460	40,575	105	55,847	53,533	104	107,367	114,855	93	144,244	165,249	87
2005	42,691	42,191	101	56,158	56,172	100	108,183	125,574	86	140,916	183,723	77
2006	43,335	42,885	101	56,101	57,369	98	109,910	131,012	84	157,894	193,230	82
2007	42,735	43,994	97	56,007	59,149	95	111,282	136,392	82	156,536	201,972	78
2008	43,312			56,703			109,812			143,624		
2009	42,564	41,917	102	56,839	55,782	102	113,420	124,753	91	156,384	183,777	85
2010	41,036	40,690	101	54,377	53,777	101	106,812	114,368	93	147,956	163,524	90

Notes. Author's estimates from HBAI (survey) and SPI (tax) data. Years refer to fiscal years ('1995' means 1995/96, and so on). No SPI unit record data have been released for 2008. Ratio: ratio of HBAI estimate to SPI estimate, in percent.

Table 2. Pareto Type I and Type II models: mean and inequality indices

Statistic	Pareto Type I	Pareto Type II
Mean	$\frac{\alpha x_m}{\alpha - 1}$, $\alpha > 1$	$\lambda + \left(\frac{\sigma}{1 - \xi}\right), \xi < 1$
Gini coefficient (<i>G</i>)	$\frac{1}{2\alpha-1}, \alpha>1$	$1 - \left[\frac{\lambda + 2\left(\frac{\sigma}{\xi^2}\right) B\left(\frac{2 - \xi}{\xi}, 2\right)}{\lambda + \left(\frac{\sigma}{\xi^2}\right) B\left(\frac{1 - \xi}{\xi}, 2\right)} \right], \xi < 1$
Mean logarithmic deviation (L)	$\log\left(\frac{\alpha}{\alpha-1}\right)-\left(\frac{1}{\alpha}\right)$, $\alpha>1$	No closed form expression
Theil index (T)	$\left(\frac{1}{\alpha-1}\right) - \log\left(\frac{\alpha}{\alpha-1}\right)$, $\alpha > 1$	No closed form expression
Half the coefficient of variation squared (HSCV)	$\frac{1}{2\alpha(\alpha-2)}, \alpha > 2$	$\frac{\sigma^2}{2(1-2\xi)[\lambda(1-\xi)+\sigma]^2}, \xi < \frac{1}{2}$

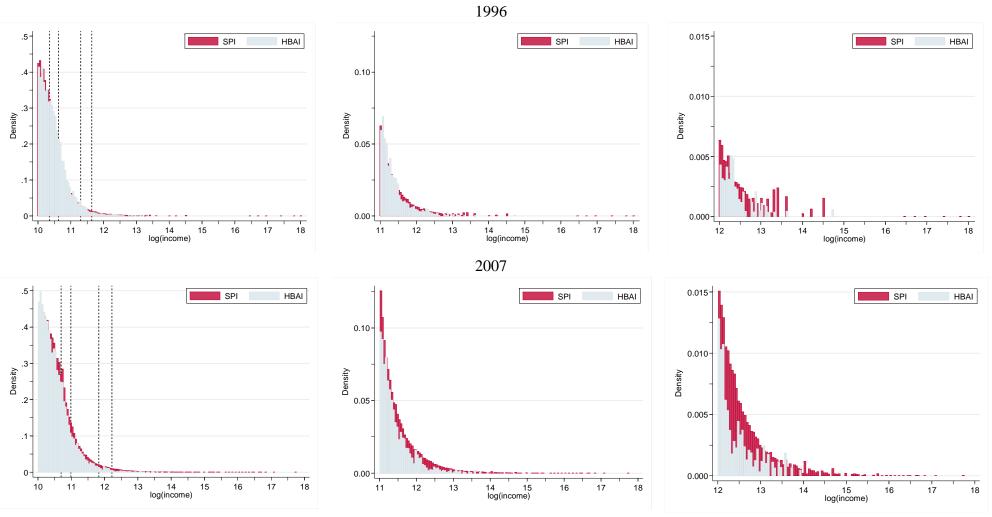
Notes. For the formulae for the survivor functions of the Pareto I and II models, see the main text. B(.) is the Beta distribution. Sources for formulae: Arnold (2008), Cowell (2007), Kleiber and Kotz (2003), and Singh and Guo (1995). L, T, and HSCV are members of the generalized entropy family of inequality indices, I(a), with a = 0, 1, and 2 respectively. Values of the L and T for the Pareto II distribution may be derived by numerical integration using the formulae for generalized moments in Cowell (1989), if the relevant moments exist.

Figure 1. Estimating inequality: approaches to addressing top income issues in survey data

Approach		Survey data		Tax data	Examples		
търноасн		Survey data		Tax uata	Dampies		
A.	Semi- parametric: combine summary measures derived from within the survey data	Gini (& other measures) for poorest (1–p)%		Not used	Alfons et al. (2013), Burkhauser et al. (2012), Cowell and Flachaire (2007), Ruiz and Woloszko (2015)		
		Pareto-estimated Gini (& other measures) for richest p% Combined Gini & other measures					
В.	Non- parametric: tax data cell- means replace top incomes in survey data	Survey	←	Tax data	Bach et al. (2009), Burkhauser et al. (2016), Department for Work and Pensions (2015)		
		Gini & other measures					
C.	Semi- parametric: combine inequality indices derived from survey and tax data	Survey data		Tax data	Atkinson (2007), Atkinson et al. (2011), Alvaredo (2011), Alvaredo and Londoño Vélez (2015), Diaz- Bazan (2015), Anand and Segal (2016), Lakner and Milanovic (2016), this paper		
		Gini (& other		Pareto-estimated			
		measures) for poorest		Gini (& other			
		(1–p)%		measures) for			
		1		richest p%			
		er measures)					
Combined Gini (& other measures)							

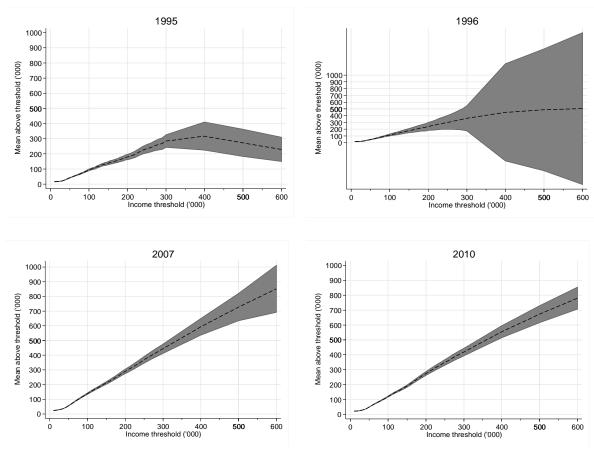
Note. Approach C may also be implemented using non-parametric estimates from tax data: see main text.

Figure 2. The concentration of income in high and extremely high income ranges: survey and tax return data compared, 1996 and 2007



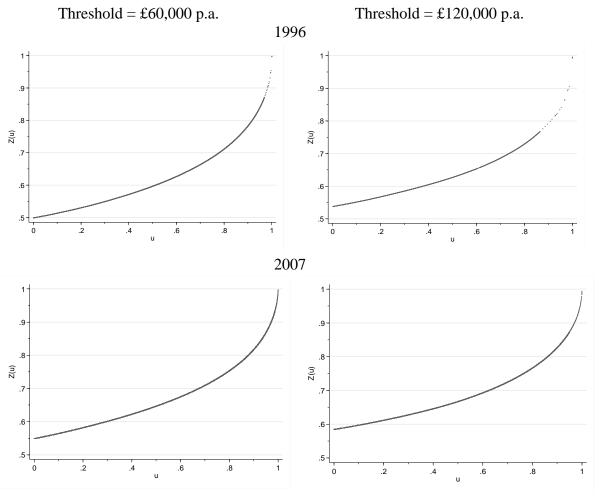
Notes. Author's estimates from SPI (tax) and HBAI (survey) data. Income is in £ per year, 2012/13 prices. Vertical dashed lines show (from left to right) p90, p95, p99, p99.5. For plots for other years, see Appendix A.

Figure 3. Mean excess plots for top incomes, tax return data, by year



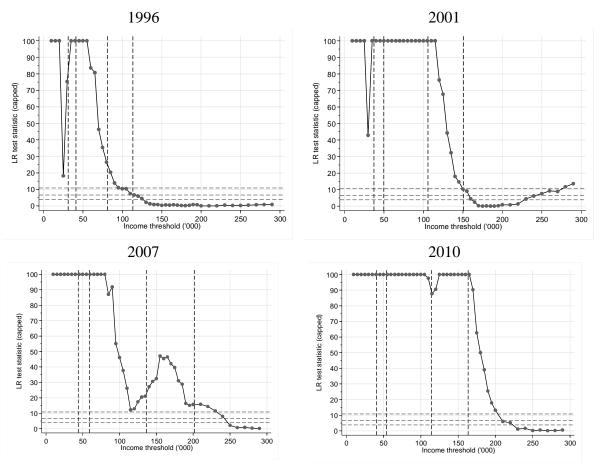
Notes. Author's estimates from SPI data. For plots for other years, see Appendix C. The shaded areas represent pointwise 95% confidence bands. Thresholds are in £ per year, 2012/13 prices. Plots estimated at intervals of £5,000 for thresholds between £10,000 and £200,000, £10,000 between £210,000 and £300,000, and £100,000 thereafter.

Figure 4. Zenga plots for top incomes, tax return data, by threshold and year



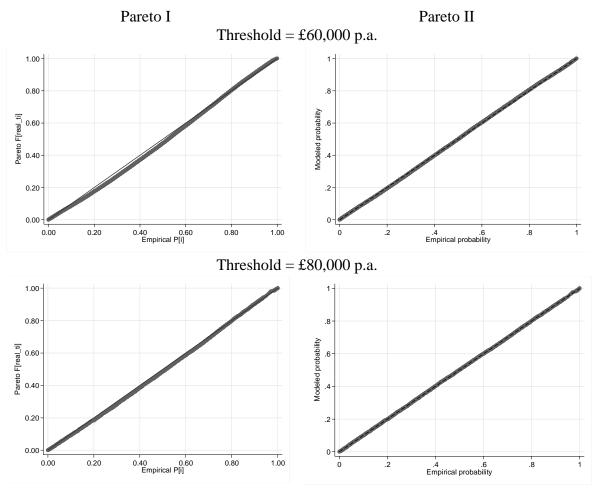
Notes. Author's estimates from SPI data. For plots for other years and thresholds, see Appendix D. On the Zenga plot, see the main text and Cirillo (2013).

Figure 5. Likelihood ratio test statistics (Pareto I versus Pareto II), by threshold: tax return data for 1996, 2001, 2007, and 2010



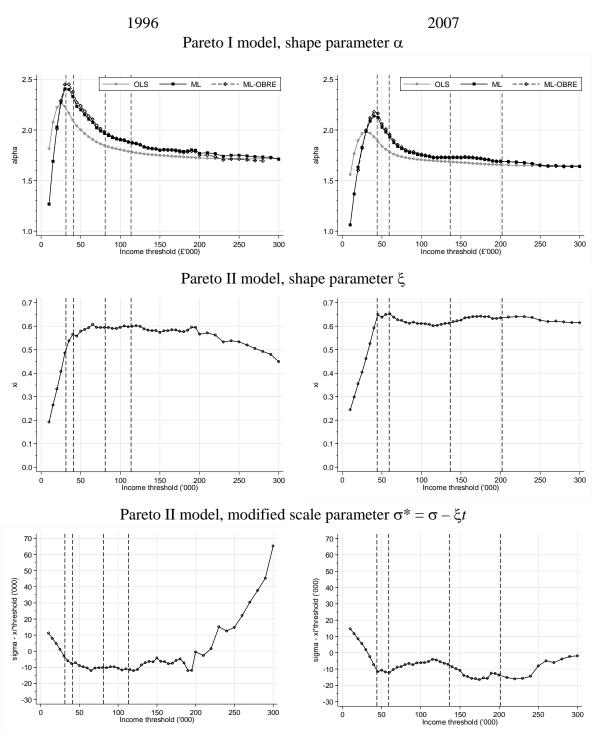
Notes. Author's estimates from SPI data. The figures plot twice the difference in log-likelihood for Pareto I and II models (each fitted using ML). Test statistics are capped at 100 for plotting purposes. Dotted horizontal lines show critical values of the $\chi^2(1)$ distribution at significance levels 0.05, 0.01, and 0.001. Vertical dashed lines show (from left to right) p90, p95, p99, p99.5. For plots for other years, see Appendix E.

Figure 6. PP plots for top incomes, by threshold: tax return data for 2007



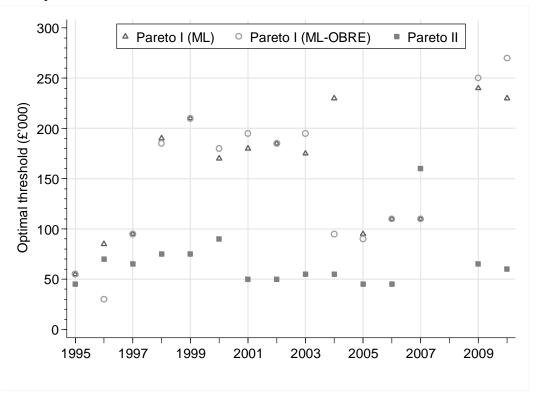
Notes. Author's estimates from SPI data. The charts plot modelled (cumulative) probabilities against empirical probabilities: see text. For plots for other years and thresholds, see the Appendix F. ML estimator used for both models.

Figure 7. Pareto I and II parameter estimates, by threshold, tax return data for 1996 and 2007



Notes. Author's estimates from SPI data. Vertical dashed lines show (from left to right) *p*90, *p*95, *p*99, *p*99.5. For plots for other years, see Appendix G.

Figure 8. Optimal Pareto threshold (KS criterion), tax return data, by estimator and year



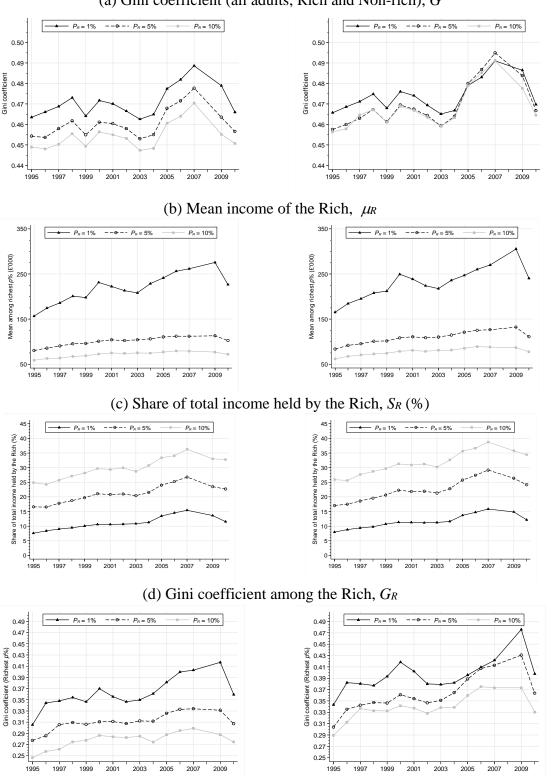
Notes. Author's estimates from SPI data. The figure plots the thresholds selected using the Kolmogorov-Smirnov criterion described in eq. (3) and main text.

Figure 9. Combined data estimates (Approach C): Gini coefficient overall, mean income, income share, and Gini coefficient of the Rich, by Pareto model and high-income threshold

Pareto I estimates

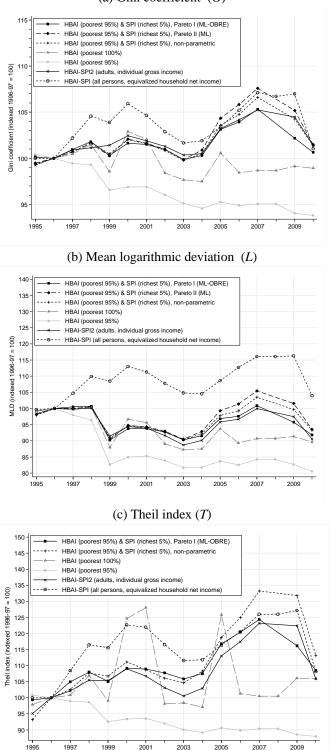
Pareto II estimates

(a) Gini coefficient (all adults, Rich and Non-rich), G



Notes. Author's derivations from SPI and HBAI data using eqn. (5). Pareto I (ML-OBRE) and II models fitted using each of three thresholds to define the Rich group: $P_R = 1\%$, 5%, and 10% (cut-offs derived from survey data – see text for further explanation). All series refer to distributions of individual gross income among adults. Estimates of μ_R , μ_N , S_R , S_N , G_R , and G_N are listed in Appendix H.

Figure 10. UK inequality (indexed 1996 = 100), by series and inequality index (a) Gini coefficient (G)



Notes. Author's derivations from SPI, HBAI, HBAI-SPI (Department for Work and Pensions 2015), and HBAI-SPI2 data (Burkhauser et al. 2016). All series shown are based on the distribution of individual gross income among adults, with the exception of the HBAI-SPI series which refers to equivalized household net income among all individuals (see main text). There are no Pareto II estimates for the Theil index. Threshold: p95 in the HBAI data (see main text). The corresponding graphs for the other two percentile thresholds are shown in Appendix I.

Online Supplementary Material (Appendices)

to accompany

Pareto models, top incomes, and recent trends in UK income inequality

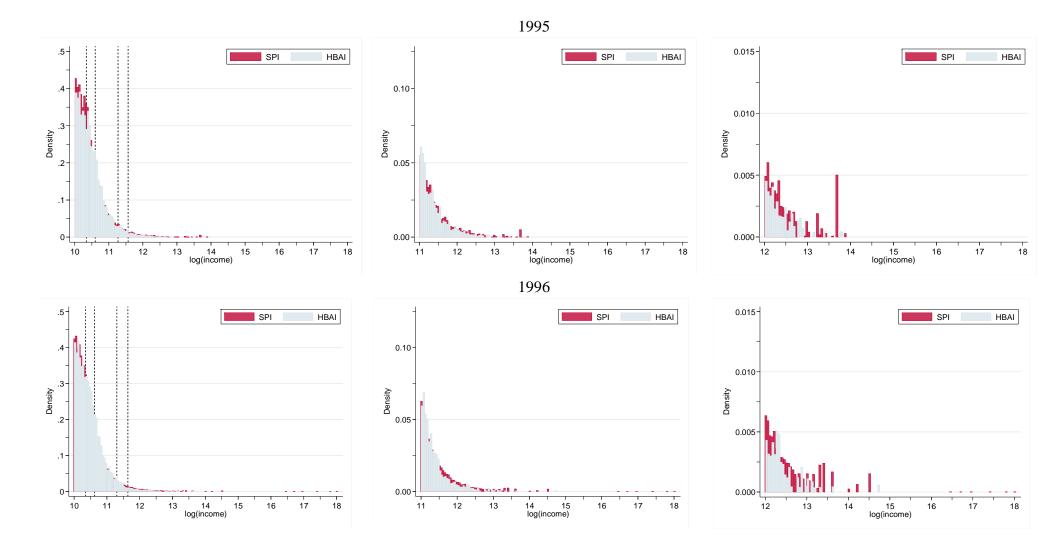
Stephen P. Jenkins (LSE, ISER (University of Essex), and IZA)

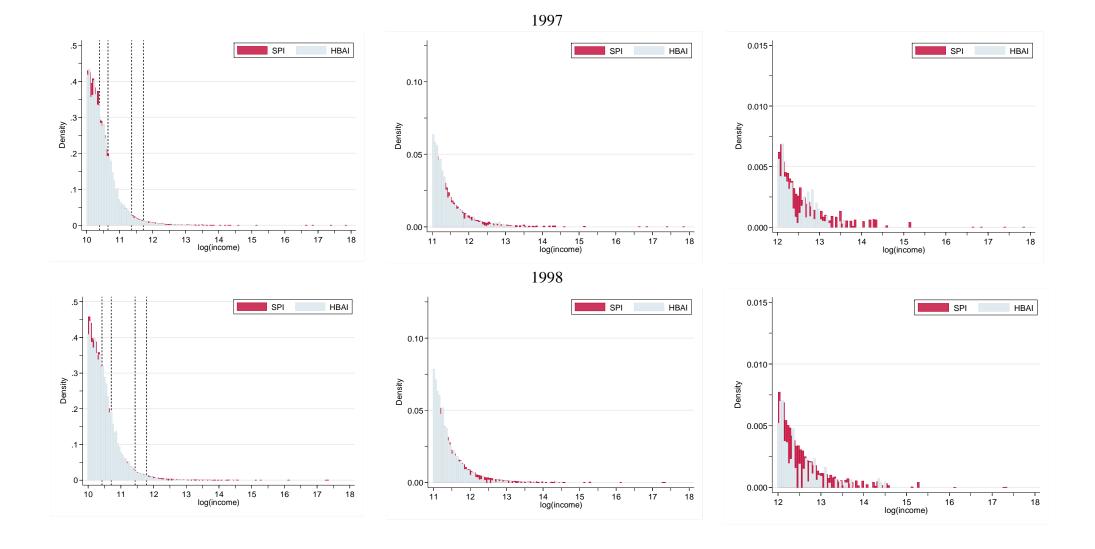
Appendices:

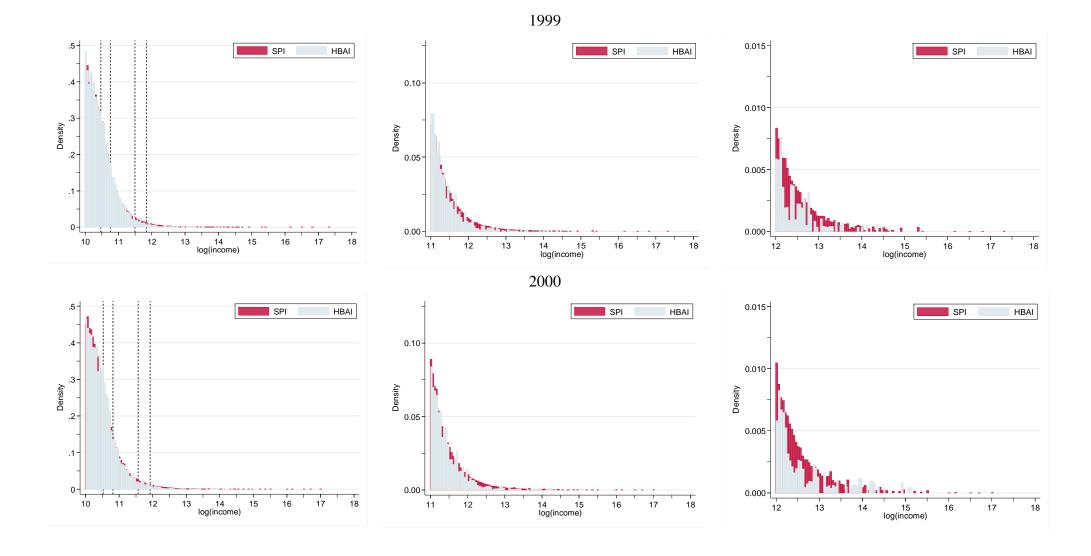
- A. The concentration of incomes at high and extremely high incomes: survey and tax data
- B. Three OLS regression methods for estimating the Pareto I model
- C. Zipf plots, by year
- D. Mean excess plots, by year
- E. Zenga plots, by year
- F. Likelihood ratio tests, Pareto I versus Pareto II model, by year and threshold
- G. Probability (PP) plots, by year and threshold
- H. Estimated parameters of Pareto I and Pareto II models, by year and three thresholds
- I. Combined data estimates of inequality, plus accompanying statistics, by year and three thresholds

The concentration of income in high and extremely high income ranges: survey and tax return data, by year

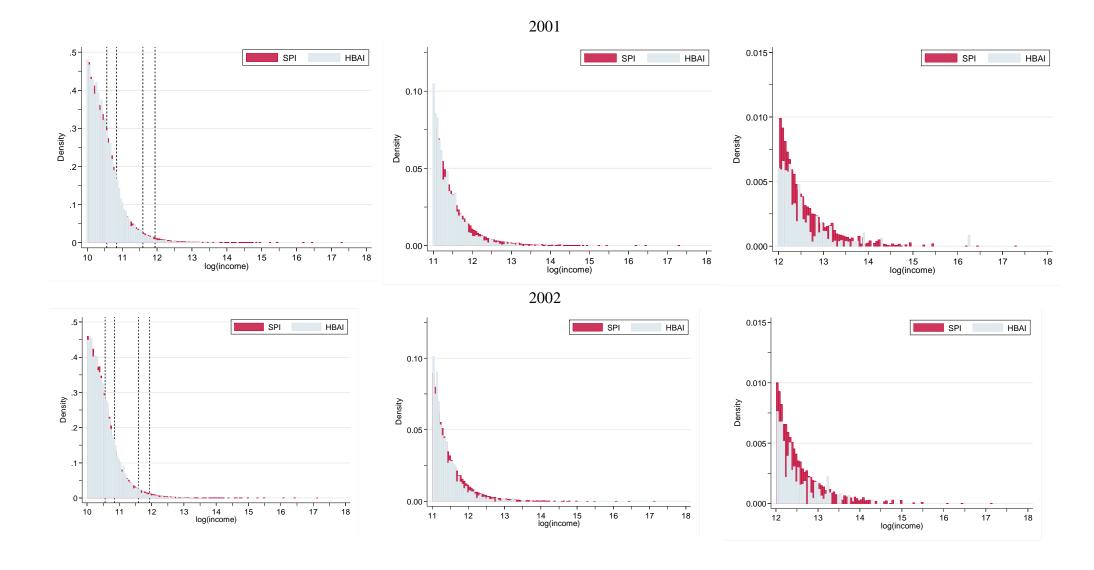
Vertical dashed lines show (from left to right) p90, p95, p99, p99.5. Income is in £ per year (2012/13 prices)



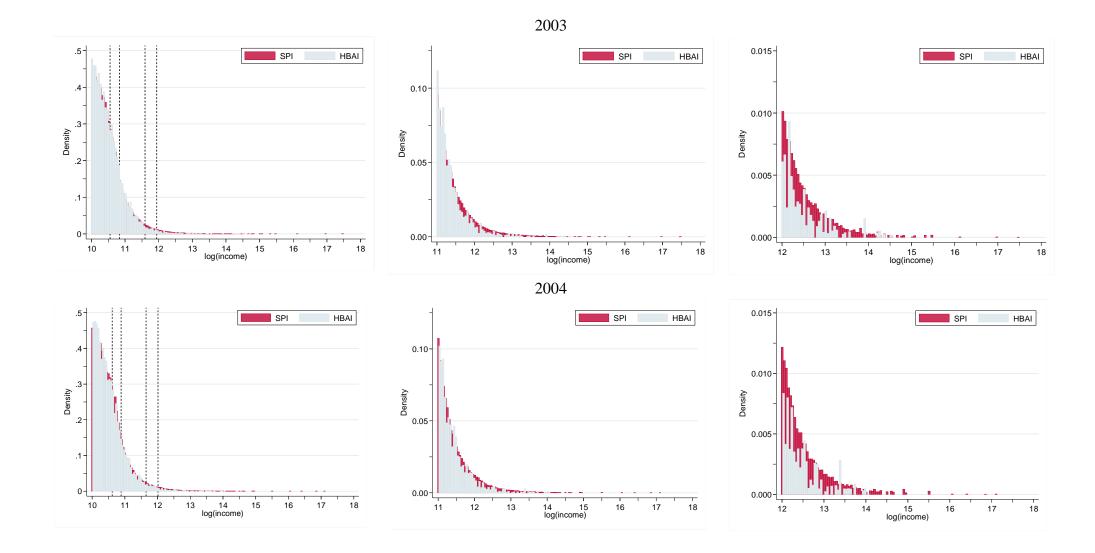


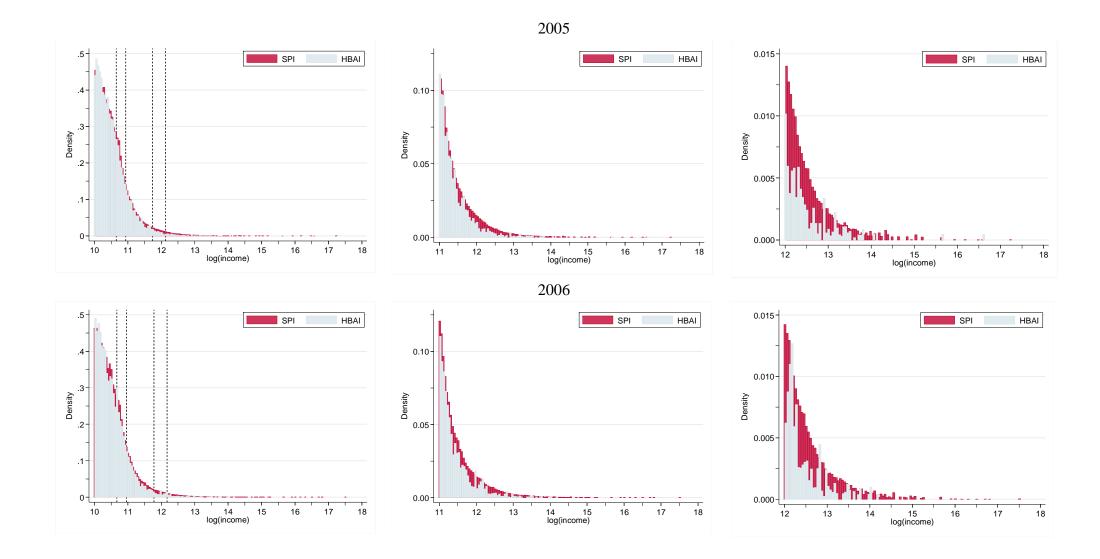


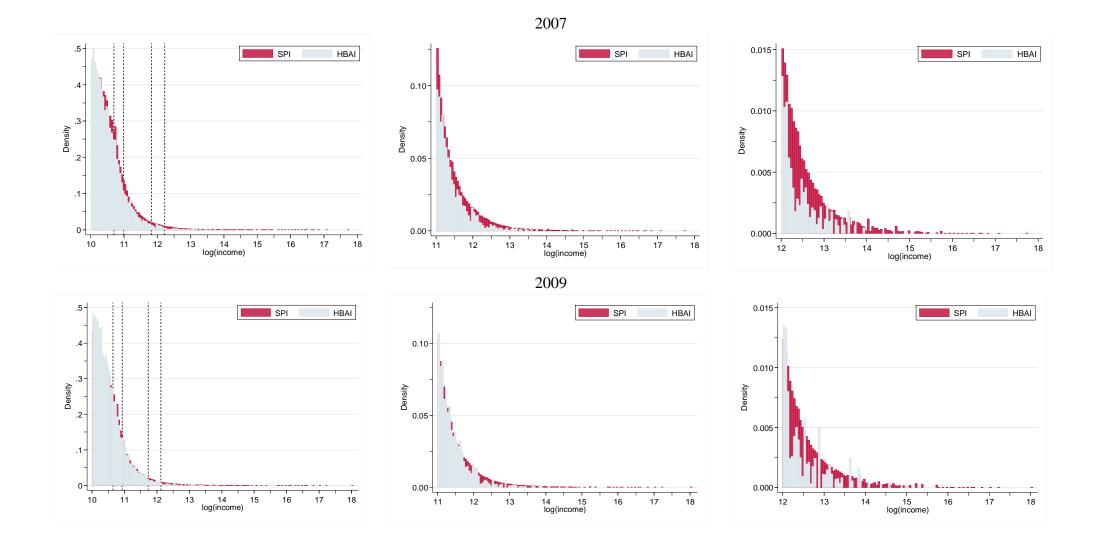
Appendix A-3

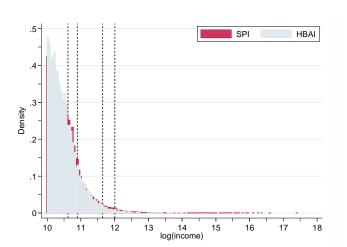


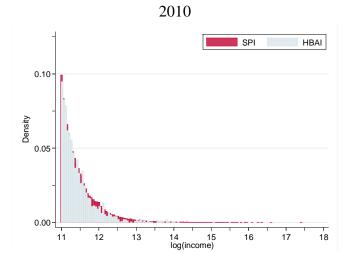
Appendix A-4

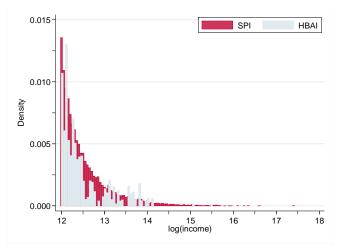












Atkinson (2016) explains that the Pareto shape parameter α may be estimated by OLS in three ways, depending on the information available:

- 1. the income range (e.g. above some specific income, x)
- 2. the fraction of income units with incomes greater than or equal to some value, the survivor function S(x)
- 3. The total income received by these income units, divided by the total population, $\Omega(x)$

With control totals for population and income available (as in this paper), Atkinson remarks that $\Omega(x)$ divided by the mean is the income share of those units with incomes of x or greater.

The first OLS estimation method is the 'Zipf' curve regression employed in the main text of this paper, in which $\log[S(x)]$ is regressed on $\log(x)$ using all income units with x > threshold t. For estimated slope coefficient β_1 , the estimate of α is $-\beta_1$.

The second OLS estimation method, which Atkinson (2016) attributes to Champernowne, is a regression of $\log[\Omega(x)]$ on $\log(x)$ using all income units with x > threshold t. For estimated slope coefficient β_2 , the estimate of α is $1-\beta_2$.

The third OLS estimation method, which Atkinson (2016) attributes to McGregor (1936) and Frechet (1945), is a regression of $\log[\Omega(x)]$ on $\log[S(x)]$ using all income units with x > threshold t. For estimated slope coefficient β_3 , the estimate of α is $1/(1-\beta_3)$.

Atkinson (2016) states that "the differences [in estimates of alpha] would not arise if the Pareto distribution provided a fully satisfactory representation of the data ... [t]he differences between the results from the three methods provide therefore a simple diagnostic device".

In the remainder of this appendix, I present for each year, the three estimates derived for each of a large number of income thresholds t. At the end, I report the estimates in numerical rather than graphical form, together with the R^2 from the corresponding regression.

Overall, the results confirm Atkinson's conclusions, based on estimates from UK SPI data in grouped form, covering 1918/19 to 2012/13 (using a threshold of around the 95th percentile in each year), that the three estimates are not always in close agreement with each other.

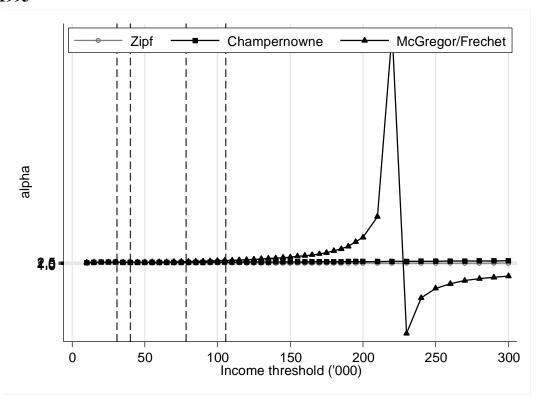
At relatively low thresholds (but disregarding extremely low ones), the Zipf method provides the highest estimates of α and the McGregor/Frechet method the lowest. Estimates converge as the threshold is increased to between around the 95th and 99th percentile, and then diverge again thereafter. That is, there is a 'cross over' with the Zipf method providing the lowest estimates and the McGregor/Frechet method the highest estimates as the threshold increases.

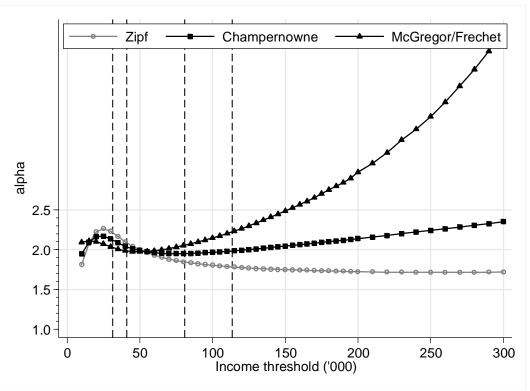
The Zipf estimates of the Pareto α are closer to the Maximum Likelihood estimates than the estimates from the other two OLS methods (see Figure 7 and Appendix F).

The Champernowne method consistently yields the smallest R^2 . The Zipf method provides the largest R^2 at most thresholds, but the McGregor/Frechet method tends to provide the highest R^2 at relatively low thresholds. But there are some exceptions to these patterns across the different years.

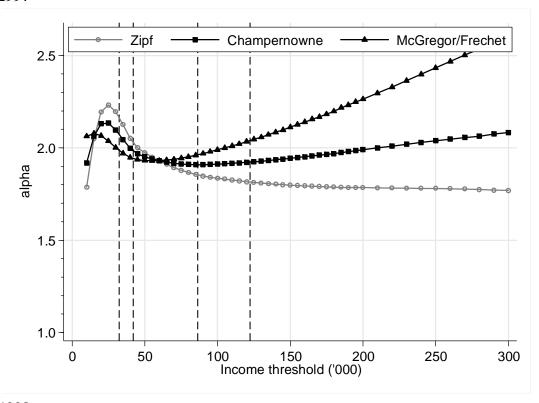
The vertical dashed lines show, from left to right, p90, p95, p99, p99.5 for each year.

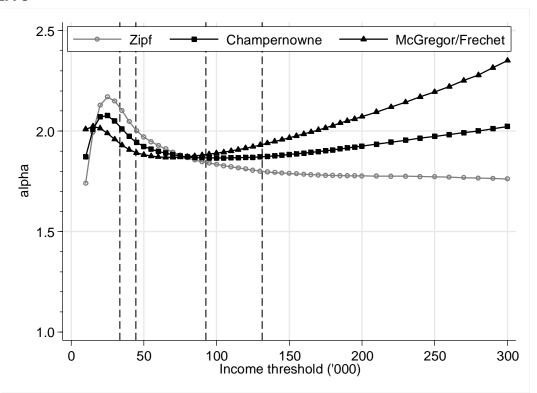
1995



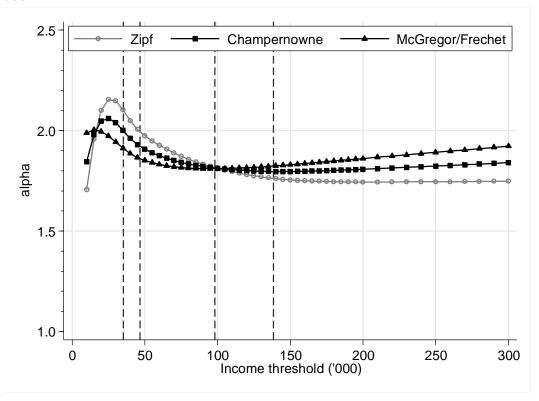


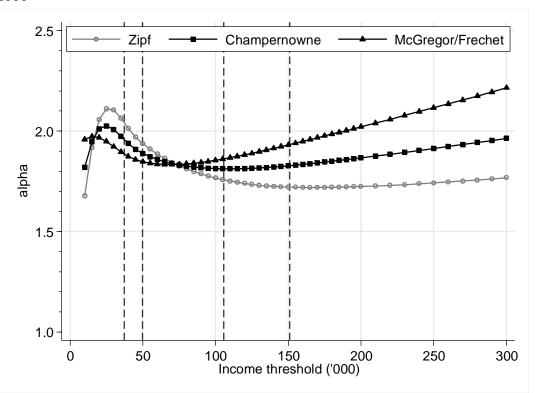
1997



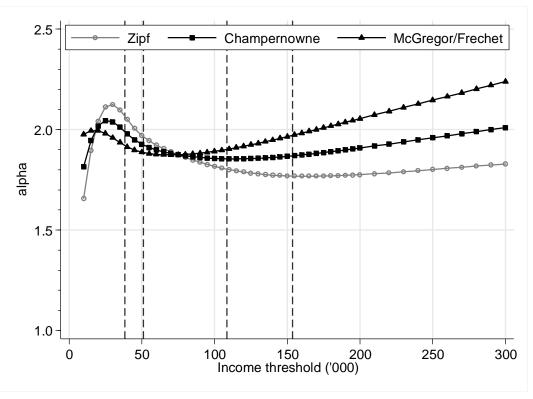


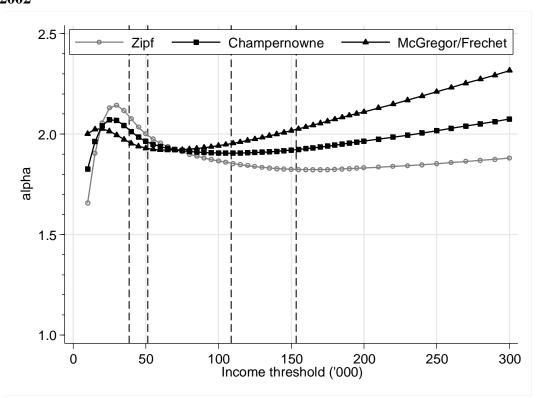
1999



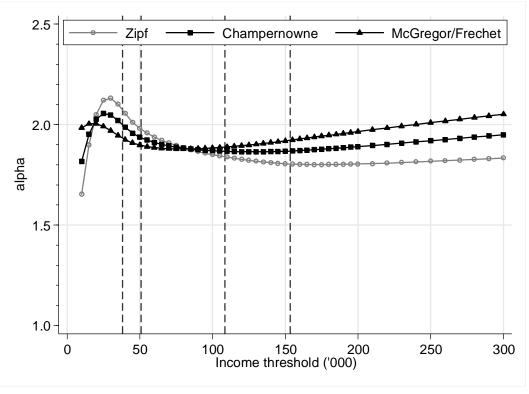


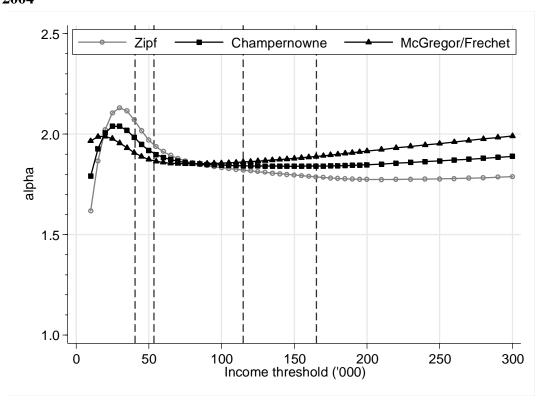
2001



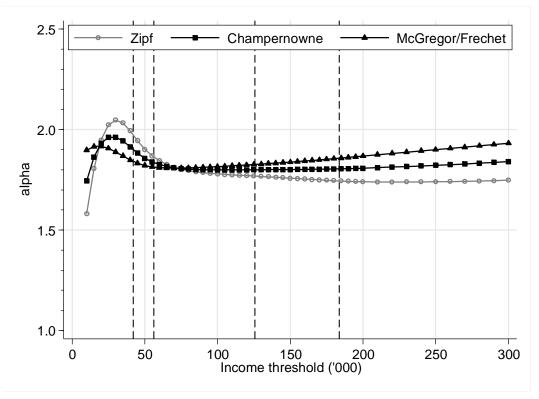


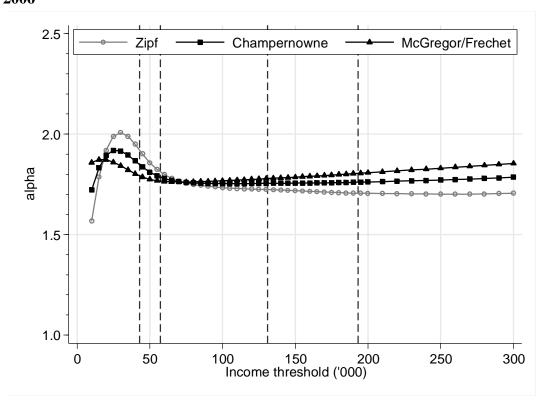
2003



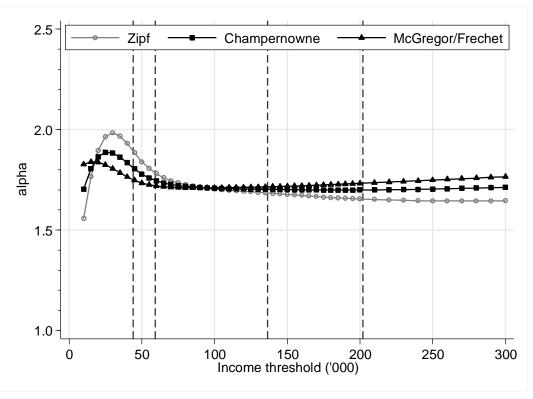


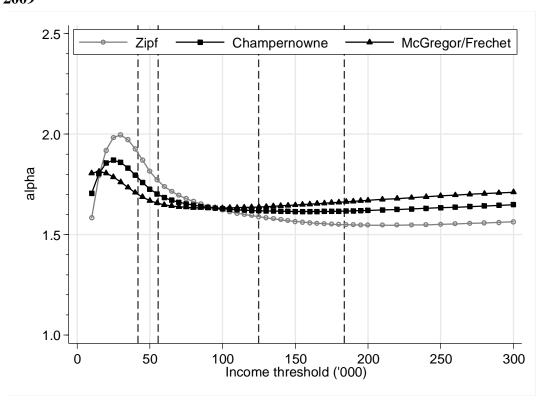
2005



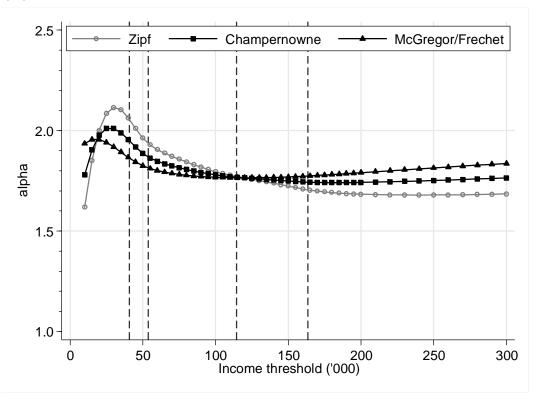


2007





$\textbf{Estimates of Pareto I alpha: Zipf, Champernowne, McGregor/Frechet OLS regressions} \ (pareto 02) \\$



Estimates of α are listed below for each model, together with the \mbox{R}^2 from the regression Kev:

Zipf: "ols", Champernowne "ols2", McGregor/Frechet (ols3"

list year threshold alpha_ols alpha_ols2 alpha_ols3 r2_ols r2_ols2 r2_ols3, noobs sepby(year)

+							+
year	thresh~d	alpha_~s	alpha_~2	alpha_o~3	r2_ols	r2_ols2	r2_ols3
1995	10000	1.842078	2.016769	2.246252	.954354	.9433437	.9974367
1995	15000	2.146887	2.206385	2.283974	.985137	.98283	.9973323
1995	20000	2.318627	2.307382	2.291517	.9945325	.9929944	.9963069
1995	25000	2.378236	2.33533	2.278956	.9945367	.9917693	.9946872
!		2.346169	2.33533				
1995	30000			2.261108	.9929382	.9893767	.9923073
1995	35000	2.273248	2.266073	2.252713	.9929606	.988107	.9884446
1995	40000	2.204729	2.232077	2.261793	.993497	.985855	.9834747
1995	45000	2.156929	2.215601	2.286677	.9930517	.9816053	.9777972
1995	50000	2.124672	2.21011	2.319169	.9920871	.9767706	.9723192
1995	55000	2.10006	2.211349	2.360072	.9907016	.9714163	.9666806
1995	60000	2.0795	2.214756	2.403405	.9893155	.9663018	.9615814
1995	65000	2.059019	2.220057	2.455541	.9877642	.9607713	.9563669
1995	70000	2.040164	2.226691	2.512949	.9861513	.9553099	.951515
1995	75000	2.021583	2.233775	2.576258	.9845361	.949882	.9470292
1995	80000	2.000748	2.243257	2.659736	.9825583	.9435759	.9422311
1995	85000	1.985999	2.255581	2.746111	.9803591	.9380925	.9382416
1995	90000	1.972787	2.269228	2.84174	.9779752	.9328467	.9346814
1995	95000	1.96176	2.285009	2.949055	.9753132	.9278992	.9314993
1995	100000	1.952426	2.304247	3.078094	.972155	.9230276	.9285116
1995	105000	1.947538	2.324104	3.204714	.9690783	.9193286	.9262096
1995	110000	1.942958	2.339779	3.31681	.9664783	.916361	.9245554
1995	115000	1.93626	2.355845	3.45241	.9635407	.9129741	.9229738
1995	120000	1.92737	2.378127	3.660814	.9593113	.9085647	.9212145
1995	125000	1.923476	2.396996	3.834484	.955913	.9058152	.9201415
1995	130000	1.920428	2.42228	4.078705	.9514323	.9028688	.9190864
1995	135000	1.918802	2.443502	4.301288	.9476274	.9007592	.9184157
1995	140000	1.916484	2.462059	4.527122	.9440398	.8987644	.917929
1995	145000	1.913456	2.479303	4.770984	.9404566	.8967519	.9175695
1995	150000	1.909016	2.49701	5.070746	.9364451	.8944161	.9173107
1995	155000	1.904242	2.517485	5.465396	.9316779	.8918646	.9171728
1995	160000	1.900676	2.532568	5.801149	.9280174	.8899867	.9171491
1995	165000	1.894508	2.550088	6.297121	.92327	.8873368	.9172409
1995	170000	1.889225	2.564844	6.793129	.9190938	.885074	.9173973
1995	175000	1.882667	2.580251	7.443322	.9143768	.8824441	.9176563
1995	180000	1.874641	2.599339	8.453877	.9083003	.8791955	.9181103
1995	185000	1.869161	2.615272	9.477061	.9032506	.8767505	.9185395
1995	190000	1.862776	2.631124	10.85853	.8978189	.874043	.9190489
1995	195000	1.854774	2.649967	13.21169	.8910083	.8707019	.9197904
1995	200000	1.849046	2.663234	15.63433	.8859451	.8682213	.9203165
1995	210000	1.836531	2.693352	26.78219	.8738763	.8624935	.9215789
1995	220000	1.822622	2.72569	126.1193	.8596005	.8557858	.9230181
1995	230000	1.810687	2.77028	-35.91547	.8405885	.8480669	.9248375
1995	240000	1.807609	2.818608	-16.87738	.8217947	.8418055	.9260812
1995	250000	1.807158	2.86157	-11.748	.8045915	.8361614	.9266669
1995	260000	1.808551	2.901755	-9.299731	.7882563	.8308823	.9268131
1995	270000	1.811598	2.94893	-7.567878	.7682695	.8241833	.9263741
1995	280000	1.819195	2.998701	-6.493437	.7482621	.8177645	.9252896
1995	290000	1.827019	3.040745	-5.858939	.7310248	.8119905	.9238468
1995	300000	1.849434	3.121548	-5.110957	.7017434	.803059	.9205881
1995	400000	2.559833	4.256126	-4.251876	.5917667	.8219123	.8782439
1995	500000	3.454192	5.501071	-5.190177	.566201	.8744838	.8410628
1995	600000	4.337626	6.252917	-37.06926	.4602654	.7973911	.7744112
1996	10000	1.81429	1.945506	2.093523	.9616552	.9555989	.9982563
1996	15000	2.077037	2.093235	2.110409	.9875807	.9862447	.9979427
1996	20000	2.223107	2.164287	2.100091	.9948734	.9916192	.9971456
1996	25000	2.264165	2.169915	2.07158	.9941064	.9882629	.9963065
1996	30000	2.231411	2.134916	2.037096	.992304	.9857166	.9953011
1996	35000	2.165521	2.086303	2.006542	.9922144	.9859854	.9937001
1996	40000	2.096596	2.042281	1.98627	.9933559	.9870256	.9912836
1996	45000	2.040947	2.010458	1.97647	.9942189	.9865514	.9881023
1996	50000	2.000719	1.990164	1.974491	.9947044	.9849535	.9847485
1996	55000	1.963965	1.974224	1.978018	.9953182	.982697	.9809366
1996	60000	1.931504	1.962476	1.986291	.9959918	.9798691	.976895
1996	65000	1.904748	1.954949	1.998113	.9965536	.9766212	.9728811
1996	70000	1.880896	1.950614	2.014357	.9969999	.9727163	.9685473
1996	75000	1.862713	1.949577	2.032323	.9972423	.9688041	.9645226
1996	80000	1.847404	1.95055	2.0523	.9973999	.9648387	.9606302
1 2000	55500	1.01/101	1.75055	2.0323			.5000502

	1996	85000	1.834515	1.953111	2.073861	.9974834	.9609147	.9569112	
i	1996	90000	1.823058	1.956935	2.097513	.9975243	.9569651	.9532771	
- 1									
	1996	95000	1.813348	1.961687	2.122062	.9975206	.9531985	.9498914	
	1996	100000	1.804499	1.966872	2.147498	.9975116	.9495777	.9467303	
i	1996	105000	1.796268	1.972444	2.174057	.9974996	.9460649	.9437523	
	1996	110000	1.788285	1.97891	2.203714	.9974713	.9424549	.9407709	
	1996	115000	1.781293	1.985623	2.233646	.9974248	.9390988	.938065	
ď	1996	120000	1.774792	1.992651	2.264848	.9973693	.9358652	.9355292	
. !									
	1996	125000	1.768552	2.00026	2.298571	.9973001	.9326446	.9330723	
	1996	130000	1.762821	2.008921	2.335943	.9971946	.9294202	.9306486	
i	1996	135000	1.758688	2.017888	2.372544	.9970461	.9266339	.9285275	
	1996	140000	1.755244	2.026994	2.40953	.9968809	.9240832	.9265963	
	1996	145000	1.752088	2.03592	2.446649	.9967137	.9217175	.9248469	
i	1996	150000	1.749015	2.0458	2.488326	.9965196	.9192923	.9230802	
١.									
Į	1996	155000	1.746433	2.054366	2.525625	.996347	.9172758	.921654	
	1996	160000	1.743509	2.063469	2.567209	.9961631	.9151479	.9202179	
i	1996	165000	1.740634	2.072211	2.608878	.9959848	.9131435	.9189241	
H									
_ !	1996	170000	1.737674	2.081475	2.654549	.9957916	.9111049	.9176594	
	1996	175000	1.735071	2.091299	2.703362	.9955744	.9091396	.9164504	
i	1996	180000	1.732879	2.101052	2.752567	.9953493	.907349	.9153638	
ď	1996	185000	1.730712	2.109697	2.798681	.9951473	.905743	.9144503	
	1996	190000	1.728369	2.117583	2.843636	.9949645	.9042124	.9136478	
	1996	195000	1.72555	2.126752	2.898403	.9947494	.9024435	.9127756	
i	1996	200000	1.722844	2.139488	2.973583	.9944322	.9004123	.9117789	
	1996	210000	1.72051	2.158303	3.085213	.9939312	.8979182	.9105033	
ı	1996	220000	1.717272	2.178483	3.219058	.9933642	.8951585	.9092902	
i	1996	230000	1.716057	2.202332	3.379089	.9926716	.8927521	.9081592	
	1996	240000	1.715524	2.221139	3.514563	.9921007	.8910481	.907384	
	1996	250000	1.714673	2.241076	3.67276	.9914578	.889212	.906633	
i	1996	260000	1.713956	2.262305	3.856486	.9907393	.8873472	.90591	
i	1996	270000	1.714166	2.283944	4.055539	.9899917	.8857377	.9052448	
	1996	280000	1.715087	2.305349	4.266506	.9892387	.8843589	.9046262	
	1996	290000	1.716447	2.326716	4.494789	.9884673	.8831026	.9040179	
i	1996	300000	1.719188	2.352382	4.78819	.9875513	.8818973	.9032896	
- 1									
. !	1996	400000	1.76708	2.573726	9.102162	.9804314	.880906	.8975928	
	1996	500000	1.765861	2.708644	28.53136	.9730909	.8742464	.8935123	
	1996	600000	1.714929	2.759379	-35.63996	.9696519	.8574803	.8880096	
i								i	
ď	1997	10000	1.786295	1.918212	2.06288	.959937	.9542783	.9987873	
	1997	15000	2.050162	2.063387	2.077465	.9872045	.9860109	.9986351	
	1997	20000	2.194104	2.131001	2.065727	.9948101	.9913324	.9981908	
i	1997	25000	2.232445	2.13401	2.036737	.9940737	.9879766	.9979829	
i	1997	30000	2.195671	2.096457	2.001798	.9926053	.9863396	.9979782	
	1997	35000	2.12549	2.045128	1.969956	.9933661	.9885681	.9978544	
	1997	40000	2.051772	1.998189	1.948169	.9957748	.9923205	.9973354	
i	1997	45000	2.000439	1.967511	1.936513	.9970066	.9936016	.9964134	
H	1997		1.973794	1.952292		.9971637			
		50000			1.931746		.9931952	.9954668	
	1997	55000	1.949437	1.93976	1.930026	.9973688	.9925539	.9943662	
	1997	60000	1.929731	1.93068	1.930738	.9975187	.9916795	.9932338	
i	1997	65000	1.910344	1.922725	1.933494	.9977687	.9906583	.9919956	
H			1.892629					.9906477	
. !	1997	70000		1.916516	1.938299	.9980006	.9893672		
	1997	75000	1.878702	1.912654	1.944316	.9981321	.9879341	.9893379	
	1997	80000	1.866297	1.910118	1.951733	.9982238	.9863183	.987973	
i	1997	85000	1.855658	1.908918	1.960342	.998262	.9845616	.9865811	
	1997	90000	1.847324	1.908947	1.96933	.998242	.9828181	.9852636	
	1997	95000	1.840432	1.910289	1.979779	.9981544	.9809021	.983858	
	1997	100000	1.835379	1.91208	1.989371	.9980498	.9792089	.982643	
i	1997	105000	1.830468	1.914192	1.999705	.9979364	.9774411	.9814065	
ŀ			1.825722	1.916397			.9756891		
. !	1997	110000			2.010266	.9978274		.9802179	
	1997	115000	1.820888	1.918698	2.021377	.9977215	.9738909	.9790372	
	1997	120000	1.816059	1.921495	2.033876	.997597	.9719415	.9777921	
i	1997	125000	1.812257	1.924684	2.046252	.9974515	.9700973	.9766314	
ď									
. !	1997	130000	1.809004	1.927797	2.057967	.9973096	.9684052	.975591	
	1997	135000	1.805931	1.931694	2.071572	.9971316	.966535	.9744589	
ı	1997	140000	1.803128	1.935322	2.084403	.9969636	.9648082	.973443	
i	1997	145000	1.800518	1.938991	2.0973	.9967923	.9631234	.9724765	
ŀ	1997	150000							
			1.798117	1.943423	2.112086	.996586	.9612961	.9714453	
	1997	155000	1.796032	1.947538	2.125854	.9963895	.9596322	.9705278	
ĺ	1997	160000	1.79409	1.951646	2.139632	.9961905	.9580173	.9696603	
i	1997	165000	1.792339	1.956443	2.155206	.9959576	.9562766	.9687378	
. !				1.9605					
		170000		1.4005	2.168451	.9957565	.9548362	.9679927	
Į	1997	170000	1.790955						
		170000 175000	1.790955	1.964561	2.182649	.995548	.9532964	.9672377	
	1997				2.182649 2.198107	.995548 .9953232	.9532964 .9516575	.9672377 .9664671	
	1997 1997 1997	175000 180000	1.789128 1.78709	1.964561 1.968853	2.198107	.9953232	.9516575	.9664671	
	1997 1997 1997 1997	175000 180000 185000	1.789128 1.78709 1.785888	1.964561 1.968853 1.97499	2.198107 2.217706	.9953232 .9950176	.9516575 .949805	.9664671 .9655818	
	1997 1997 1997 1997 1997	175000 180000 185000 190000	1.789128 1.78709 1.785888 1.785239	1.964561 1.968853 1.97499 1.979578	2.198107 2.217706 2.232192	.9953232 .9950176 .9947836	.9516575 .949805 .9484715	.9664671 .9655818 .964947	
	1997 1997 1997 1997	175000 180000 185000	1.789128 1.78709 1.785888	1.964561 1.968853 1.97499	2.198107 2.217706	.9953232 .9950176	.9516575 .949805	.9664671 .9655818	
	1997 1997 1997 1997 1997	175000 180000 185000 190000	1.789128 1.78709 1.785888 1.785239	1.964561 1.968853 1.97499 1.979578	2.198107 2.217706 2.232192	.9953232 .9950176 .9947836	.9516575 .949805 .9484715	.9664671 .9655818 .964947	

$\textbf{Estimates of Pareto I alpha: Zipf, Champernowne, McGregor/Frechet OLS regressions} \ (pareto 02) \\$

l 19	97	210000	1.783424	1.999832	2.296747	.9937134	.9430019	.9624785
19	97	220000	1.782407	2.009364	2.328928	.9931694	.9404511	.9614388
19	97	230000	1.781539	2.019437	2.363606	.9925753	.9378604	.9604451
			1.780894			.9919652		:
	97	240000		2.029444	2.398724		.9353839	.9595506
19	97	250000	1.780024	2.038939	2.433724	.9913522	.9329911	.9587585
j 19	97	260000	1.779006	2.047717	2.467619	.9907556	.9307427	.9580774
19	97	270000	1.777123	2.055949	2.50275	.990146	.9283893	.9574549
19	97	280000	1.774373	2.062717	2.535715	.9896004	.9261285	.9569437
i 19	97	290000	1.770786	2.074821	2.593598	.9886432	.9226339	.9563161
1 19	97	300000	1.769647	2.083373	2.632323	.9879605	.9204715	.9559202
19	97	400000	1.798681	2.208663	3.156063	.9791327	.9031504	.953341
i 10	97	500000	1.873444	2.355122	3.75624	.9724935	.8999645	.9523372
!								
İTA	97	600000	1.952106	2.481714	4.288064	.969758	.9036796	.9510152
İ 19	98	10000	1.740285	1.871952	2.008976	.9612613	.9546931	.9979084
1 19	98	15000	1.994609	2.008951	2.023253	.9886332	.986528	.9975042
19	98	20000	2.12852	2.071123	2.014035	.9962683	.9918702	.9966143
i 19	98	25000	2.169295	2.077244	1.989493	.9962393	.9888123	.9956346
•								
	98	30000	2.149392	2.050374	1.959128	.9950801	.9860157	.9944821
19	98	35000	2.101925	2.011497	1.930047	.9949651	.9851372	.9928152
İ 19	98	40000	2.047515	1.9736	1.907589	.9960595	.9854215	.9904645
•	98	45000	2.001765	1.943699	1.891756	.9970641	.9845603	.98728
19	98	50000	1.970188	1.923701	1.881744	.9975156	.9822623	.983613
19	98	55000	1.947057	1.909743	1.875504	.9977293	.9792486	.9796715
•	98	60000	1.928408	1.899233	1.871721	.9978603	.9757962	.9754751
19	98	65000	1.911614	1.890583	1.869762	.9980199	.9720808	.9710529
19	98	70000	1.894674	1.882698	1.869358	.9983069	.9681183	.9663208
	98	75000	1.879618	1.876493	1.870467	.9985217	.963412	.9609518
•								
19	98	80000	1.867038	1.872016	1.872733	.998693	.9585774	.9555731
19	98	85000	1.856203	1.868894	1.876077	.9988139	.9533549	.949884
i 19	98	90000	1.847486	1.867146	1.88021	.9988736	.9479766	.9441162
	98	95000	1.840276	1.866438	1.885039	.998892	.9424205	.9382128
19	98	100000	1.834451	1.86632	1.889849	.9988978	.9373405	.9328451
19	98	105000	1.827986	1.866215	1.895361	.998936	.9319494	.9271754
	98	110000	1.822038	1.866696	1.901615	.9989583	.926259	.9212191
	98	115000	1.816535	1.867414	1.908032	.9989849	.9207605	.9154899
19	98	120000	1.810913	1.868339	1.91509	.9990238	.915049	.9095674
İ 19	98	125000	1.805568	1.869635	1.922743	.9990599	.9092029	.9035291
	98	130000	1.800794	1.87146	1.931012	.9990782	.9032157	.8973567
•								
19	98	135000	1.796715	1.874018	1.940175	.9990707	.8969518	.8908939
19	98	140000	1.79388	1.876761	1.948567	.999044	.8914643	.8852156
•	98	145000	1.791444	1.880032	1.957721	.9990038	.8857344	.8792703
19	98	150000	1.789213	1.883284	1.966743	.9989639	.8803006	.8736377
19	98	155000	1.787018	1.886573	1.975925	.9989249	.8749656	.8681177
İ 19	98	160000	1.785021	1.890361	1.986048	.9988759	.8693267	.8622695
	98	165000	1.78349	1.8942	1.995883	.9988223	.8640693	.8567977
19	98	170000	1.781989	1.897994	2.005707	.9987698	.858999	.8515267
İ 19	98	175000	1.78053	1.902024	2.016114	.9987134	.8538242	.8461452
•	98							:
		180000	1.779065	1.906285	2.027168	.9986535	.8485323	.8406432
19	98	185000	1.778154	1.911787	2.040425	.9985729	.8425224	.8343227
19	98	190000	1.778045	1.916302	2.050622	.9985064	.8381172	.8296281
	98	195000	1.777605	1.920648	2.060965	.9984403	.8337567	.8250136
	98	200000	1.7772	1.925356	2.072194	.998368	.8291866	.8201677
19	98	210000	1.776274	1.934688	2.094996	.9982226	.8203855	.8108408
	98	220000	1.775533	1.944837	2.119996	.9980616	.8114258	.8013058
					2.144122			.7927346
	98	230000	1.774985	1.954499		.9979058	.8034028	:
19	98	240000	1.773962	1.964562	2.170536	.9977385	.7951902	.7840034
19	98	250000	1.772835	1.973494	2.194901	.9975876	.7881172	.7765042
	98	260000	1.770936	1.982383	2.221038	.9974385	.780962	.7690136
	98	270000	1.76847	1.992194	2.251362	.9972762	.7732392	.7609839
19	98	280000	1.766142	2.000813	2.27909	.9971353	.7666835	.7542007
j 19	98	290000	1.76386	2.012285	2.315669	.9969389	.7588642	.7460339
	98	300000	1.761857	2.023201	2.351351	.9967488	.7518818	.7387279
	98	400000	1.75315	2.144211	2.798252	.994455	.6997433	.6821928
19	98	500000	1.750763	2.26615	3.425282	.9918205	.6710307	.6485234
	98	600000	1.74519	2.39821	4.541643	.9885294	.6521078	.6249622
i								
		10000	1 705001	1 045355	1 00000	050555	0501100	000000
•	99	10000	1.705801	1.845357	1.987897	.9585576	.9521103	.9987963
19	99	15000	1.956411	1.979742	2.002954	.9864486	.9853048	.998741
•	99	20000	2.099462	2.046924	1.995654	.9954987	.9926549	.9983452
	99	25000	2.153924	2.060394	1.973018	.9962698	.9906601	.9981551
19	99	30000	2.147776	2.039991	1.943159	.9950001	.9881202	.9982793
19	99	35000	2.103029	2.001144	1.912263	.9948021	.9886618	.9985873
	99	40000	2.049397	1.96135	1.886013	.9957091	.9910497	.9988685
:								
	99	45000	2.005408	1.929613	1.865652	.9963911	.9928622	.999046
19	99	50000	1.974258	1.907298	1.851312	.9966911	.9938634	.9991381
	99	55000	1.948253	1.88928	1.840245	.9969206	.9946316	.9991748
, -,		22300						

$\textbf{Estimates of Pareto I alpha: Zipf, Champernowne, McGregor/Frechet OLS regressions} \ (pareto 02) \\$

1999	60000	1.92695	1.874849	1.831653	.9970417	.9951355	.9991675	1
•								1
1999	65000	1.907622	1.862568	1.825187	.997247	.9956623	.9991254	į
1999	70000	1.888512	1.851082	1.819884	.9975097	.9961863	.9990425	
1999	75000	1.871931	1.841612	1.816123	.9977659	.9966033	.9989327	1
1999	80000	1.85688	1.83339	1.813352	.9979829	.9968917	.9987915	i
•								1
1999	85000	1.844064	1.826717	1.811568	.9981546	.9970574	.9986346	ı
1999	90000	1.832731	1.82112	1.810539	.9983013	.9971389	.9984641	
1999	95000	1.822428	1.816318	1.81013	.9984449	.99717	.9982851	i
•								i
1999	100000	1.812464	1.811958	1.81027	.9986009	.9971645	.9980913	l
1999	105000	1.803759	1.808414	1.810893	.998722	.9970866	.9978925	
1999	110000	1.795909	1.805434	1.811879	.9988407	.9969819	.9976981	
1999	115000	1.788298	1.802763	1.813266	.9989625	.9968419	.9974945	i
•								l
1999	120000	1.781217	1.800516	1.815032	.9990724	.9966592	.9972855	l
1999	125000	1.775132	1.798822	1.817019	.999158	.9964465	.9970848	
1999	130000	1.769608	1.797535	1.81932	.9992242	.9961954	.9968796	ı
1999	135000	1.764881	1.796705	1.821824	.999267	.9959199	.9966781	i
•								1
1999	140000	1.760787	1.796214	1.824451	.9992953	.9956337	.9964835	l
1999	145000	1.757201	1.796077	1.827327	.9993068	.9953246	.9962855	
1999	150000	1.754475	1.796373	1.830288	.9992964	.9950135	.9960932	ı
1999	155000	1.752376	1.796901	1.833156	.9992763	.9947197	.9959152	i
•								l
1999	160000	1.750611	1.797651	1.836165	.9992484	.99442	.9957354	l
1999	165000	1.749055	1.798483	1.839164	.9992181	.9941263	.9955622	
1999	170000	1.747733	1.799371	1.842074	.9991863	.9938466	.9953993	1
1999	175000	1.746566	1.800371	1.845075	.999151	.9935638	.995236	i
•								į
1999	180000	1.74542	1.801439	1.848204	.9991135	.9932718	.9950704	l
1999	185000	1.744919	1.803014	1.851727	.9990637	.9929758	.994892	ı
j 1999	190000	1.744648	1.804426	1.854727	.9990192	.9927272	.99474	1
1999	195000	1.744264	1.805699	1.857578	.9989769	.9924858	.9945976	i
•								1
1999	200000	1.743785	1.807024	1.860631	.9989315	.9922251	.9944479	ı
1999	210000	1.743611	1.81034	1.867322	.9988264	.9916969	.9941279	
j 1999	220000	1.744204	1.813704	1.873393	.9987286	.9912605	.9938433	1
1999	230000	1.744746	1.816979	1.879363	.9986289	.9908315	.993567	i
•								-
1999	240000	1.745032	1.820126	1.88536	.9985243	.9903882	.9932941	ı
1999	250000	1.745152	1.823245	1.891501	.9984137	.9899272	.9930202	
1999	260000	1.745484	1.826557	1.897846	.9982964	.989467	.992743	i
1999	270000	1.745981	1.829671	1.903646	.9981869	.9890618	.9924936	i
•								
1999	280000	1.746533	1.833158	1.910171	.9980597	.9886079	.9922168	ı
1999	290000	1.747269	1.836639	1.916514	.9979337	.9881838	.9919511	
j 1999	300000	1.748643	1.840368	1.922696	.9978144	.9878236	.9916936	i
1999	400000				.9965674	.9847143	.9892269	i
•		1.763353	1.876436	1.981238				1
1999	500000	1.777488	1.90833	2.03118	.9952106	.9820508	.9866046	ı
1999	600000	1.784775	1.933446	2.074334	.9935476	.9786553	.983604	
i							i	ı
2000	10000	1.67751	1.818917	1.95906	.9571629	.9499953	.9981178	i
								1
2000	15000	1.918771	1.946296	1.972987	.9860769	.984103	.9979017	l
2000	20000	2.056582	2.011008	1.967734	.9952909	.9917002	.997224	
2000	25000	2.110395	2.025672	1.948395	.9961178	.9896054	.9965207	
2000	30000	2.105224	2.008204	1.922745	.9948288	.9865414	.9958338	i
								l
2000	35000	2.064232	1.973941	1.896413	.9944384	.9857336	.9949111	l
2000	40000	2.014381	1.938616	1.87458	.9950499	.9861133	.9935286	
2000	45000	1.970136	1.909316	1.858377	.9957205	.9858723	.9915951	
2000	50000	1.937803	1.888695	1.847753	.9960144	.9845966	.989366	i
								i
2000	55000	1.910318	1.872374	1.840739	.9963264	.9829484	.9868989	l
2000	60000	1.885899	1.858908	1.836303	.9966505	.9808804	.9841365	ı
2000	65000	1.863899	1.847724	1.83402	.997001	.9784414	.9811149	1
2000	70000	1.84404	1.838476	1.833556	.9973837	.9757084	.9779096	i
							:	i
2000	75000	1.826751	1.831194	1.834653	.9976681	.9724362	.9743902	1
2000	80000	1.812029	1.825671	1.836951	.9979024	.96896	.9708218	ı
2000	85000	1.799503	1.821527	1.840066	.9981065	.9654585	.9673375	
2000	90000	1.787206	1.817942	1.844183	.9983441	.9616466	.9636164	1
2000	95000				.9985344		:	i
		1.776474	1.815416	1.849083		.9576508	.9598218	l
2000	100000	1.766818	1.813736	1.854805	.9986919	.9534052	.955873	ı
2000	105000	1.758724	1.812934	1.860953	.9988019	.9491559	.951987	ı
2000	110000	1.75178	1.812744	1.86737	.9988844	.9449642	.9481999	1
2000	115000	1.745467	1.812955	1.874128	.9989573	.9407589	.9444373	i
							:	i
2000	120000	1.739294	1.813569	1.881736	.9990264	.9362348	.9404259	l
2000	125000	1.734424	1.814735	1.889308	.9990578	.9319166	.9366185	ı
2000	130000	1.730096	1.816457	1.897638	.9990669	.9273435	.9326003	1
2000	135000	1.726979	1.818689	1.905899	.9990441	.9229724	.9287537	i
•								1
2000	140000	1.724407	1.821365	1.914664	.9990053	.9184787	.9247962	l
2000		1.722622	1.824192	1.922994	.998956	.9143328	.9211341	ı
	145000				0000000	0101503	0154450	
•			1.82732	1.931587	.9988978	.9IUI/U3	.91/4458 I	١
2000	150000	1.72129	1.82732	1.931587	.9988978	.9101703	.9174458	1
2000 2000	150000 155000	1.72129 1.720168	1.83045	1.940042	.9988381	.9061626	.913897	
2000 2000 2000	150000 155000 160000	1.72129 1.720168 1.719452	1.83045 1.834041	1.940042 1.94917	.9988381 .9987684	.9061626 .9019524	.913897 .9101496	
2000 2000	150000 155000	1.72129 1.720168	1.83045	1.940042	.9988381	.9061626	.913897	
2000 2000 2000 2000	150000 155000 160000 165000	1.72129 1.720168 1.719452 1.719128	1.83045 1.834041 1.837711	1.940042 1.94917 1.958108	.9988381 .9987684 .9986972	.9061626 .9019524 .8979338	.913897 .9101496 .9065557	
2000 2000 2000	150000 155000 160000	1.72129 1.720168 1.719452	1.83045 1.834041	1.940042 1.94917	.9988381 .9987684	.9061626 .9019524	.913897 .9101496	

2000	180000	1.720664	1.850149	1.985696	.9984774	.8861722	.8958638
2000	185000	1.721442	1.854	1.993996	.9984123	.8827732	.8927475
2000	190000	1.722214	1.857994	2.002716	.9983429	.879254	.8895243
j 2000	195000	1.723285	1.862447	2.012239	.9982699	.8755004	.8860633
2000	200000	1.724537	1.866933	2.021675	.9982004	.8718628	.8826873
:			1.875334		.9980683		.8764455
2000	210000	1.726888		2.039532		.8651461	
2000	220000	1.729869	1.884258	2.058087	.9979434	.8584602	.870158
2000	230000	1.733462	1.893978	2.078074	.9978213	.8515589	.8635989
2000	240000	1.737748	1.903674	2.097217	.9977352	.8452837	.857502
2000	250000	1.742063	1.913313	2.11638	.9976563	.8392211	.8515707
2000	260000	1.746864	1.923241	2.135771	.9976012	.8333587	.8457372
2000	270000	1.751473	1.932723	2.154442	.9975559	.8279086	.8402742
2000	280000	1.756664	1.943066	2.17474	.9975245	.8222225	.8345023
					.9975067		
2000	290000	1.761846	1.953257	2.194823		.8168235	.8289643
2000	300000	1.768009	1.96432	2.215895	.9975388	.8114694	.8233083
2000	400000	1.805437	2.052252	2.414879	.9972819	.7676522	.7778927
2000	500000	1.830101	2.1337	2.646952	.99672	.7312257	.7401201
2000	600000	1.841039	2.225133	3.015376	.9955093	.6934617	.7026932
j							i
2001	10000	1.657559	1.815531	1.975865	.9550027	.9459922	.9981713
2001	15000	1.896344	1.945222	1.994246	.9842471	.9819884	.9981575
				1.994601			
2001	20000	2.041023	2.017665		.9945227	.9919522	.9975795
2001	25000	2.112527	2.044888	1.980567	.9966709	.9916348	.9968757
2001	30000	2.124597	2.03843	1.959095	.9958082	.9887911	.9961836
2001	35000	2.096822	2.012005	1.935774	.995109	.9873074	.9953422
2001	40000	2.05075	1.978423	1.914403	.9955282	.987402	.9940786
2001	45000	2.00586	1.948748	1.898553	.9964109	.9875493	.9923431
2001	50000	1.970776	1.926504	1.887695	.9969473	.9865752	.9901531
2001	55000	1.944695	1.910773	1.880996	.9972483	.9849361	.9877797
2001	60000	1.923036	1.898495		.9974554	.9828042	.9851406
				1.87683			
2001	65000	1.905063	1.888998	1.874642	.9975979	.9803479	.9823494
2001	70000	1.888932	1.881152	1.87396	.997743	.9776321	.9793787
2001	75000	1.874136	1.874578	1.874553	.9978957	.9746568	.9762205
2001	80000	1.860594	1.869134	1.876249	.9980547	.9714689	.9729219
2001	85000	1.848471	1.864798	1.878881	.9981975	.9680887	.9695172
2001	90000	1.837113	1.861216	1.882378	.9983494	.9645123	.9659799
2001	95000	1.826691	1.858381	1.886585	.9985012	.9608176	.9623891
2001	100000	1.816918	1.856204	1.891613	.9986459	.9568717	.9586199
2001	105000	1.808382	1.85485	1.89723	.998757	.9528185	.9548129
2001	110000	1.800737	1.854149	1.903431	.9988458	.9486338	.9509324
2001	115000	1.794301	1.854264	1.91023	.9988899	.9442922	.9469479
2001	120000	1.788961	1.854822	1.916953	.9989144	.9401833	.9432041
2001	125000	1.78372	1.855811	1.924614	.9989308	.9356893	.9391343
2001	130000	1.779757	1.857233	1.931958	.9989196	.9315371	.935385
2001	135000	1.776104	1.859105	1.940057	.9988939	.9271068	.931395
2001	140000	1.773301	1.861339	1.948119	.9988506	.9228374	.9275474
		1.771087		1.956292	.9987953		
2001	145000		1.863876			.918633	.9237539
2001	150000	1.769262	1.866847	1.965095	.9987269	.9142294	.9197733
2001	155000	1.768269	1.870273	1.974052	.998646	.9098884	.9158177
2001	160000	1.76795	1.873935	1.982832	.9985616	.9057523	.9120172
2001	165000	1.767969	1.877653	1.991413	.9984775	.9017996	.9083675
2001	170000	1.768194	1.881599	2.000347	.9983894	.8977692	.9046342
2001	175000	1.768714	1.885556	2.009013	.9983042	.893944	.901069
2001	180000	1.769729	1.890048	2.018383	.9982154	.8899128	.8972734
2001	185000	1.7709	1.894358	2.027184	.9981342	.8862038	.8937587
2001	190000	1.772323	1.898999	2.036515	.9980507	.8823497	.890085
2001	195000	1.773921	1.903532	2.04541	.9979758	.8787558	.88663
2001	200000	1.775608	1.908025	2.05414	.9979051	.8752924	.8832818
2001	210000	1.780153	1.918416	2.073618	.9977705	.8678344	.8759602
2001	220000	1.784479	1.927673	2.09076	.9976665	.8615006	.8696665
2001	230000	1.789915	1.938472	2.110378	.997572	.8545357	.8626387
2001	240000	1.795647	1.948722	2.128304	.9975258	.848465	.8563648
2001	250000	1.801494	1.959264	2.146945	.9974843	.8423361	.8499866
2001	260000	1.806998	1.969213	2.164681	.9974532	.8366842	.8440576
2001	270000	1.812335	1.979071	2.182559	.9974225	.8311452	.8382227
2001	280000	1.8182	1.98994	2.202439	.9973972	.8251958	.8319042
2001	290000	1.823843	2.000094	2.220877	.9973955	.819905	.8261985
2001	300000	1.828797	2.009585	2.238762	.9973786	.814882	.8208053
2001	400000	1.863458	2.102053	2.448324	.9966146	.7653935	.7683964
2001	500000	1.877702	2.181331	2.690163	.9953657	.7260909	.7274758
2001	600000	1.909678	2.301015	3.098217	.9941338	.6902412	.6861027
							i
2002	10000	1.657691	1.826017	2.002043	.9530511	.942882	.9981501
2002	15000	1.903986	1.96269	2.023541	.9833587	.9808553	.998239
2002	20000	2.055593	2.041197	2.026366	.9946879	.9924644	.9977124
2002			2.071943		.9972291		
	25000	2.129704		2.014728		.9929688	.9970157
2002	30000	2.14338	2.067764	1.994998	.9965879	.9905502	.9962503

2002	35000	2.117373	2.043047	1.972996	.9959847	.9890811	.9952588	
2002	40000	2.076128	2.012807	1.953795	.9962787	.9887911	.9938723	i
2002	45000	2.033881	1.984953	1.939449	.9970626	.9886032	.9919951	
2002	50000	2.000891	1.964265	1.930042	.9975811	.9874686	.989695	
							:	
2002	55000	1.975266	1.949169	1.924466	.9979423	.9857457	.9871545	
2002	60000	1.954487	1.937757	1.921467	.9981928	.9835221	.9843476	
		1.937767		1.920405	.9983543			i
2002	65000		1.92929			.980947	.9813721	
2002	70000	1.923508	1.922741	1.920798	.9984664	.9780341	.9781697	
2002	75000	1.911393	1.917755	1.922283	.9985593	.9750184	.9749426	
2002	80000	1.899789	1.913515	1.924808	.998666	.9717111	.9714603	
2002	85000	1.889649	1.910411	1.928254	.9987392	.9681457	.9677901	
			1.908212	1.932493		.964372	.9639655	i
2002	90000	1.88064			.998792			
2002	95000	1.873153	1.906894	1.937102	.9988202	.960659	.9602488	
2002	100000	1.866174	1.906052	1.942261	.9988456	.956813	.9564311	
2002	105000	1.859428	1.905548	1.947977	.9988761	.9528202	.9524968	
2002	110000	1.853103	1.905535	1.954382	.9988967	.948593	.9483619	
		1.847806			.9988981			i
2002	115000		1.906053	1.960935		.9444682	.9443504	
2002	120000	1.84296	1.906978	1.96797	.9988889	.9402175	.940235	
2002	125000	1.838641	1.908305	1.975402	.9988672	.9358912	.9360602	
2002	130000	1.834513	1.90979	1.98308	.9988465	.9315664	.9319057	
2002	135000	1.831059	1.911857	1.991377	.9988031	.9270567	.9275723	
2002	140000	1.828254	1.91426	1.999781	.9987472	.9226304	.9233168	
2002	145000	1.826042	1.917004	2.008359	.9986792	.9182458	.9190929	
2002	150000	1.824442	1.920271	2.017476	.9985962	.9137258	.9147168	
								i
2002	155000	1.823502	1.923654	2.026163	.9985101	.9095361	.9106379	
2002	160000	1.822879	1.927489	2.035572	.9984134	.9051101	.9063107	
2002	165000	1.822783	1.931515	2.044853	.9983154	.9008605	.9021245	
2002	170000	1.822938	1.935595	2.054022	.9982174	.8967535	.8980607	
j 2002	175000	1.823558	1.940234	2.063968	.998112	.8924136	.8937289	
2002	180000	1.824714	1.945132	2.073898	.9980106	.8882015	.8894734	
2002	185000	1.826345	1.950212	2.083697	.9979173	.8841586	.8853347	
2002	190000	1.828304	1.955336	2.093218	.9978341	.8803279	.8813648	
2002	195000	1.830174	1.960096	2.102036	.9977588	.8768374	.8777295	
2002	200000	1.831855	1.964711	2.110807	.9976802	.8734	.8741574	
								i
2002	210000	1.835147	1.974511	2.129961	.9975013	.8660442	.8665184	1
2002	220000	1.838862	1.984547	2.149292	.9973311	.8589196	.8590301	
2002	230000	1.842588	1.994675	2.169032	.9971583	.851903	.8516114	
2002	240000	1.847064	2.005641	2.189963	.9969936	.8448061	.8439874	
2002	250000	1.852308	2.017048	2.21103	.996859	.8380331	.8365495	
2002	260000	1.857817	2.028337	2.231538	.996752	.8317438	.8295154	
2002	270000	1.863502	2.039986	2.252847	.9966494	.825465	.8224192	
2002	280000	1.869265	2.051321	2.273336	.9965746	.8197119	.8157958	
2002	290000	1.874432	2.062074	2.293396	.9964901	.8142415	.8094966	
2002	300000	1.880563	2.074546	2.316587	.9964114	.8082113	.8024421	
2002	400000	1.922727	2.181785	2.545354	.9953341	.759859	.7448723	
2002	500000	1.949023	2.289373	2.842427	.9935468	.7195978	.6953136	
2002	600000	1.971643	2.406095	3.246034	.9913122	.6883991	.6537082	ı
2002	00000	1.9/1043	2.400093	3.240034	. 9913122	.0003331	.0337002	
2003	10000	1.653749	1.817157	1.984579	.9531948	.9444011	.9989878	
								i
2003	15000	1.899351	1.95135	2.003969	.9834496	.9820028	.9992208	
2003	20000	2.048523	2.026594	2.004618	.9946073	.9932318	.9989993	
2003	25000	2.120529	2.05458	1.991047	.9970115	.993676	.9988265	
•								
2003	30000	2.131197	2.047491	1.969356	.9962446	.9916161	.998858	_
2003	35000	2.101205	2.019927	1.945725	.9957571	.9912843	.9990184	
2003	40000	2.055959	1.986979	1.924753	.996337	.9927136	.9991605	
2003	45000	2.011092	1.95716	1.908616	.9973602	.9944853	.9991941	_
2003	50000	1.981158	1.937354	1.897826	.9977636	.9950832	.99913	
2003	55000	1.95748	1.92245	1.890542	.9980805	.9953787	.9990112	
•								
2003	60000	1.937706	1.910583	1.885424	.9983228	.9954232	.9988453	
2003	65000	1.92121	1.901187	1.882015	.9985029	.9952646	.9986436	
								i
2003	70000	1.908046	1.894057	1.879919	.9986026	.9949206	.9984193	į
2003	75000	1.896192	1.888063	1.878801	.9987022	.9944975	.9981753	
2003	80000	1.885188	1.882899	1.878498	.9988105	.9940054	.9979129	
•								
2003	85000	1.875045	1.878497	1.878898	.998931	.9934675	.9976423	ı
2003	90000	1.865293	1.874647	1.880003	.9990464	.9928064	.9973398	
2003	95000				.9991084	.9920678	.9970382	
		1.857558	1.871991	1.88161				
2003	100000	1.850802	1.869968	1.883583	.9991572	.9912953	.9967393	
2003	105000	1.844631	1.86836	1.88586	.9992037	.9904966	.9964424	
•								i
2003	110000	1.8385	1.866926	1.888473	.999264	.9896626	.9961418	ı
2003	115000	1.832539	1.865731	1.891432	.99933	.9887816	.9958363	
2003	120000	1.826883	1.864864	1.894783	.9993922	.9878353	.9955225	
•								
2003	125000	1.822085	1.864476	1.898312	.9994349	.9868751	.9952179	
2003	130000	1.817597	1.864354	1.902113	.9994738	.9858753	.9949125	
								i
2003	135000	1.813705	1.864541	1.906004	.9995018	.98488	.9946194	J
2003	140000	1.810066	1.865046	1.910308	.9995221	.9838073	.994314	
•								i
2003	145000	1.807205	1.865984	1.914757	.9995242	.9827272	.9940144	
2003	150000	1.805067	1.867283	1.919252	.9995129	.9816624	.9937247	
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2003 150000 1.803469 1.868812 1.9223707 .9994938 .9905279 .99931706 .99931707 .99931706 .99931707 .99931706 .99931707 .99931706 .99931707 .99931706 .99931707 .999								
2003	2003	155000	1.803469	1.868812	1.923707	.9994938	.9806279	.9934475
2003 165000 1.801554 1.87262 1.932916 9994386 9978506 9928994 2003 175000 1.801062 1.871717 1.932267 29930721 7976108 99232672 2003 180000 1.801347 1.875658 1.9468653 3993334 9755374 9921125 2003 180000 1.801744 1.882096 1.951266 3993057 7976055 9918702 2003 20000 1.801215 1.88422 1.95563 3993737 9736854 5918732 2003 200000 1.801215 1.88422 1.95563 3993737 9736055 9918702 2003 200000 1.80369 1.891873 1.95643 3993057 9717755 59911385 2003 200000 1.80369 1.891879 1.97428 5991454 9999155 990455 990455 990450 2003 20000 1.80369 1.891879 1.97428 9991454 9969175 99011385 2003 200000 1.80165 1.907512 1.99212 999045 9661072 9901446 2003 200000 1.801433 1.913609 2.000667 9990135 966395 9892619 2003 200000 1.801429 1.913913 2.000202 9999823 9630215 9982619 2003 200000 1.801429 1.913913 2.000202 9999823 9630215 9882619 2003 200000 1.801261 1.935002 2.017472 9989464 9681925 9882619 2003 200000 1.801264 1.935002 2.017472 9989464 9681925 9882619 2003 200000 1.801264 1.935002 2.017472 9989464 9681925 9882619 2003 200000 1.801264 1.935002 2.017472 9989464 9681925 9882619 2003 200000 1.801264 1.935002 2.017472 9989464 9681925 9882619 2003 200000 1.801264 1.935002 2.017472 9989464 9681925 9882619 2003 200000 1.801264 1.935002 2.017472 9989464 9891925 9882619 2003 200000 1.801064 1.935002 2.948264 998946 9891925 9882619 2004 20000 1.801064 2.94826 2.94826 998946 9891925 989192			1 002272				0705012	
2003 170000 1.801101 1.87477 1.937542 9994066 9925273 9926336 9926336 2003 180000 1.801347 1.879658 1.946853 9993364 9755374 9921125 2003 180000 1.801724 1.882096 1.951266 9993057 9756055 9918702 2003 180000 1.802135 1.884522 1.95563 9992731 9756354 9991375 9918702 2003 180000 1.802135 1.884522 1.95563 9992731 9736854 99186332 2003 210000 1.80281 1.884526 1.95653 1.992373 9726355 9918703 991								
2003	2003	165000	1.801554	1.87262	1.932916	.9994386	.9785506	.9928994
2003	2003	170000	1.801101	1.87477	1.937542	.9994066	.977531	.9926336
2003								
2003 180000 1.801724 1.882096 1.991266 9993037 9746035 9918702 2003 190000 1.802851 1.887365 1.960521 9992376 9736935 9913707 2003 200000 1.80369 1.89 1.897486 1.974236 9991454 992635 9913707 2003 20000 1.803769 1.897364 1.974236 9991454 992635 9913707 2003 20000 1.803769 1.897364 1.974236 9991454 992635 991375 9906456 2003 20000 1.811065 1.975167 1.982072 999023 9681072 9901846 2003 20000 1.811065 1.975167 1.992125 9990461 9662244 9897148 2003 20000 1.811043 1.91306 2.00086 999013 9663244 9897148 2003 20000 1.820246 1.925002 2.017472 9988464 9613925 9888601 2003 260000 1.820246 1.925002 2.017472 9988464 9613925 9888601 2003 20000 1.820246 1.937024 2.035272 9988906 9595886 997588 997582 2003 20000 1.833406 1.948957 2.051502 9988562 9954234 9966338 2003 20000 1.833406 1.948957 2.051502 9988562 9954234 9966338 2003 20000 1.852244 2.039351 2.215513 9976488 9936134 9966338 2003 20000 1.85224 2.039351 2.215513 9976488 990873 9782667 2003 20000 1.85224 2.039351 2.215513 9976488 996834 9968633 2003 20000 1.85524 2.039351 2.215513 9976488 996834 9968638 2003 2004 2000 2.021236 2.005171 1.98931 9.9266 9999083 9985766 2004 2000 2.021236 2.005171 1.98931 9.9266 9999083 9985766 2004 2000 2.021236 2.005171 1.98931 9.9266 9999083 9985766 2004 2000 2.00148 2.00548 1.93627 1.998517 9991300 9985856 9992488 2004 40000 2.10307 2.039145 1.955673 9991306 9999083 9985766 2004 40000 2.00148 2.00584 1.93627 1.90831 9.9266 9999083 9985766 2004 40000 2.00148 2.00584 1.93627 1.90831 9.9266 9.999083 9.998576 2004 40000 2.00148 1.93627 1.90831 9.99865 9.998386 9.998688 9.99868 2.99868 2.99868 2.99868 2.99868 2.99868 2.9	2003	175000		1.877171	1.942267	.9993721		.9923672
2003 190000 1.802135 1.804522 1.95562 .9992736 .9736854 .9916327 .9003 .2003 200000 1.803651 1.807565 1.995784 .974236 .9992376 .9726695 .9913707 .9911385 .9003 .2003 .200000 1.80369 1.80 1.964882 .9992075 .9726895 .99913185 .990425 .9904255 .990	2003	180000	1.801347	1.879658	1.946853	.9993384	.9755374	.9921125
2003 190000 1.802135 1.804522 1.95562 .9992736 .9736854 .9916327 .9003 .2003 200000 1.803651 1.807565 1.995784 .974236 .9992376 .9726695 .9913707 .9911385 .9003 .2003 .200000 1.80369 1.80 1.964882 .9992075 .9726895 .99913185 .990425 .9904255 .990	i 2003	185000	1 801724	1 882096	1 951266	9993057	9746055	9918702 İ
2003 195000 1.80369 1.89 1.960521 9992376 9712775 9.991370 2003 200000 1.805769 1.895784 1.974236 9991454 3658755 9906456 2003 220000 1.80167 1.901467 1.983072 9991454 3658755 9906456 2003 220000 1.811065 1.907512 1.992125 9990461 3663244 9887148 2003 220000 1.811453 1.913609 2.008667 999113 9663244 2003 250000 1.80246 1.925002 2.07472 9988464 3613925 988291 2003 250000 1.80246 1.925002 2.07472 9988464 3613925 9884001 2003 270000 1.80246 1.925002 2.07472 9988464 3613925 9884001 2003 280000 1.80246 1.927424 2.03527 2.988930 3579444 .9874789 2003 280000 1.80246 1.927424 2.03527 2.988930 3579444 .9874789 2003 280000 1.80246 1.927424 2.03527 2.988930 3579444 .9874789 2003 280000 1.80246 1.927424 2.03527 2.988930 3579444 .9874789 2003 280000 1.80246 1.927424 2.03527 2.988839 381944 .9874789 2003 280000 1.80246 1.92842 1.99894 2.03837 3.988184 .982584 2003 280000 1.805842 1.99994 2.113320 1.998839 3.98144 .982584 2003 500000 1.80584 2.093511 2.125513 .9976448 2.208573 .978667 2004 10000 1.617271 1.79072 1.965596 .9503185 3402251 .9987645 2004 15000 1.86588 1.926653 1.987391 .9802468 .9785361 .9990662 2004 25000 2.104834 2.03219 1.976996 .9989454 .993791 2004 25000 2.104834 2.03219 1.976996 .9989454 .998384 2004 2000 2.021236 2.001571 1.99331 .9926 .993030 .998189 2004 25000 2.10483 1.98160 1.98160 .998485 .998466 2004 45000 2.107584 1.98160 1.98160 .998485 .998466 .998486 2004 45000 2.107584 1.98160 .998567 .998545 .998586 .998986 .998786 2004 45000 2.007584 1.98160 1.88167 1.88167 .998586 .998586 .998586 .998586 .998586 .998586 .998586 .998586 .998586 .998586 .9985								
2003 20000	2003	190000	1.802135	1.884522	1.95563	.9992731	.9736854	.9916332
2003 20000	2003	195000	1.802851	1.887365	1.960521	.9992376	.9726695	.9913707
2003 20000 1.805769 1.895784 1.974236 .9991454 .9688755 .9906456 2003 220000 1.811065 1.907512 1.992125 .9990461 .9663244 .9897148 2003 240000 1.8114353 1.913609 2.000867 .999105 .9663244 .9897149 .999225 .990615 .9663244 .9897149 .999225 .990615 .9663245 .9982619								
2003 220000 1.80817 1.901467 1.983072 9990925 9961072 9991846 2003 230000 1.811065 1.907512 1.992125 9990461 9663244 9897146 2003 250000 1.817429 1.91391 2.00202 9988923 9630215 9988219 2003 250000 1.817429 1.913911 2.00202 9988923 9630215 9888219 2003 260000 1.820246 1.925002 2.017472 9989464 9613925 9884001 2003 270000 1.820246 1.937424 2.035272 9988909 9595989 987929 2003 280000 1.826946 1.937424 2.035272 9988909 95979444 9874789 2003 290000 1.833406 1.948957 2.051502 9988562 9588254 9866338 9807929 2003 200000 1.833406 1.948957 2.051502 9988562 9588254 9866338 9807929 2003 200000 1.855424 2.093951 2.215513 9576448 9208573 9788067 2003 200000 1.855294 2.039351 2.215513 9576448 9208573 9788067 2004 2000 1.855294 2.039351 2.215513 9576448 9208573 9788067 2004 2000 2.021236 2.005171 1.99599 959348 935002 9388189 2004 25000 2.04834 2.093919 1.985673 9986633 9301813 9751292 2004 25000 2.04834 2.093919 1.985673 999594 999084 999084 2004 25000 2.04834 2.093919 1.985673 999594 999084 999084 2004 25000 2.04834 2.093919 1.995673 999594 999084 2004 25000 2.01236 2.005171 1.98931 99126 991300 9988189 2004 25000 2.01236 2.005171 1.98331 9995545 999464 1.99868 999084 2004 45000 2.070584 1.983627 1.995673 9995545 999464 1.99868 999084 2004 45000 2.070584 1.983627 1.907891 9991106 9894588 999084 2004 45000 2.070584 1.983627 1.907891 9991106 9894588 9990845 2004 45000 1.970386 1.918314 1.873582 996655 9997444 9998274 2004 45000 1.970386 1.918314 1.873582 998655 9992446 9993845 2004 45000 1.970386 1.988697 1.883897 1.888797 999303 9998249 9999088 2004 45000 1.876698 1.884677 1.883698 9990908 9990908 2004 450								
2003 230000 1.811065 1.907512 1.992125 9990451 9.9652244 9.987149 2003 250000 1.817429 1.919391 2.009202 9989823 9630215 9882291 2003 250000 1.802046 1.925002 2.017472 998944 9513925 9884001 2003 270000 1.823261 1.931133 2.02658 998906 9595989 897929 2003 280000 1.826946 1.931133 2.02658 998906 9595989 959793 2003 280000 1.830152 1.943168 2.043371 9988721 9563865 9870578 2003 2003 200000 1.830152 1.943168 2.043371 9988721 9563865 9870578 2003 300000 1.852842 1.999594 2.133301 998389 9357944 998778 2003 2003 200000 1.852942 2.039351 2.215513 997648 928673 798867 2003 2000 1.855294 2.039351 2.215513 997648 928673 798867 2004 2000 1.655294 2.03951 2.215513 997648 928673 798867 2004 2000 1.655294 2.03951 2.215513 997648 928673 798867 2004 2000 2.021236 2.005171 1.98931 9926 9931300 9988189 998662 2.004 2000 2.021236 2.005171 1.98931 9926 9931300 9988189 2004 2000 2.012386 2.005171 1.98931 9926 9938548 9987466 2.004 30000 2.13037 2.039145 1.955673 9955854 998648 998766 2.004 30000 2.13037 2.039145 1.955673 995166 898988 9988766 2.004 40000 2.070584 1.988627 1.907896 9958545 992446 998784 2.004 40000 2.070584 1.988627 1.907896 9958545 992446 998786 2.004 40000 2.070584 1.988627 1.907896 9958545 992446 998786 2.004 40000 2.070584 1.988627 1.907896 9958545 994468 998786 2.004 40000 2.070584 1.988627 1.907896 9958545 994468 998786 2.004 40000 2.070584 1.988627 1.98862	2003	210000	1.805769	1.895784	1.974236	.9991454	.9698755	.9906456
2003 230000 1.811065 1.907512 1.992125 9990451 9.9652244 9.987149 2003 250000 1.817429 1.919391 2.009202 9989823 9630215 9882291 2003 250000 1.802046 1.925002 2.017472 998944 9513925 9884001 2003 270000 1.823261 1.931133 2.02658 998906 9595989 897929 2003 280000 1.826946 1.931133 2.02658 998906 9595989 959793 2003 280000 1.830152 1.943168 2.043371 9988721 9563865 9870578 2003 2003 200000 1.830152 1.943168 2.043371 9988721 9563865 9870578 2003 300000 1.852842 1.999594 2.133301 998389 9357944 998778 2003 2003 200000 1.852942 2.039351 2.215513 997648 928673 798867 2003 2000 1.855294 2.039351 2.215513 997648 928673 798867 2004 2000 1.655294 2.03951 2.215513 997648 928673 798867 2004 2000 1.655294 2.03951 2.215513 997648 928673 798867 2004 2000 2.021236 2.005171 1.98931 9926 9931300 9988189 998662 2.004 2000 2.021236 2.005171 1.98931 9926 9931300 9988189 2004 2000 2.012386 2.005171 1.98931 9926 9938548 9987466 2.004 30000 2.13037 2.039145 1.955673 9955854 998648 998766 2.004 30000 2.13037 2.039145 1.955673 995166 898988 9988766 2.004 40000 2.070584 1.988627 1.907896 9958545 992446 998784 2.004 40000 2.070584 1.988627 1.907896 9958545 992446 998786 2.004 40000 2.070584 1.988627 1.907896 9958545 992446 998786 2.004 40000 2.070584 1.988627 1.907896 9958545 994468 998786 2.004 40000 2.070584 1.988627 1.907896 9958545 994468 998786 2.004 40000 2.070584 1.988627 1.98862	2003	220000	1.80817	1,901467	1.983072	.9990925	.9681072	.9901846 l
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2004 20000 2.021236 2.005171 1.98931 .9926 .9913002 .9988189 2004 25000 2.104834 2.039219 1.976995 .9958185 .9924815 .9928818 2004 30000 2.113515 2.038045 1.935673 .9951966 .9899083 .998768 2004 40000 2.070584 1.983627 1.907891 .994106 .9894588 .9997848 2004 45000 2.070584 1.983627 1.907891 .994106 .9894588 .9999845 2004 45000 2.07248 1.947941 1.888176 .9955654 .9951323 .999414 .99404 .9000 .970386 .918314 .873582 .996495 .9951233 .999414 .99404 .9000 .912879 .883897 1.858878 .99832 .997444 .9993274 .9992215 .996248 .9993975 .9004 .9000 .1912879 .883897 1.858378 .99832 .997424 .9993274 .9902215 .2004 .65000 1.87638 1.851271 .853282 .9986555 .9979249 .9992255 .2004 .75000 1.86592 1.858824 1.85227 .9991317 .9983642 .998513 .99448 .994086 .2004 .85000 .849038 .851211 .852479 .9992255 .9982575 .998353 .997934 .2004 .85000 .849038 .851211 .852499 .9992955 .9982957 .9986355 .9987934 .2004 .95000 .837429 .846886 .854391 .9992995 .9992915 .9999317 .9983655 .998303 .998455 .998255	!							
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2004 30000 2.13037 2.039145 1.955673 99951966 9989083 9987848 2004 40000 2.070584 1.983627 1.907891 .994106 .9894588 .9990845 2004 45000 2.071248 1.947941 1.888176 .9955555 .99525365 .9993145 2004 55000 1.970386 1.918314 1.873582 .9969495 .9951233 .9994089 2004 55000 1.937104 1.898107 1.864583 .9978127 .9966248 .9993375 2004 65000 1.912879 1.883879 1.858878 .99932 .997444 .9993274 2004 65000 1.878638 1.855179 1.853328 .9986655 .997249 .9999068 2004 75000 1.86592 1.858824 1.852123 .999933 .998249 .9999068 2004 75000 1.86592 1.858824 1.85210 .9992303 .998355 .9987934 2004 85000 1.842815 1.848767 1.853227 .9992303 .9983535 .9987934 2004 85000 1.842815 1.848767 1.853279 .9992958 .9982557 .9986552 2004 95000 1.832817 1.845499 1.855779 .999295 .997711 .993085 2004 100000 1.828567 1.844366 1.854391 .999295 .9977867 .998138 2004 100000 1.828567 1.844366 1.85735 .9992875 .9975944 .9979693 2004 105000 1.828567 1.844366 1.85735 .9992875 .9975944 .9979693 2004 105000 1.828567 1.844366 1.85735 .9992875 .997806 .9974528 .9004 .15000 1.802405 1.842815 1.848133 1.86510 .9992871 .9973956 .9978066 .9004 .15000 1.802405 1.842815 1.848183 1.86510 .9992871 .9973956 .9978066 .9004 .15000 1.802405 1.842816 1.86108 .9992879 .997182 .9976273 .2004 .15000 1.802405 1.842816 1.86108 .9992879 .997182 .9976273 .2004 .15000 1.802405 1.842816 1.86108 .9992879 .997182 .9976273 .2004 .15000 1.802405 1.840489 1.876979 .9992875 .9973956 .9978066 .9978006 .	2004	20000	2.021236	2.005171	1.98931	.9926	.9913002	.9988189
2004 30000 2.13037 2.039145 1.955673 99951966 9989083 9987848 2004 40000 2.070584 1.983627 1.907891 .994106 .9894588 .9990845 2004 45000 2.071248 1.947941 1.888176 .9955555 .99525365 .9993145 2004 55000 1.970386 1.918314 1.873582 .9969495 .9951233 .9994089 2004 55000 1.937104 1.898107 1.864583 .9978127 .9966248 .9993375 2004 65000 1.912879 1.883879 1.858878 .99932 .997444 .9993274 2004 65000 1.878638 1.855179 1.853328 .9986655 .997249 .9999068 2004 75000 1.86592 1.858824 1.852123 .999933 .998249 .9999068 2004 75000 1.86592 1.858824 1.85210 .9992303 .998355 .9987934 2004 85000 1.842815 1.848767 1.853227 .9992303 .9983535 .9987934 2004 85000 1.842815 1.848767 1.853279 .9992958 .9982557 .9986552 2004 95000 1.832817 1.845499 1.855779 .999295 .997711 .993085 2004 100000 1.828567 1.844366 1.854391 .999295 .9977867 .998138 2004 100000 1.828567 1.844366 1.85735 .9992875 .9975944 .9979693 2004 105000 1.828567 1.844366 1.85735 .9992875 .9975944 .9979693 2004 105000 1.828567 1.844366 1.85735 .9992875 .997806 .9974528 .9004 .15000 1.802405 1.842815 1.848133 1.86510 .9992871 .9973956 .9978066 .9004 .15000 1.802405 1.842815 1.848183 1.86510 .9992871 .9973956 .9978066 .9004 .15000 1.802405 1.842816 1.86108 .9992879 .997182 .9976273 .2004 .15000 1.802405 1.842816 1.86108 .9992879 .997182 .9976273 .2004 .15000 1.802405 1.842816 1.86108 .9992879 .997182 .9976273 .2004 .15000 1.802405 1.840489 1.876979 .9992875 .9973956 .9978066 .9978006 .	2004	25000	2.104834	2.039219	1.976996	.9958545	.9924461	.9985849 İ
2004 35000 2.115152 2.018045 1.931761 9939796 9984588 9990845 2004 40000 2.070584 1.983627 1.907891 994106 99954588 9990845 2004 50000 1.970386 1.918314 1.888176 9955654 9925365 999314 2004 55000 1.937104 1.888107 1.864583 9978127 9966248 9993975 2004 65000 1.9312879 1.883897 1.855828 9996655 9979249 9993274 2004 65000 1.894132 1.873389 1.855328 9996655 9979249 9993275 2004 70000 1.87638 1.865177 1.853253 99986655 9979249 99992285 2004 75000 1.86592 1.858824 1.85227 9991317 9983535 99990588 2004 75000 1.856186 1.854278 1.852109 9992303 9983535 9987934 2004 85000 1.842815 1.884677 1.852429 9992558 9982557 9986352 2004 95000 1.832817 1.845499 1.855779 9992955 9979113 9993085 2004 95000 1.832817 1.845499 1.855779 9992955 9979711 9993085 2004 105000 1.824395 1.84366 1.85739 9992955 9977867 999318 2004 105000 1.824395 1.84366 1.85739 9992875 9977867 9998138 2004 115000 1.82395 1.843486 1.85139 1.992875 99779544 9976273 2004 120000 1.824395 1.84368 1.85139 1.992875 9977867 999138 2004 120000 1.824395 1.84386 1.85735 9992875 9977867 997806 2004 125000 1.824395 1.84368 1.85139 9992871 997395 997806 2004 125000 1.824305 1.84486 1.86108 9992879 997182 9976273 2004 125000 1.80267 1.840597 1.860999 1.80299								
2004 40000 2.070584 1.983627 1.907891 .994106 .9894588 .999314 2004 50000 1.970386 1.918314 1.873582 .9969495 .9951233 .9994089 2004 50000 1.9737104 1.888107 1.864583 .9978127 .9966248 .9993375 2004 65000 1.912879 1.883887 1.858878 .99832 .997444 .9993274 2004 65000 1.878638 1.855177 1.853325 .9986655 .9979249 .99992235 2004 75000 1.878638 1.855177 1.853225 .9989333 .998249 .9999068 2004 75000 1.86592 1.858824 1.85217 .9991317 .9983642 .99999588 2004 75000 1.86592 1.858824 1.85219 .999233 .9983535 .9987934 2004 85000 1.842815 1.848767 1.853272 .9999131 .9983535 .9987934 2004 85000 1.842815 1.848767 1.853272 .9992915 .9981307 .9984755 2004 95000 1.832817 1.845499 1.855779 .999295 .9977817 .9983085 2004 100000 1.828567 1.844366 1.854391 .999297 .9973711 .9983085 2004 105000 1.828567 1.844366 1.85735 .9992875 .9975944 .9979693 2004 115000 1.820305 1.842486 1.86108 .999287 .997182 .9976273 2004 125000 1.812926 1.841813 1.863245 .9992899 .9997182 .9976273 2004 125000 1.812926 1.841813 1.863245 .9992899 .9997182 .9976273 2004 125000 1.809494 1.840957 1.867909 .9992824 .9964882 .9971136 2004 135000 1.809494 1.840957 1.867909 .9992824 .9964882 .9971136 2004 135000 1.809494 1.840957 1.867909 .9992844 .996203 .997279 2004 135000 1.809494 1.840957 1.867909 .9992844 .9964882 .9971136 2004 155000 1.795901 1.840183 1.875123 .9993007 .9957938 .9966025	!							
2004 45000 2.017248 1.947941 1.888176 .9955654 .9925365 .9993149 2004 55000 1.970386 1.918314 1.873582 .9964945 .9951233 .9994089 2004 55000 1.93104 1.888107 1.864583 .9978127 .9966248 .9993375 2004 65000 1.894132 1.873389 1.855328 .9986655 .997249 .9992235 2004 70000 1.87638 1.865177 1.853253 .9986655 .997249 .9992235 2004 75000 1.87638 1.865177 1.853253 .9986655 .997249 .9992235 2004 75000 1.856186 1.854278 1.85227 .9991317 .9983642 .9989513 2004 80000 1.856186 1.854278 1.85219 .9992303 .9983535 .9987934 .998251 .998	2004	35000	2.115152		1.931761	.9939796	.9882346	.9987848
2004 45000 2.017248 1.947941 1.888176 .9955654 .9925365 .9993149 2004 55000 1.970386 1.918314 1.873582 .9964945 .9951233 .9994089 2004 55000 1.93104 1.888107 1.864583 .9978127 .9966248 .9993375 2004 65000 1.894132 1.873389 1.855328 .9986655 .997249 .9992235 2004 70000 1.87638 1.865177 1.853253 .9986655 .997249 .9992235 2004 75000 1.87638 1.865177 1.853253 .9986655 .997249 .9992235 2004 75000 1.856186 1.854278 1.85227 .9991317 .9983642 .9989513 2004 80000 1.856186 1.854278 1.85219 .9992303 .9983535 .9987934 .998251 .998	2004	40000	2.070584	1.983627	1.907891	.994106	.9894588	.9990845 İ
2004 55000 1.970386 1.918314 1.873582 .9969495 .9951233 .9994089 .9904	!							:
2004 55000 1.937104 1.883807 1.864583 .9978127 .996248 .9993274 .9903274 .9903274 .9903274 .9903274 .9903274 .9903274 .9903274 .9903274 .9903274 .9903274 .9903274 .9903274 .9903274 .9903274 .9903274 .9903275 .9004 .90000 1.876638 1.865176 1.855328 .9986655 .9979249 .9990268 .9903274 .9903275 .9976273 .9903274								:
2004 65000 1.912879 1.883897 1.858878 .998625 .997444 .9993274 .9993274 .9990275 .9004 .9000 1.878638 1.865177 1.853253 .9989383 .998249 .9990968 .9004 .9000 1.86592 1.858248 1.85210 .9991317 .9983642 .9989513 .9987934 .9990968 .9004 .9000 1.85186 1.854278 1.85210 .9992303 .9983535 .9987934 .9982049 .9990968 .9004 .9000 1.842815 1.848767 1.85227 .9991317 .9983635 .9987934 .9000 .9000 1.842815 1.848767 1.852499 .9992658 .9982557 .9986352 .998257 .9986352 .9004 .95000 1.832817 1.845499 1.853272 .9992935 .9978130 .9984755 .9004 .95000 1.832817 1.845499 1.855779 .9992935 .9977807 .998138 .9004 .95000 1.822817 1.845499 1.855779 .9992875 .9977897 .9998035 .9004 .100000 1.828357 1.843353 1.859101 .9992871 .9973954 .9979693 .9004 .15000 1.822367 1.841361 .185556 .9992869 .996562 .9974528 .9004 .15000 1.816452 1.841813 1.865245 .9992869 .996562 .9974528 .2004 .125000 1.812926 .1841361 1.86556 .9992814 .9967203 .997273 .2004 .135000 1.80567 1.840489 1.870528 .9992869 .9964882 .997136 .2004 .135000 1.80567 1.840489 1.870528 .9992804 .996288 .9964882 .997136 .2004 .155000 1.80567 1.840489 1.870528 .9992804 .996288 .9964882 .997136 .2004 .155000 1.80567 1.840489 1.870528 .9992804 .996288 .9964882 .997136 .2004 .155000 1.80567 .184089 1.870528 .9993007 .9995788 .9967678 .2004 .155000 1.792771 .840248 1.885265 .9993183 .9995185 .9966025 .2004 .155000 1.792771 .840248 1.885265 .9993183 .99951652 .9962823 .2004 .155000 1.778261 .184058 .184058 .1885405 .9993183 .99951652 .9962823 .2004 .150000 1.778261 .184058 .1885405 .9993163 .9995165 .9966025 .2004 .150000 1.778676 .184058 .1885619 .9993163 .9993164 .9995165 .996605 .996605 .996606	2004	50000	1.970386	1.918314	1.873582	.9969495	.9951233	.9994089
2004	2004	55000	1.937104	1.898107	1.864583	.9978127	.9966248	.9993975
2004	i 2004	60000	1.912879	1.883897	1.858878	. 99832	997444	.9993274
2004 70000 1.878638 1.855177 1.853253 .998383 .9982429 .9990968 2004 80000 1.856186 1.854278 1.852270 .9991317 .9983642 .998513 2004 85000 1.849038 1.851211 1.852499 .9992658 .9982557 .9986352 2004 95000 1.842815 1.8484767 1.853272 .9992915 .9981309 .9984755 2004 95000 1.832817 1.845499 1.855377 .9992955 .9987911 .9983085 2004 105000 1.832817 1.845499 1.855377 .9992995 .997711 .9983085 2004 105000 1.828567 1.844366 1.85735 .9992875 .9977867 .9983085 2004 105000 1.824395 1.843353 1.859101 .9992871 .9973956 .9976006 2004 115000 1.824395 1.843486 1.86108 .9992879 .9977182 .9976273 2004 125000 1.816452 1.841813 1.865245 .9992861 .9963552 .9974528 2004 125000 1.812926 1.841261 1.86556 .9992814 .9967203 .997279 2004 135000 1.809494 1.840957 1.867909 .9992824 .9964882 .9971136 2004 145000 1.798999 1.840189 1.876220 .9993045 .9966025 .99767678 2004 145000 1.798999 1.840189 1.876207 .9993045 .9954855 .9966025 2004 155000 1.792771 1.84028 1.873351 .9993007 .9955738 .9967678 2004 155000 1.792771 1.84028 1.88265 .9993183 .9951652 .9962823 2004 155000 1.792771 1.84028 1.882565 .9993485 .9951652 .9962823 2004 156000 1.778766 1.84038 1.885455 .9993489 .9954855 .9966025 .2004 150000 1.778056 1.84038 1.885455 .9993489 .9954855 .9956105 .9956025 .2004 150000 1.778056 1.84028 1.888535 .9993484 .994899 .9956105 .2004 150000 1.778056 1.84038 1.8879123 .9993106 .9954855 .9956105 .2004 150000 1.778056 1.84038 1.8879123 .9993404 .9945897 .9955353 .2004 150000 1.778136 1.84028 1.888535 .9993489 .9956105 .9955353 .2004 150000 1.778136 1.840286 1.8895975 .9993489 .9955353 .2004 .20000 1.774324 1.847341 1.915505 .999388 .99859774 .9955353 .2004								!
2004 75000 1.86592 1.858824 1.85217 9.991317 9.9983642 9.989513 2.004 80000 1.856186 1.854278 1.852109 9.992303 9.993535 9.99734 2.004 85000 1.849038 1.851211 1.852499 9.992658 9.982557 9.986352 2.004 95000 1.842815 1.848767 1.853272 9.992915 9.981309 9.984755 2.004 95000 1.832817 1.845499 1.854391 9.992955 9.997911 9.983085 2.004 1.00000 1.832817 1.845499 1.855779 9.992935 9.997916 9.98138 2.004 1.05000 1.828567 1.844366 1.85735 9.992875 9.9975944 9.997693 2.004 1.05000 1.824395 1.843353 1.859101 9.992875 9.9973856 9.9978006 2.004 1.15000 1.820305 1.842486 1.86108 9.992879 9.997182 9.9978006 2.004 1.25000 1.812926 1.841361 1.865245 9.9928679 9.997182 9.9976273 2.004 1.35000 1.805497 1.840389 1.867909 9.992814 9.9967203 9.997279 2.004 1.35000 1.805497 1.840489 1.870528 9.992864 9.996882 9.9971136 2.004 1.40000 1.802201 1.84028 1.870528 9.992861 9.992864 9.9968482 9.9971136 2.004 1.45000 1.795901 1.840183 1.879123 9.993007 9.9959738 9.9966025 2.004 1.55000 1.795901 1.840183 1.879123 9.993106 9.995445 9.9966025 2.004 1.55000 1.795901 1.840183 1.879123 9.993106 9.995445 9.9966025 2.004 1.55000 1.786681 1.840582 1.888553 9.993404 9.994885 9.9964435 2.004 1.50000 1.784055 1.840489 1.870207 9.993347 9.995899 9.9956814 2.004 1.50000 1.784055 1.84048 1.88262 9.993484 9.994299 9.9958295 2.004 1.55000 1.77425 1.840248 1.888545 9.993340 9.995899 9.9956814 2.004 1.50000 1.778625 1.840449 1.895975 9.993474 9.993989 9.9956814 2.004 1.50000 1.77625 1.84044 1.895975 9.99337 9.993762 9.9955353 2.004 1.50000 1.77625 1.84044 1.90385 9.99337 9.993762 9.995387 2.004 2.00000 1.77625 1.840544 1.995005 9.99337 9.993762 9.995383 2.004 2.0000 1.77625								
2004	2004	70000	1.878638	1.865177	1.853253	.9989383	.9982249	.9990968
2004	2004	75000	1.86592	1.858824	1.85227	.9991317	.9983642	.9989513
2004 85000 1.849038 1.851211 1.852499 .9992658 .9982557 .9986352 2004 90000 1.842815 1.846767 1.853272 .9992915 .9981309 .9984755 2004 95000 1.837429 1.846886 1.854391 .9992995 .9977867 .9981388 2004 105000 1.828567 1.844366 1.855779 .9992935 .9977867 .9981388 2004 110000 1.828567 1.844366 1.85735 .9992875 .9973956 .9978036 2004 115000 1.820305 1.842486 1.86108 .9992871 .9973956 .9978006 2004 115000 1.816452 1.841313 1.863245 .9992879 .997182 .9976273 2004 120000 1.812926 1.841361 1.86556 .9992814 .9967203 .997279 2004 135000 1.80567 1.840489 1.870528 .9992824 .9964882 .9971136 2004 135000 1.80567 1.84028 1.870528 .9992824 .9964882 .9971136 2004 145000 1.798999 1.840199 1.876207 .9993045 .9957101 .9966025 2004 155000 1.795990 1.840183 1.879123 .9993104 .9954855 .9964435 2004 155000 1.792771 1.84028 1.88262 .9993183 .9951652 .9962823 2004 165000 1.789766 1.84038 1.88262 .9993183 .9951652 .9962823 2004 165000 1.786681 1.84058 1.884505 .9993288 .994885 .9961305 2004 175000 1.781666 1.84038 1.895975 .9993454 .9942999 .9958295 2004 175000 1.778166 1.84038 1.895975 .9993474 .994397 .9957744 2004 175000 1.7781366 1.84034 1.895975 .9993474 .999370 .9957889 .9958295 2004 185000 1.777722 1.840248 1.895975 .9993163 .9933702 .9953947 2004 185000 1.777523 1.845645 1.991389 .9992654 .9928168 .9952748 2004 200000 1.777625 1.84645 1.93158 .9993007 .9912608 .9945818 2004 200000 1.77625 1.84645 1.93158 .9990057 .9912608 .9945818 2004 200000 1.778625 1.87072 1.96631 1.995864 .9990057 .9912608 .9943832 2004 200000 1.778668 1.875242 1.96631 1.995845 .999571 .9935333 2004 200000 1.78667 1.875242 1.966351 .9995869 .9996682 .9993386 .99								
2004 95000 1.837429 1.846866 1.853272 .9992915 .99979711 .9984755 2004 100000 1.837817 1.8458499 1.855779 .9992935 .9977867 .998138 2004 105000 1.828567 1.845499 1.855779 .9992875 .9977867 .998138 2004 110000 1.824395 1.843353 1.859101 .9992871 .9973956 .9976006 2004 115000 1.820305 1.842486 1.85735 .9992879 .997182 .9976273 2004 120000 1.816452 1.841813 1.863245 .9992869 .99969562 .9974528 2004 125000 1.812926 1.841361 1.86556 .9992814 .9967023 .997279 2004 130000 1.809494 1.840957 1.867909 .9992824 .9964882 .9971136 2004 135000 1.80567 1.840289 1.870528 .9992901 .9959583 .9967678 2004 145000 1.802201 1.84028 1.873351 .9993007 .9959738 .9967678 2004 145000 1.798999 1.840189 1.876207 .9993045 .9957101 .9966025 2004 155000 1.795901 1.840183 1.879123 .9993106 .995455 .9962823 2004 165000 1.789766 1.840388 1.885405 .9993183 .9951652 .9962823 2004 165000 1.789766 1.840388 1.885405 .9993184 .9948885 .9961305 2004 165000 1.786681 1.840562 1.88853 .9993140 .9945887 .9957944 2004 170000 1.784005 1.84093 1.89226 .9993454 .9942999 .9958295 2004 155000 1.77625 1.84044 1.895975 .9993472 .993389 .9956814 2004 180000 1.777472 1.84334 1.90385 .9993163 .993702 .9953947 2004 180000 1.77625 1.84434 1.907404 .9992931 .993166 .9953947 2004 200000 1.77625 1.84444 1.895975 .999388	!							
2004	2004	85000	1.849038	1.851211		.9992658	.9982557	.9986352
2004	2004	90000	1.842815	1.848767	1.853272	.9992915	.9981309	.9984755
2004	i 2004	95000	1.837429	1.846886	1.854391	. 9992995	. 9979711	.9983085 İ
2004								
2004								
2004	2004	105000	1.828567	1.844366	1.85735	.9992875	.9975944	.9979693
2004	2004	110000	1.824395	1.843353	1.859101	.9992871	.9973956	.9978006
2004	i 2004	115000	1 820305	1 842486	1 86108	0002870	997182	9976273
2004								
2004	2004	120000	1.816452	1.841813	1.863245	.9992869	.9969562	.9974528
2004	2004	125000	1.812926	1.841361	1.86556	.9992814	.9967203	.997279
2004	1 2004	130000	1 809494	1 840957	1 867909	9992824	9964882	9971136 İ
2004	:							
2004								
2004	2004	140000	1.802201	1.84028	1.873351	.9993007	.9959738	.9967678
2004	2004	145000	1.798999	1.840199	1.876207	.9993045	.9957101	.9966025 i
2004	•							
2004	!							
2004	2004	155000	1.792771	1.840248	1.882262	.9993183	.9951652	.9962823
2004	2004	160000	1.789766	1.840358	1.885405	.9993288	.9948885	.9961305 İ
2004								
2004	!							
2004	2004	170000	1.784005	1.84093	1.89226	.9993454	.9942999	.9958295
2004	2004	175000	1.781366	1.841449	1.895975	.9993472	.9939899	.9956814 I
2004	•							
2004	•							
2004								
2004	2004	190000	1.77625	1.84444	1.907404	.9992931	.9931064	.9952748 İ
2004 200000 1.774324 1.847341 1.915505 .99923 .9925411 .9950207 2004 210000 1.773701 1.850619 1.923105 .9991586 .992066 .9948003 2004 220000 1.774187 1.854645 1.931158 .9990803 .9916322 .9945818 2004 230000 1.775231 1.858761 1.938846 .9990057 .9912608 .9943832 2004 240000 1.776332 1.86634 1.945991 .9989354 .9909317 .9942059 2004 250000 1.777205 1.86632 1.95303 .9988623 .9906008 .9940386 2004 260000 1.778625 1.87072 1.961044 .998781 .9902632 .9938569 2004 270000 1.780679 1.875242 1.968631 .9987124 .9900069 .993691 2004 280000 1.782778 1.879695 1.976037 .9986458 .989774 .9935333 2004 290000 1.785486 1.884517 1.983561 .9985899 .9895971 .9933764 2004 300000 1.78823 1.889069 1.990449 .9985452 .9894682 .993234 2004 400000 1.808667 1.929168 2.056321 .9979389 .9881229 .991939 2004 500000 1.823232 1.963493 2.117628 .9971635 .9869143 .9907565 2004 600000 1.834717 1.994995 2.177589 .9961665 .9855632 .9894667								.9951469 İ
2004 210000 1.773701 1.850619 1.923105 .9991586 .992066 .9948003 2004 220000 1.774187 1.854645 1.931158 .9990803 .9916322 .9945818 2004 230000 1.775231 1.858761 1.938846 .9990057 .9912608 .9943832 2004 240000 1.776332 1.862634 1.945991 .9989354 .9909317 .9942059 2004 250000 1.777205 1.86632 1.95303 .9988623 .9906008 .9940386 2004 260000 1.778625 1.87072 1.961044 .998781 .9902632 .9938569 2004 270000 1.780679 1.875242 1.968631 .9987124 .9900069 .993691 2004 280000 1.782778 1.879695 1.976037 .9986458 .989774 .9935333 2004 290000 1.785486 1.884517 1.983561 .9985899 .9895971 .9933764 2004 300000 1.78823 1.889069 1.990449 .9985452 .9894682 .993234 2004 400000 1.808667 1.929168 2.056321 .9979389 .9881229 .991939 2004 500000 1.823232 1.963493 2.117628 .9971635 .9869143 .9907565 2004 600000 1.834717 1.994995 2.177589 .9961665 .9855632 .9894667	•							
2004 220000 1.774187 1.854645 1.931158 .9990803 .9916322 .9945818 2004 230000 1.775231 1.858761 1.938846 .9990057 .9912608 .9943832 2004 240000 1.776332 1.862634 1.945991 .9989354 .9909317 .9942059 2004 250000 1.777205 1.86632 1.95303 .9988623 .9906008 .9940386 2004 260000 1.778625 1.87072 1.961044 .998781 .9902632 .9938569 2004 270000 1.780679 1.875242 1.968631 .9987124 .9900069 .993691 2004 280000 1.782778 1.879695 1.976037 .9986458 .989774 .9935333 2004 290000 1.785486 1.884517 1.983561 .9985899 .9895971 .9933764 2004 300000 1.78823 1.889069 1.990449 .9985452 .9894682 .993234 2004 400000 1.808667 1.929168 2.056321 .9979389 .9881229 .991939 2004 500000 1.823232 1.963493 2.117628 .9971635 .9869143 .9907565 2004 600000 1.834717 1.994995 2.177589 .9961665 .9855632 .9894667	•							!
2004 230000 1.775231 1.858761 1.938846 .9990057 .9912608 .9943832 2004 240000 1.776332 1.862634 1.945991 .9989354 .9909317 .9942059 2004 250000 1.777205 1.86632 1.95303 .9988623 .9906008 .9940386 2004 260000 1.778625 1.87072 1.961044 .998781 .9902632 .9938569 2004 270000 1.780679 1.875242 1.968631 .9987124 .9900069 .993691 2004 280000 1.782778 1.879695 1.976037 .9986458 .989774 .9935333 2004 290000 1.785486 1.884517 1.983561 .9985899 .9895971 .9933764 2004 300000 1.78823 1.889069 1.990449 .9985452 .9894682 .993234 2004 400000 1.808667 1.929168 2.056321 .9979389 .9881229 .991939 2004 500000 1.823232 1.963493 2.117628 .9971635 .9869143 .9907565 2004 600000 1.834717 1.994995 2.177589 .9961665 .9855632 .9894667	2004	210000	1.773701	1.850619	1.923105	.9991586	.992066	.9948003
2004 230000 1.775231 1.858761 1.938846 .9990057 .9912608 .9943832 2004 240000 1.776332 1.862634 1.945991 .9989354 .9909317 .9942059 2004 250000 1.777205 1.86632 1.95303 .9988623 .9906008 .9940386 2004 260000 1.778625 1.87072 1.961044 .998781 .9902632 .9938569 2004 270000 1.780679 1.875242 1.968631 .9987124 .9900069 .993691 2004 280000 1.782778 1.879695 1.976037 .9986458 .989774 .9935333 2004 290000 1.785486 1.884517 1.983561 .9985899 .9895971 .9933764 2004 300000 1.78823 1.889069 1.990449 .9985452 .9894682 .993234 2004 400000 1.808667 1.929168 2.056321 .9979389 .9881229 .991939 2004 500000 1.823232 1.963493 2.117628 .9971635 .9869143 .9907565 2004 600000 1.834717 1.994995 2.177589 .9961665 .9855632 .9894667	2004	220000	1.774187	1.854645	1.931158	.9990803	.9916322	.9945818 İ
2004								
2004 250000 1.777205 1.86632 1.95303 .9988623 .9906008 .9940386 2004 260000 1.778625 1.87072 1.961044 .998781 .9902632 .9938569 2004 270000 1.780679 1.875242 1.968631 .9987124 .9900069 .993691 2004 280000 1.782778 1.879695 1.976037 .9986458 .989774 .9935333 2004 290000 1.785486 1.884517 1.983561 .9985899 .9895971 .9933764 2004 300000 1.78823 1.889069 1.990449 .9985452 .9894682 .993234 2004 400000 1.808667 1.929168 2.056321 .9979389 .9881229 .991939 2004 500000 1.823232 1.963493 2.117628 .9971635 .9869143 .9907565 2004 600000 1.834717 1.994995 2.177589 .9961665 .9855632 .9894667								
2004 260000 1.778625 1.87072 1.961044 .998781 .9902632 .9938569 2004 270000 1.780679 1.875242 1.968631 .9987124 .9900069 .993691 2004 280000 1.782778 1.879695 1.976037 .9986458 .989774 .9935333 2004 290000 1.785486 1.884517 1.983561 .9985899 .9895971 .9933764 2004 300000 1.78823 1.889069 1.990449 .9985452 .9894682 .993234 2004 400000 1.808667 1.929168 2.056321 .9979389 .9881229 .991939 2004 500000 1.823232 1.963493 2.117628 .9971635 .9869143 .9907565 2004 600000 1.834717 1.994995 2.177589 .9961665 .9855632 .9894667								
2004 260000 1.778625 1.87072 1.961044 .998781 .9902632 .9938569 2004 270000 1.780679 1.875242 1.968631 .9987124 .9900069 .993691 2004 280000 1.782778 1.879695 1.976037 .9986458 .989774 .9935333 2004 290000 1.785486 1.884517 1.983561 .9985899 .9895971 .9933764 2004 300000 1.78823 1.889069 1.990449 .9985452 .9894682 .993234 2004 400000 1.808667 1.929168 2.056321 .9979389 .9881229 .991939 2004 500000 1.823232 1.963493 2.117628 .9971635 .9869143 .9907565 2004 600000 1.834717 1.994995 2.177589 .9961665 .9855632 .9894667	2004	250000	1.777205	1.86632	1.95303	.9988623	.9906008	.9940386
2004 270000 1.780679 1.875242 1.968631 .9987124 .9900069 .993691 2004 280000 1.782778 1.879695 1.976037 .9986458 .989774 .9935333 2004 290000 1.785486 1.884517 1.983561 .9985899 .9895971 .9933764 2004 300000 1.78823 1.889069 1.990449 .9985452 .9894682 .993234 2004 400000 1.808667 1.929168 2.056321 .9979389 .9881229 .991939 2004 500000 1.823232 1.963493 2.117628 .9971635 .9869143 .9907565 2004 600000 1.834717 1.994995 2.177589 .9961665 .9855632 .9894667	•							
2004 280000 1.782778 1.879695 1.976037 .9986458 .989774 .9935333 2004 290000 1.785486 1.884517 1.983561 .9985899 .9895971 .9933764 2004 300000 1.78823 1.889069 1.990449 .9985452 .9894682 .993234 2004 400000 1.808667 1.929168 2.056321 .9979389 .9881229 .991939 2004 500000 1.823232 1.963493 2.117628 .9971635 .9869143 .9907565 2004 600000 1.834717 1.994995 2.177589 .9961665 .9855632 .9894667	•							
2004 290000 1.785486 1.884517 1.983561 .9985899 .9895971 .9933764 2004 300000 1.78823 1.889069 1.990449 .9985452 .9894682 .993234 2004 400000 1.808667 1.929168 2.056321 .9979389 .9881229 .991939 2004 500000 1.823232 1.963493 2.117628 .9971635 .9869143 .9907565 2004 600000 1.834717 1.994995 2.177589 .9961665 .9855632 .9894667								
2004 290000 1.785486 1.884517 1.983561 .9985899 .9895971 .9933764 2004 300000 1.78823 1.889069 1.990449 .9985452 .9894682 .993234 2004 400000 1.808667 1.929168 2.056321 .9979389 .9881229 .991939 2004 500000 1.823232 1.963493 2.117628 .9971635 .9869143 .9907565 2004 600000 1.834717 1.994995 2.177589 .9961665 .9855632 .9894667	2004	280000	1.782778	1.879695	1.976037	.9986458	.989774	.9935333
2004 300000 1.78823 1.889069 1.990449 .9985452 .9894682 .993234 2004 400000 1.808667 1.929168 2.056321 .9979389 .9881229 .991939 2004 500000 1.823232 1.963493 2.117628 .9971635 .9869143 .9907565 2004 600000 1.834717 1.994995 2.177589 .9961665 .9855632 .9894667	!							
2004 400000 1.808667 1.929168 2.056321 .9979389 .9881229 .991939 2004 500000 1.823232 1.963493 2.117628 .9971635 .9869143 .9907565 2004 600000 1.834717 1.994995 2.177589 .9961665 .9855632 .9894667								
2004								
2004 600000 1.834717 1.994995 2.177589 .9961665 .9855632 .9894667	2004	400000	1.808667	1.929168	2.056321	.9979389	.9881229	.991939
2004 600000 1.834717 1.994995 2.177589 .9961665 .9855632 .9894667	2004	500000	1.823232	1.963493	2.117628	.9971635	.9869143	.9907565 İ
!	!							
	2004	800000	1.034/1/	1.334333	2.1//389	• 230T002	. 2033032	

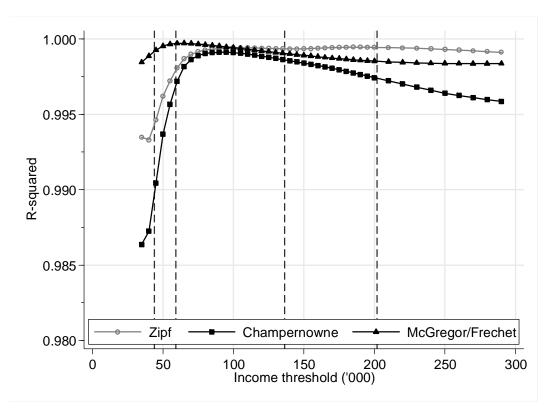
2005	10000	1.580641	1.744421	1.897573	.9540405	.9447801	.99886	ı
							.9991382	i
2005	15000	1.806155	1.863122	1.915884	.9818283	.9802902		l
2005	20000	1.947238	1.93171	1.917475	.9930002	.9918398	.9989129	ı
2005	25000	2.023149	1.961304	1.906776	.9958696	.9927613	.998711	i
								i
2005	30000	2.046969	1.961666	1.888883	.9953004	.9905097	.9987338	i
2005	35000	2.032735	1.943131	1.868685	.9941705	.9890677	.9989526	
2005	40000	1.994165	1.914278	1.849078	.9941658	.9900657	.9992434	i
								1
2005	45000	1.944777	1.882876	1.832763	.9955995	.9930599	.9994673	
2005	50000	1.900828	1.85671	1.821076	.9970117	.9956049	.9995586	1
								i .
2005	55000	1.869271	1.838858	1.814253	.9979158	.9970803	.9995501	l
2005	60000	1.845303	1.826056	1.810402	.9985528	.9979789	.9994895	
j 2005	65000	1.826399	1.816592	1.808519	.9990273	.9985278	.9994007 İ	i
•								l
2005	70000	1.811763	1.809771	1.808007	.9993287	.9987804	.9992929	l
2005	75000	1.802068	1.805643	1.808404	.9994584	.9988042	.9991838	ı
2005	80000	1.794921	1.802935	1.80933	.9995236	.9987412	.9990754	i
								1
2005	85000	1.789508	1.801202	1.810633	.9995483	.9986266	.9989657	ı
2005	90000	1.785647	1.800306	1.812206	.9995405	.9984781	.9988546	
2005	95000	1.782634	1.79983	1.813858	.9995229	.9983242	.998749	i
•								1
2005	100000	1.779874	1.799524	1.81563	.9995034	.9981641	.998644	ı
2005	105000	1.777283	1.799345	1.817511	.9994829	.9979982	.9985397	
2005	110000	1.774732	1.799278	1.819586	.9994606	.997819	.9984317	i
								1
2005	115000	1.772534	1.799361	1.821652	.9994363	.9976431	.9983297	ı
2005	120000	1.770481	1.799598	1.823902	.9994073	.9974543	.998224	
2005	125000	1.768716	1.79996	1.826149	.999376	.9972683	.998123	i
								į
2005	130000	1.766828	1.800235	1.828358	.9993499	.9970849	.9980279	ı
j 2005	135000	1.764732	1.800483	1.830718	.9993263	.9968897	.9979312	1
						.9966899		i
2005	140000	1.762576	1.800729	1.833148	.9993053		.9978369	l
2005	145000	1.760404	1.800972	1.835607	.999287	.996489	.9977469	
2005	150000	1.75814	1.801225	1.838191	.9992709	.9962794	.9976581	ı
								i
2005	155000	1.755905	1.801568	1.840948	.9992529	.9960584	.9975697	l
2005	160000	1.753768	1.801932	1.843677	.9992363	.9958413	.997488	
j 2005	165000	1.751681	1.802312	1.846417	.9992211	.9956248	.9974117	1
								i
2005	170000	1.749476	1.802718	1.849344	.9992074	.9953949	.9973366	l
2005	175000	1.747414	1.803292	1.852497	.9991876	.9951526	.9972624	
j 2005	180000	1.745618	1.803923	1.855533	.999166	.9949229	.997197 İ	ı
								į
2005	185000	1.744003	1.804675	1.85866	.9991398	.9946917	.9971354	ı
2005	190000	1.742631	1.805572	1.861869	.9991083	.9944616	.9970778	
2005	195000	1.741422	1.806499	1.864996	.9990758	.9942412	.9970266	i
								1
2005	200000	1.74036	1.807588	1.868332	.9990379	.9940138	.9969771	ı
2005	210000	1.73907	1.810182	1.87508	.9989501	.9935867	.9968911	
								i
2005	220000	1.738919	1.813156	1.881513	.9988579	.9932299	.9968234	1
2005	230000	1.739171	1.816332	1.888003	.9987617	.9928944	.9967672	
2005	240000	1.73953	1.819395	1.894187	.9986669	.9925843	.9967238	
								i
2005	250000	1.740062	1.822551	1.900428	.9985689	.9922848	.9966899	l
2005	260000	1.740989	1.825917	1.906735	.9984691	.9920101	.9966646	
2005	270000	1.74187	1.829083	1.91269	.998372	.9917548	.9966487	1
•	280000	1.743148					.9966395	i
2005			1.832738	1.919314	.9982637	.9914956		l
2005	290000	1.745494	1.836938	1.925962	.99817	.9913216	.9966378	
2005	300000	1.748029	1.841022	1.932156	.9980882	.9911929	.9966407	1
								i
2005	400000	1.774158	1.877676	1.984173	.9974788	.9907382	.9967678	1
2005	500000	1.799078	1.911734	2.031975	.9968173	.990583	.9969912	
2005	600000	1.823157	1.940135	2.067088	.9964166	.9909351	.9970683	ı
2003	00000	1.023137	1.710100	2.007000	.,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	.,,,,,,,,	.3370003	l
								l
2006	10000	1.568518	1.721735	1.85812	.9555042	.947487	.9988326	ı
2006	15000	1.785646	1.832111	1.872874	.982778	.9814849	.9989827	ı
2006	20000	1.918628	1.893817	1.872284	.9932016	.9916604	.9987064	i
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2006	25000	1.988682	1.918632	1.860211	.9956138	.991774	.9985063	l
2006	30000	2.006964	1.915677	1.842064	.994785	.9892372	.9985707	ı
2006	35000	1.988991	1.895279	1.821744	.9936304	.9879145	.9988497	i
•								l
2006	40000	1.95008	1.866626	1.802348	.9935943	.9890049	.9992056	l
2006	45000	1.90213	1.836623	1.786583	.9950079	.9921154	.9994909	1
2006	50000	1.856352	1.8101	1.774812	.9966739	.9951505	.9996431	ı
•								i
2006	55000	1.824282	1.792411	1.768013	.9976879	.9968519	.9996788	l
2006	60000	1.799336	1.77948	1.764136	.9984629	.9979739	.9996562	ı
2006	65000	1.779319	1.769757	1.762182	.9990408	.9986789	.9996007	ı
							:	i
2006	70000	1.765638	1.763529	1.761601	.9993256	.9989489	.9995322	l
2006	75000	1.756063	1.759523	1.761835	.9994704	.9990215	.9994618	ı
2006	80000	1.749174	1.756958	1.76258	.9995335	.9989883	.9993899	i
•		/-/-/-						i
			1.755473	1.763616	.9995468	.9989011	.9993202	į
2006	85000	1.74441			0005404		0000==4	
2006		1.74441 1.740606	1.754472	1.764784	.9995484	.9988021	.9992551	1
2006	85000 90000	1.740606	1.754472					1
2006 2006	85000 90000 95000	1.740606 1.736863	1.754472 1.753585	1.766125	.9995541	.9986968	.9991905	
2006 2006 2006	85000 90000	1.740606	1.754472 1.753585 1.752897					
2006 2006 2006	85000 90000 95000	1.740606 1.736863	1.754472 1.753585 1.752897	1.766125 1.76771	.9995541	.9986968	.9991905 .9991238	İ
2006 2006 2006 2006	85000 90000 95000 100000 105000	1.740606 1.736863 1.733285 1.730784	1.754472 1.753585 1.752897 1.752734	1.766125 1.76771 1.769399	.9995541 .9995568 .9995391	.9986968 .9985759 .9984435	.9991905 .9991238 .9990594	
2006 2006 2006 2006 2006	85000 90000 95000 100000 105000 110000	1.740606 1.736863 1.733285 1.730784 1.728784	1.754472 1.753585 1.752897 1.752734 1.75283	1.766125 1.76771 1.769399 1.771166	.9995541 .9995568 .9995391 .9995143	.9986968 .9985759 .9984435 .9983069	.9991905 .9991238 .9990594 .9989966	
2006 2006 2006 2006	85000 90000 95000 100000 105000	1.740606 1.736863 1.733285 1.730784	1.754472 1.753585 1.752897 1.752734	1.766125 1.76771 1.769399	.9995541 .9995568 .9995391	.9986968 .9985759 .9984435	.9991905 .9991238 .9990594	
2006 2006 2006 2006 2006 2006	85000 90000 95000 100000 105000 110000	1.740606 1.736863 1.733285 1.730784 1.728784 1.727475	1.754472 1.753585 1.752897 1.752734 1.75283 1.753239	1.766125 1.76771 1.769399 1.771166 1.772955	.9995541 .9995568 .9995391 .9995143	.9986968 .9985759 .9984435 .9983069 .9981719	.9991905 .9991238 .9990594 .9989966	
2006 2006 2006 2006 2006	85000 90000 95000 100000 105000 110000	1.740606 1.736863 1.733285 1.730784 1.728784	1.754472 1.753585 1.752897 1.752734 1.75283	1.766125 1.76771 1.769399 1.771166	.9995541 .9995568 .9995391 .9995143	.9986968 .9985759 .9984435 .9983069	.9991905 .9991238 .9990594 .9989966	

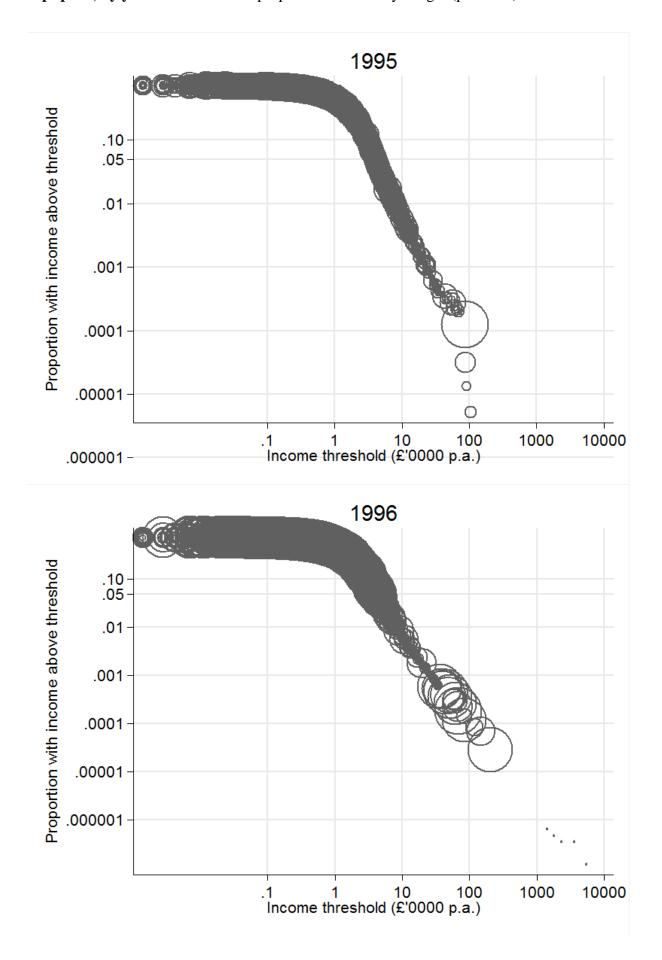
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2006	140000	1.72157	1.755471	1.781855	.999314	.9974934	.9986648
2006	145000	1.719913	1.755753	1.783758	.9992868	.9973436	.9986147
2006	150000	1.718168	1.756038	1.785755	.9992603	.9971867	.9985657
2006	155000	1.71652	1.756342	1.787715	.9992347	.9970332	.998521
2006	160000	1.714755	1.756663	1.789823	.999209	.9968686	.9984767
				1.791915		.9967067	.9984363
2006	165000	1.713144	1.757039		.9991821		
2006	170000	1.711544	1.757414	1.794011	.9991564	.9965447	.9983994
2006	175000	1.709865	1.757779	1.79617	.9991323	.9963774	.9983651
2006	180000	1.70831	1.758316	1.798562	.9991004	.9961966	.9983313
2006	185000	1.707177	1.759034	1.800942	.9990619	.9960244	.9983014
2006	190000	1.706347	1.759917	1.803381	.9990178	.9958556	.9982741
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2006	210000	1.704212	1.763533	1.812323	.9988416	.9952593	.9981982
2006	220000	1.703389	1.765477	1.816888	.9987458	.9949622	.9981735 İ
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2006	230000	1.702591	1.767366	1.821354	.9986493	.9946705	.998158
2006	240000	1.701737	1.769274	1.825945	.9985477	.9943683	.9981512
2006	250000	1.701231	1.771286	1.830443	.9984431	.994085	.998153
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2006	260000	1.700996	1.773563	1.83524	.9983271	.9937962	.9981638
2006	270000	1.701493	1.776147	1.839968	.9982097	.993549	.9981819
2006	280000	1.702466	1.778977	1.844743	.9980901	.993327	.9982066
2006	290000	1.704067	1.78207	1.84944	.9979763	.9931503	.9982362
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2006	300000	1.706225	1.785419	1.854107	.99787	.9930162	.9982699
2006	400000	1.739745	1.820045	1.890366	.9974889	.993406	.9985712
2006	500000	1.770721	1.848648	1.915262	.9974412	.9943225	.9986972
		1.786843	1.867244		.9968955		
2006	600000	1./00843	1.00/244	1.934207	. 2300333	.9941368	.998696
İ							
2007	10000	1.558274	1.703271	1.827221	.9561598	.9490001	.998671
2007	15000	1.765959	1.805814	1.839246	.982832	.9815411	.9986979
2007	20000	1.895226	1.8636	1.837324	.9930906	.9910861	.9983473
2007	25000	1.964653	1.886647	1.824475	.9955482	.9908408	.9980994
2007	30000	1.983413	1.882915	1.805678	.9947178	.9879902	.9981527
2007	35000	1.967547	1.862846	1.784795	.9934853	.986361	.9984605
2007	40000	1.931583	1.835221	1.764951	.9933168	.987244	.9988815
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2007	45000	1.884622	1.805057	1.747762	.9946327	.9904488	.9992673
2007	50000	1.839364	1.777915	1.733965	.9962006	.9936824	.999532
2007	55000	1.807318	1.759469	1.725327	.9972169	.9956704	.9996595
2007	60000	1.780805	1.744986	1.719396	.998084	.9971848	.9997131
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2007	65000	1.759843	1.733978	1.715419	.9986936	.998171	.999718
2007	70000	1.745428	1.72657	1.712953	.9989933	.9986449	.9996966
2007	75000	1.73477	1.721275	1.711433	.999167	.9989001	.9996631
2007	80000	1.726055	1.71712	1.710485	.9992805	.9990465	.999621
2007	85000	1.719477	1.714107	1.709979	.9993334	.9990997	.9995752
2007	90000	1.713921	1.711698	1.709786	.9993737	.9991236	.9995286
2007	95000	1.708612	1.709534	1.709843	.9994094	.9991277	.9994769
2007	100000	1.704456	1.70796	1.710094	.9994211	.9990999	.9994259
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2007	105000	1.70075	1.706659	1.7105	.9994258	.9990582	.999374
2007	110000	1.697436	1.705598	1.711041	.9994232	.9990034	.9993209
2007	115000	1.694656	1.704826	1.7117	.9994088	.998934	.9992664
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2007	120000	1.692428			.9993885	.998861	.9992151
2007	125000	1.690075	1.703749	1.713138	.9993742	.9987892	.9991646
2007	130000	1.687655	1.703208	1.713957	.9993632	.9987152	.9991138
2007	135000	1.685266	1.70272	1.714853	.9993526	.9986368	.9990627
2007	140000	1.682859	1.702239	1.715782	.9993472	.9985598	.9990136
2007	145000	1.680299	1.701733	1.716791	.9993477	.9984807	.9989645
2007	150000	1.677759	1.701271	1.71787	.9993498	.9983982	.9989161
2007	155000	1.675184	1.700781	1.718938	.9993618	.998322	.998872
2007	160000	1.672265	1.700232	1.720173	.9993829	.9982381	.9988255
2007	165000	1.669431	1.69974	1.721459	.999406	.9981521	.9987817
2007	170000	1.66675	1.699361	1.722839	.999425	.9980586	.9987392
2007	175000	1.664227	1.699067	1.724263	.9994422	.9979621	.9986995
2007	180000	1.661824	1.698881	1.7258	.999455	.9978575	.9986609
2007	185000	1.659779	1.698828	1.727309	.9994612	.9977548	.9986265
2007	190000	1.657897	1.698948	1.729013	.9994588	.9976401	.9985914
2007	195000	1.656488	1.699185	1.730563	.9994504	.9975379	.9985622
2007	200000	1.655089	1.699413	1.732099	.9994437	.9974365	.9985358
2007	210000	1.65227	1.699897	1.735264	.9994321	.9972281	.9984887
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2007	220000	1.649856	1.700592	1.738524	.9994128	.9970197	.99845
2007	230000	1.6476	1.701398	1.741893	.9993905	.9968078	.9984196
2007	240000	1.645749	1.702412	1.745346	.9993603	.9965997	.9983976
2007	250000	1.644759	1.703914	1.749018	.9993148	.9964069	.9983828
2007	260000	1.644507	1.705617	1.752465	.9992661	.9962513	.9983751
2007	270000	1.644486	1.707277	1.755646	.9992193	.9961171	.9983723
2007	280000	1.644493	1.709018	1.758973	.9991687	.9959782	.9983739
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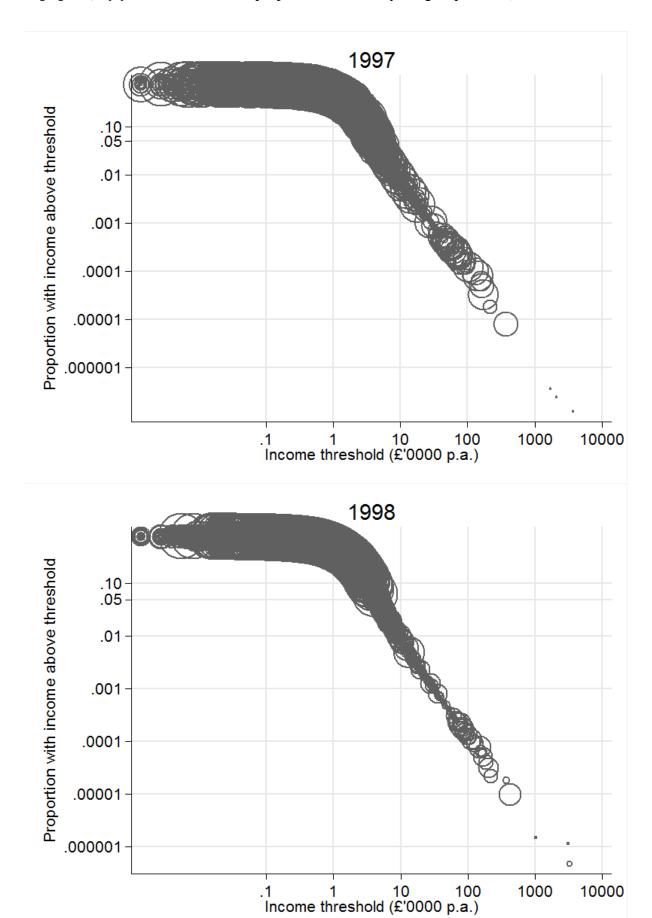
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2007	500000	1.680731	1.75555	1.816262	.9986544	.9960516	.9987454	ļ.
2007	600000	1.699266	1.772893	1.832208	.9986586	.9966416	.9987863	
İ							i	İ
2000	10000	1 502204	1.705281	1 005765	0506340	.953208	0070007	ŀ
2009	10000	1.583394		1.805765	.9586348		.9978807	ļ.
2009	15000	1.792605	1.804323	1.813314	.9834834	.9816579	.9974799	
2009	20000	1.918914	1.855431	1.805353	.9920251	.9873409	.9967942	Ĺ
2009	25000	1.982551	1.870325	1.786209	.9932718	.9841952	.9963781	i.
								!
2009	30000	1.995914	1.858986	1.761207	.9914494	.9791973	.9964378	ı
2009	35000	1.972231	1.831203	1.734584	.9894965	.9765468	.9969166	ı
i 2009	40000	1.926832	1.796089	1.709302	.9890692	.977671	.9976158	i
•								!
2009	45000	1.871061	1.759685	1.687267	.9905384	.9820347	.9983074	l
2009	50000	1.814724	1.726072	1.669134	.992863	.9873195	.9988307	l
2009	55000	1.773044	1.70222	1.657026	.9944208	.9907554	.9991081	i
								ŀ
2009	60000	1.739037	1.683606	1.648317	.9956062	.9932148	.9992368	ļ
2009	65000	1.714681	1.670582	1.642504	.996218	.9945374	.9992653	ı
2009	70000	1.695145	1.66057	1.638493	.9966586	.9954252	.9992378	Ĺ
2009	75000	1.678808	1.652564	1.635702	.9969922	.9960333	.9991738	i
•								!
2009	80000	1.664552	1.645946	1.633854	.9973003	.9964994	.9990865	ļ
2009	85000	1.651654	1.640274	1.632698	.9975783	.996842	.9989796	
2009	90000	1.640204	1.635511	1.632128	.997801	.997048	.9988581	Ĺ
2009	95000	1.630585	1.631742	1.632046	.9979783	.997152	.9987369	i
								!
2009	100000	1.62148	1.628403	1.632365	.9981349	.9971829	.9986049	l
2009	105000	1.613941	1.625828	1.632965	.9982516	.997149	.9984818	
2009	110000	1.60655	1.623486	1.633882	.9983655	.9970722	.9983522	Ĺ
2009	115000	1.600338	1.621693	1.63497	.9984452	.9969523	.9982322	i .
								ļ
2009	120000	1.594451	1.620121	1.636239	.9985275	.9968145	.9981166	
2009	125000	1.588988	1.618783	1.637647	.9986071	.9966607	.998008	ı
2009	130000	1.583715	1.6176	1.63922	.9986895	.9964904	.9979039	i
								ŀ
2009	135000	1.578854	1.616618	1.640884	.9987674	.9963094	.9978091	ļ
2009	140000	1.573938	1.61574	1.642794	.9988481	.9961014	.9977154	l
2009	145000	1.569428	1.615069	1.64481	.9989183	.9958792	.9976307	İ
2009	150000	1.565436	1.614654	1.646937	.9989673	.9956404	.9975545	ŀ
•								!
2009	155000	1.561956	1.614442	1.649079	.9990012	.9953997	.9974888	
2009	160000	1.558778	1.614377	1.651289	.999026	.9951533	.9974311	ı
2009	165000	1.555848	1.614527	1.653725	.9990354	.994886	.9973779	i
								ŀ
2009	170000	1.553591	1.614887	1.656059	.9990265	.9946368	.9973356	ļ.
2009	175000	1.551597	1.615381	1.65846	.9990092	.9943871	.9972998	l
2009	180000	1.550038	1.616038	1.660846	.9989809	.9941499	.9972711	l
2009	185000	1.548822	1.616893	1.663345	.9989419	.9939155	.9972474	i
								ŀ
2009	190000	1.54804	1.61786	1.665731	.9988977	.9937071	.99723	ļ
2009	195000	1.547493	1.618863	1.668009	.9988525	.9935175	.9972176	l
2009	200000	1.547096	1.619946	1.670332	.9988041	.9933324	.9972088	Ĺ
2009	210000	1.546696	1.622157	1.674773	.9987068	.9929991	.9972023	ŀ
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2009	220000	1.546654	1.624497	1.6792	.9986052	.9926893	.9972078	l
2009	230000	1.547243	1.627096	1.683632	.9985015	.9924234	.9972241	l
2009	240000	1.548465	1.630039	1.688218	.9983962	.9921964	.9972504	İ
2009	250000	1.550515	1.633208	1.692562	.9983091	.992059	.997282	ŀ
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2009	260000	1.552748	1.636228	1.696477	.9982376	.9919724	.9973145	ļ
2009	270000	1.555158	1.639258	1.700263	.9981738	.9919146	.9973489	l
j 2009	280000	1.557724	1.642336	1.70401	.9981145	.9918773	.9973854	ı
2009	290000	1.560537	1.645497	1.707705	.9980646	.9918711	.9974234	í
								!
2009	300000	1.563298	1.648458	1.711057	.9980261	.991889	.9974589	ļ.
2009	400000	1.591725	1.676544	1.740569	.9978229	.9925508	.997787	1
j 2009	500000	1.61507	1.698856	1.762684	.9976977	.9933051	.9980029	ı
2009	600000	1.633319	1.716863	1.780448	.997496	.9938346	.9981256	i
1 2009	555500	±.0000±9	1.710003	1.700110		.,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	.,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	1
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2010	10000	1.618442	1.779075	1.935572	.9549968	.9458587	.9985656	1
2010	15000	1.85077	1.903897	1.9551	.9816251	.9798554	.9987221	ı
2010	20000	2.000128	1.977188	1.955444	.9923394	.990446	.9983345	İ
2010			2.009975		.9955933	.9909754		i .
•	25000	2.085539		1.941309			.9979869	!
2010	30000	2.114611	2.010117	1.918849	.9950831	.987987	.9979178	
2010	35000	2.103141	1.988964	1.892727	.9937049	.9856182	.9981256	
2010	40000	2.063532	1.955553	1.866943	.9934753	.9861947	.9984903	Ĺ
2010		2.003332	1.918544		.99471			l
	45000			1.843764		.9892078	.9988508	!
2010	50000	1.962686	1.885712	1.824519	.996067	.9921531	.9991065	ļ
2010	55000	1.92884	1.863037	1.811229	.9967775	.9938045	.9992462	
2010	60000	1.905112	1.846635	1.800994	.996979	.9945349	.9993271	Ĺ
								ŀ
2010	65000	1.887889	1.834665	1.793403	.997005	.9948956	.9993734	!
2010	70000	1.87202	1.824047	1.787051	.9970412	.9952289	.9993989	ļ
2010	75000	1.857582	1.814807	1.781942	.9971052	.9955508	.9994047	1
2010	80000	1.843746	1.806329	1.777654	.9971954	.9958677	.999392	Ĺ
2010	85000							i .
•		1.830664	1.798657	1.774166	.9973099	.9961709	.9993623	!
2010	90000	1.818257	1.791711	1.771412	.9974554	.9964663	.9993176	1
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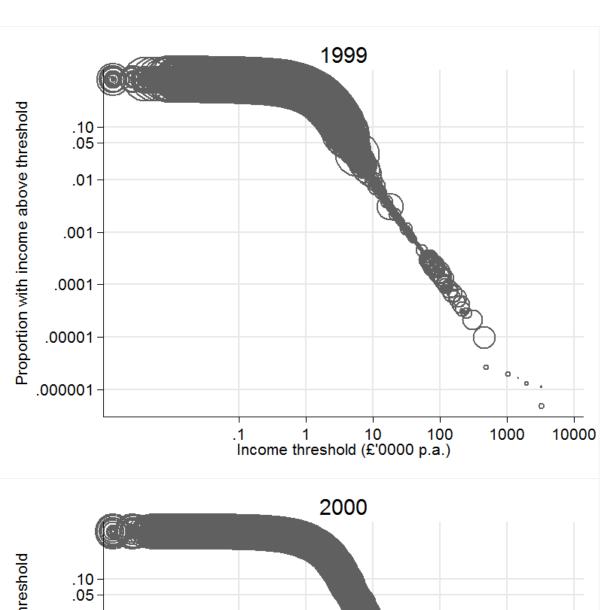
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	2010	115000	1.770676	1.767631	1.765324	.9978651	.9969791	.9989204	
	2010	120000	1.764302	1.764776	1.765182	.9978679	.9969169	.9988288	
	2010	125000	1.758188	1.762148	1.765256	.9978948	.9968666	.9987398	
	2010	130000	1.751557	1.759403	1.765539	.9979716	.996846	.9986476	
	2010	135000	1.744557	1.756617	1.766058	.9980857	.9968357	.9985508	
	2010	140000	1.737657	1.753983	1.766797	.9982211	.996823	.9984543	
	2010	145000	1.730541	1.751375	1.767785	.9983888	.9968108	.9983557	
	2010	150000	1.723528	1.74891	1.768985	.9985806	.9967961	.9982601	
	2010	155000	1.716486	1.746557	1.770453	.9987901	.9967651	.9981645	
	2010	160000	1.70936	1.744353	1.772312	.9989986	.9966893	.9980647	
	2010	165000	1.703208	1.742756	1.774536	.9991359	.9965293	.9979648	
	2010	170000	1.698755	1.741831	1.776621	.9992118	.9963534	.9978834	
	2010	175000	1.694807	1.741233	1.778925	.9992626	.9961485	.9978038	
	2010	180000	1.691576	1.740925	1.781189	.9992931	.9959438	.9977337	
	2010	185000	1.688759	1.740829	1.783522	.999311	.995733	.9976684	
	2010	190000	1.686447	1.74102	1.78599	.9993111	.995513	.9976059	
	2010	195000	1.684625	1.741405	1.788415	.9993007	.9953014	.9975497	
	2010	200000	1.683296	1.741987	1.790798	.9992806	.9951009	.9974986	
	2010	210000	1.681251	1.743444	1.795631	.9992298	.994709	.9974057	
	2010	220000	1.679924	1.745085	1.800215	.9991726	.9943532	.9973289	
	2010	230000	1.679366	1.747228	1.805135	.9991029	.9940022	.9972569	
	2010	240000	1.67932	1.749335	1.809528	.999037	.9937068	.9971996	
	2010	250000	1.679477	1.751694	1.814277	.9989636	.9933967	.9971448	
	2010	260000	1.679827	1.753909	1.818565	.9988954	.9931262	.9971009	
	2010	270000	1.680567	1.756584	1.823462	.9988171	.992836	.997057	
	2010	280000	1.68188	1.759251	1.827787	.9987528	.9926198	.9970224	
	2010	290000	1.683206	1.761917	1.832117	.9986866	.9924039	.9969912	
	2010	300000	1.684676	1.764572	1.836291	.9986241	.9922087	.9969641	
	2010	400000	1.708503	1.794199	1.875638	.9982446	.9911646	.9967797	
	2010	500000	1.734657	1.821174	1.906798	.9982275	.991017	.9966096	
	2010	600000	1.758726	1.844952	1.932922	.9983437	.9911214	.9964098	
•	+							+	

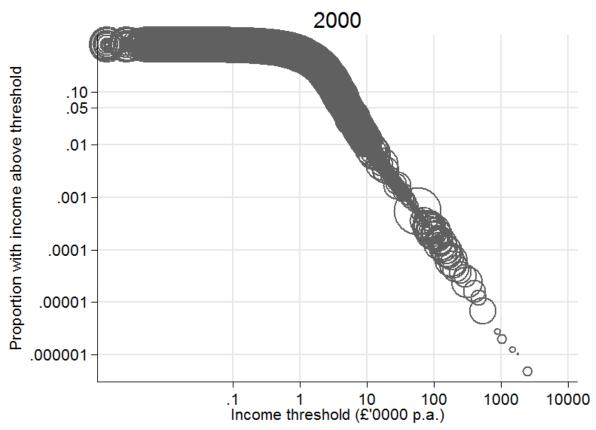
The relationship between R^2 and threshold in 2007 is shown below:

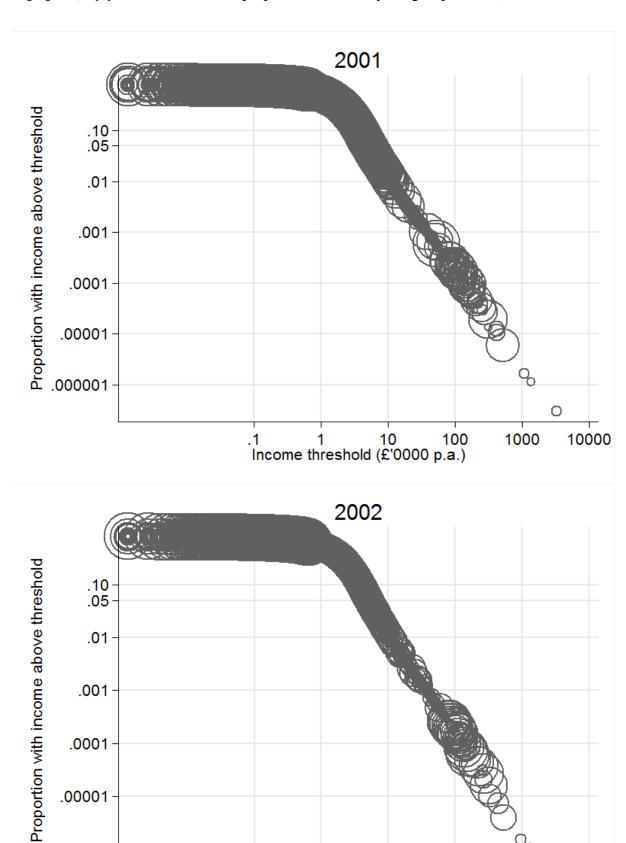










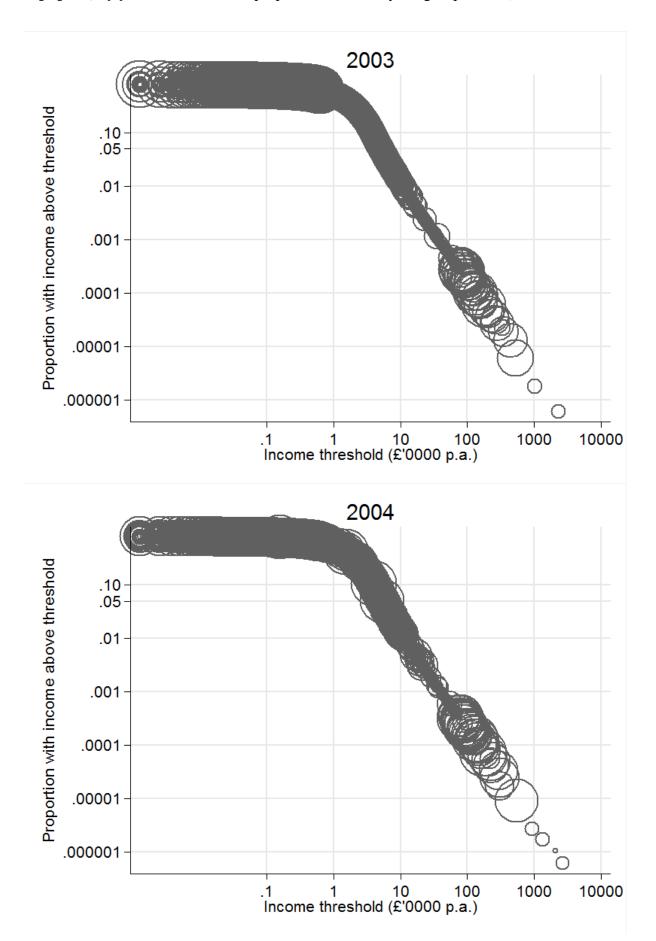


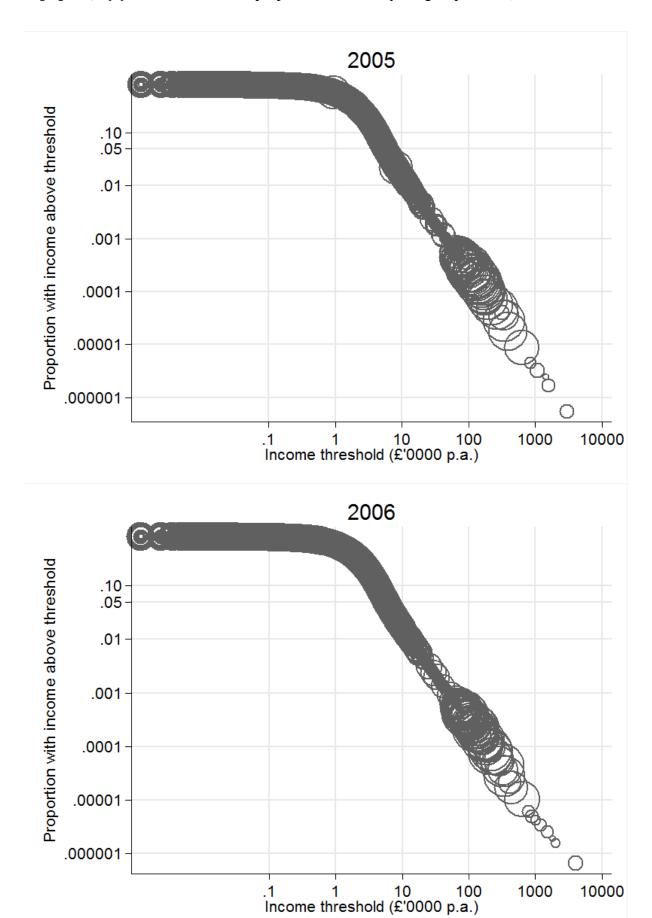
.1 1 10 100 Income threshold (£'0000 p.a.)

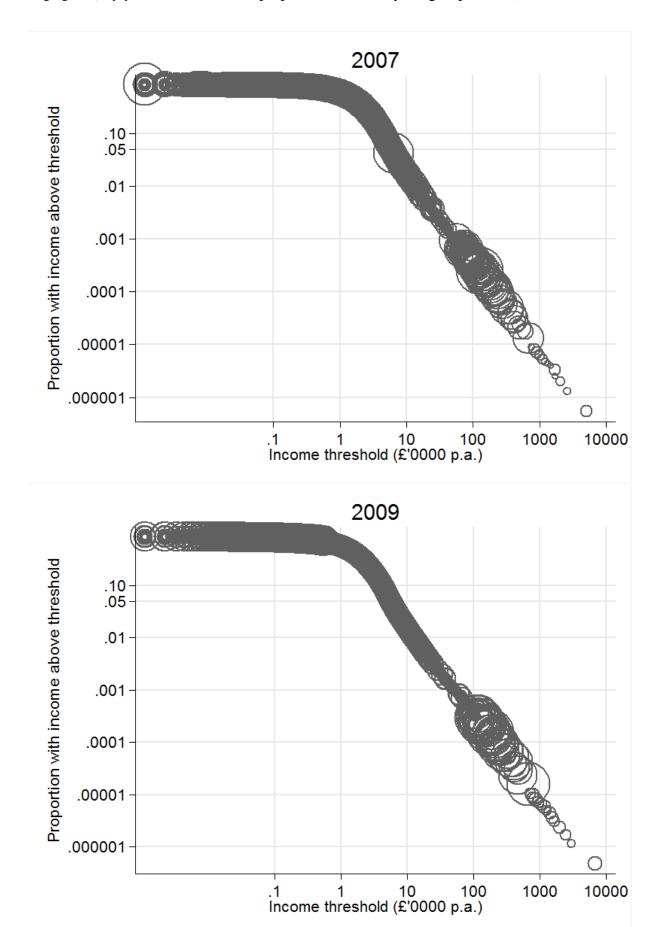
1000

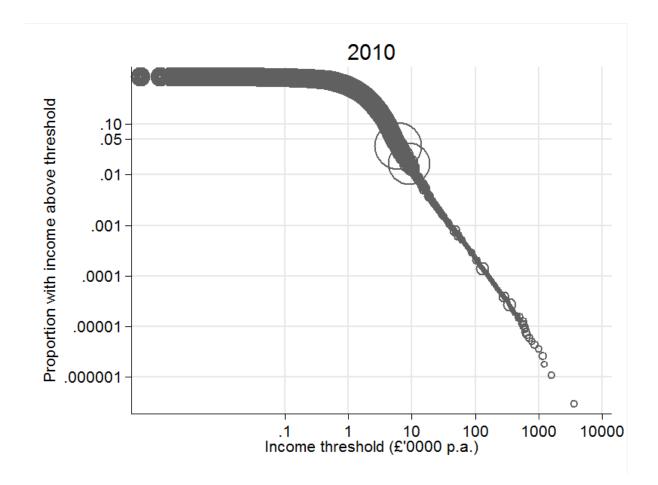
10000

.000001

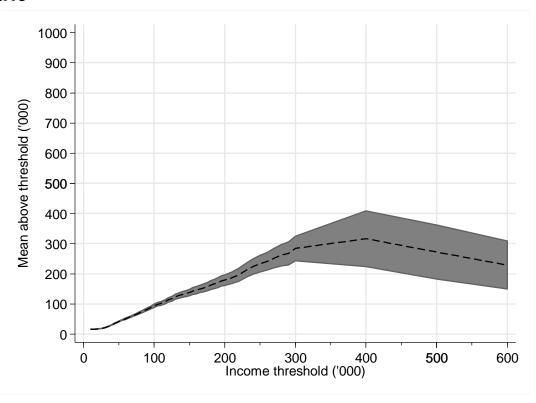


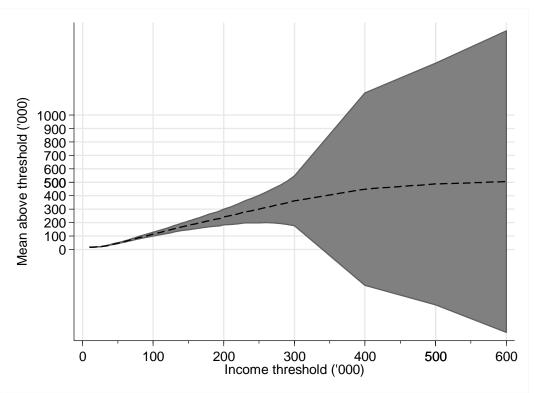




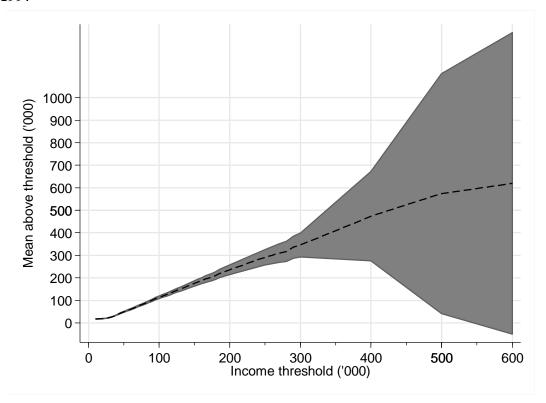


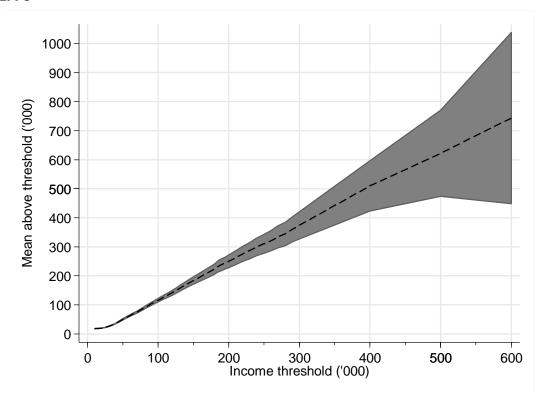
1995



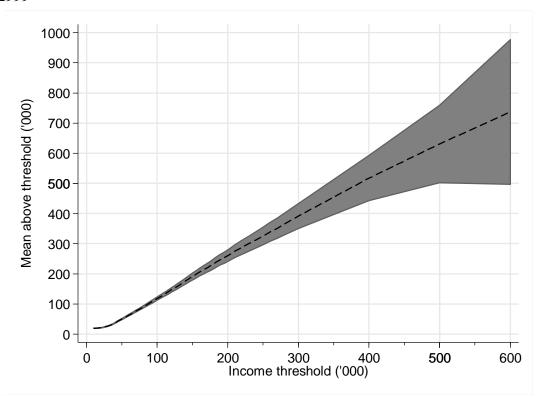


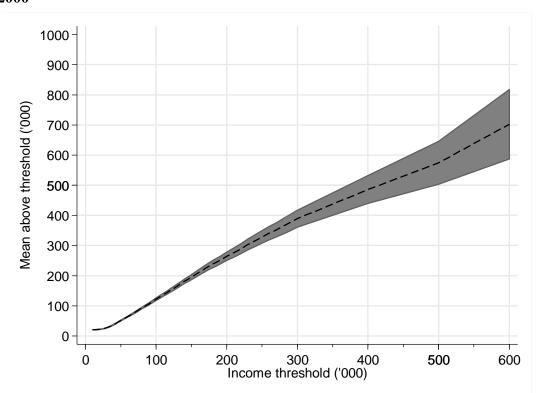
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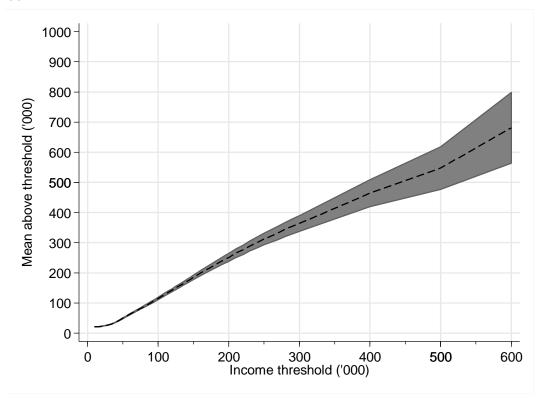


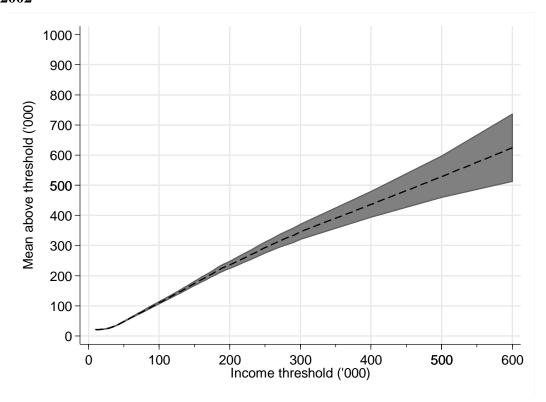
1999



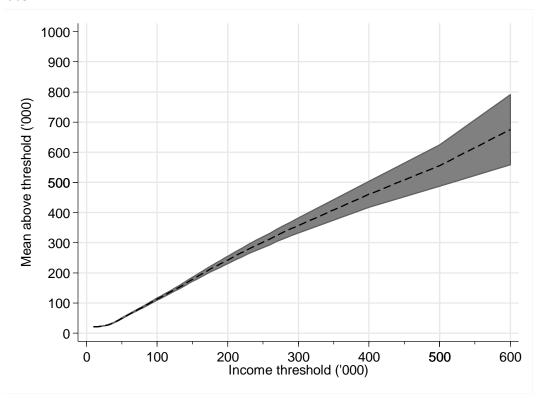


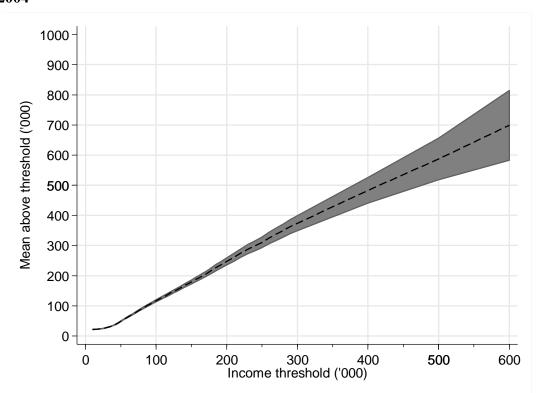
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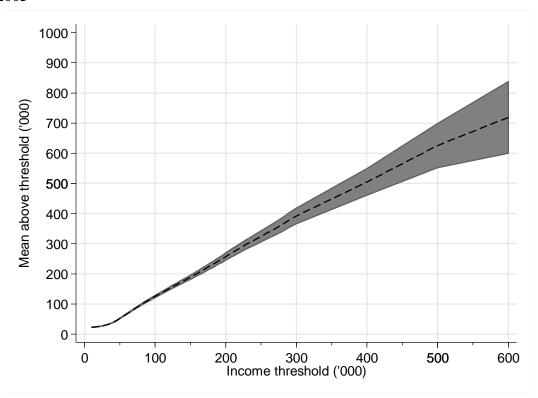


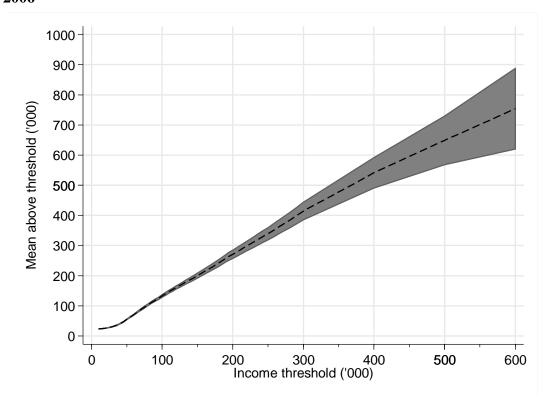
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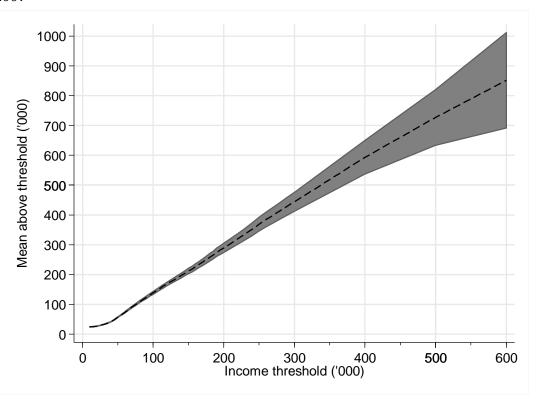


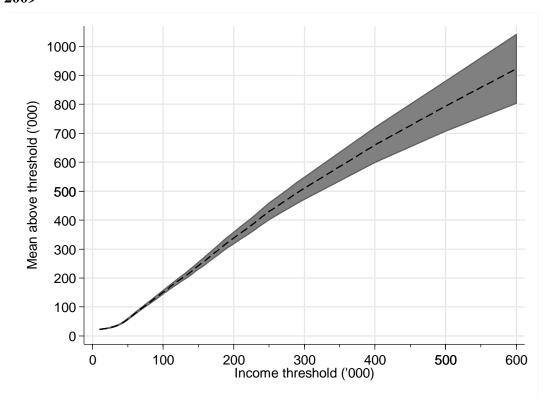
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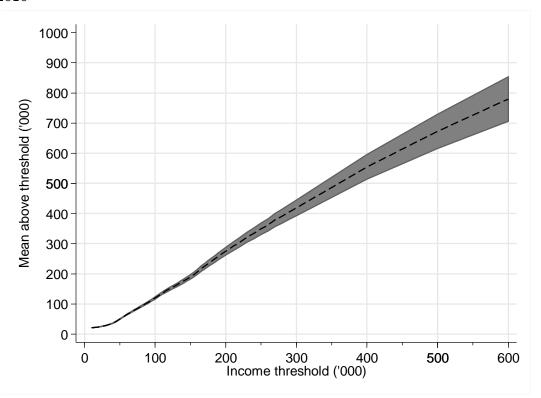




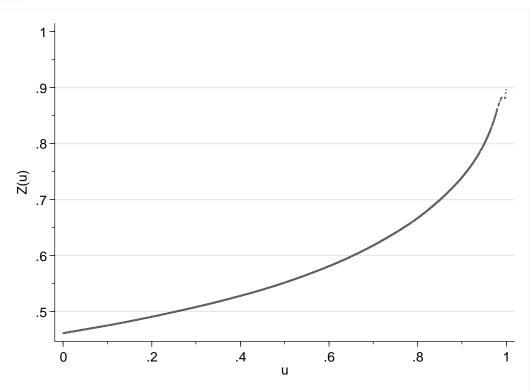
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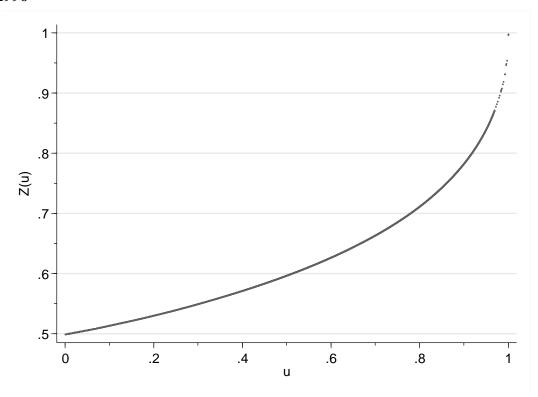




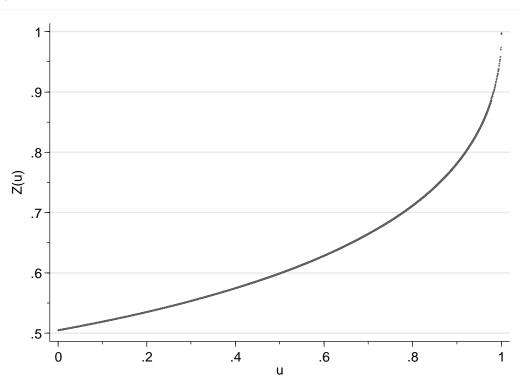


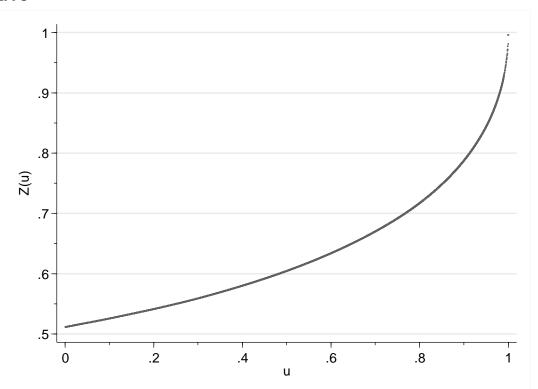
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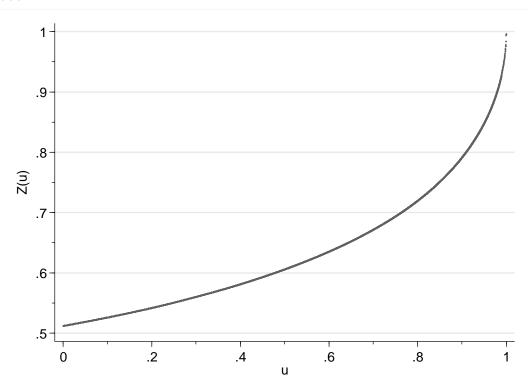


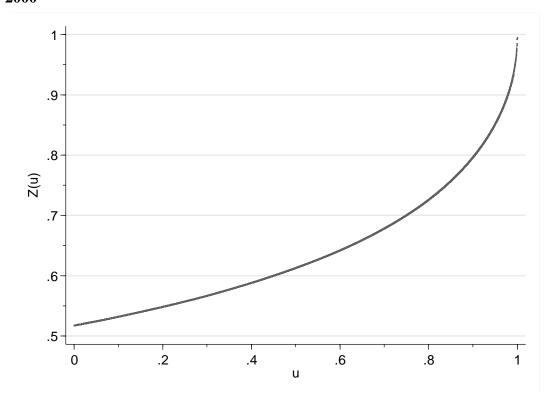


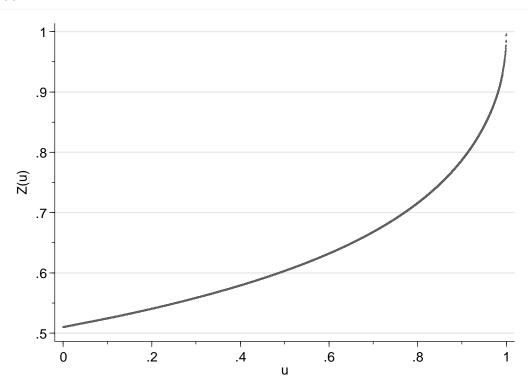


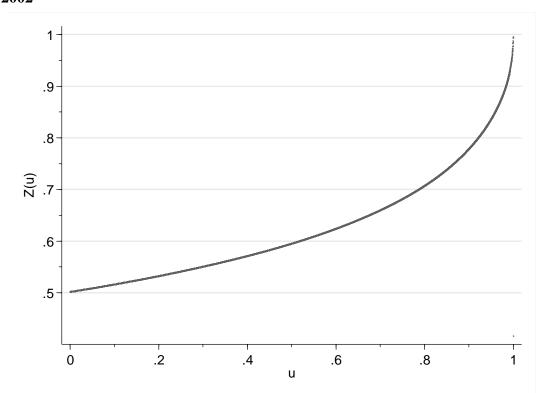


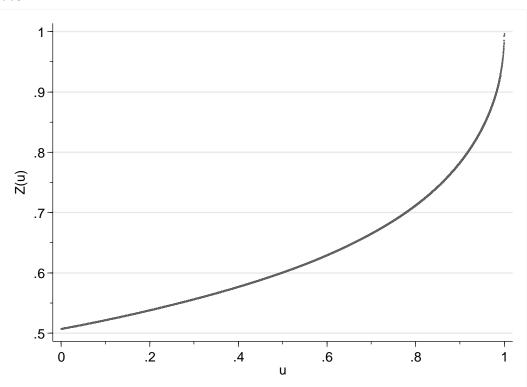


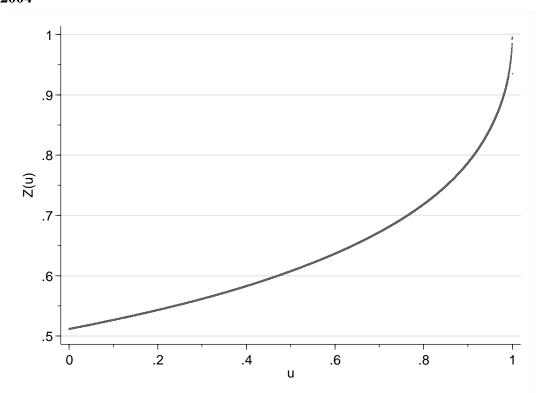


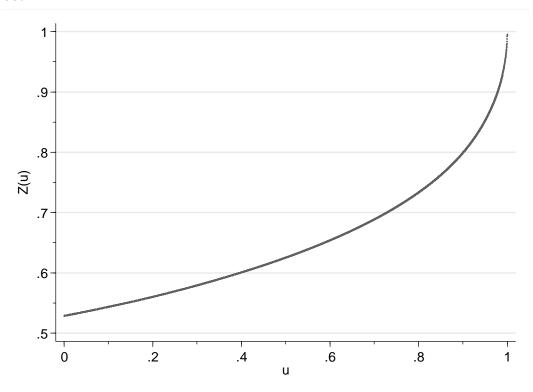


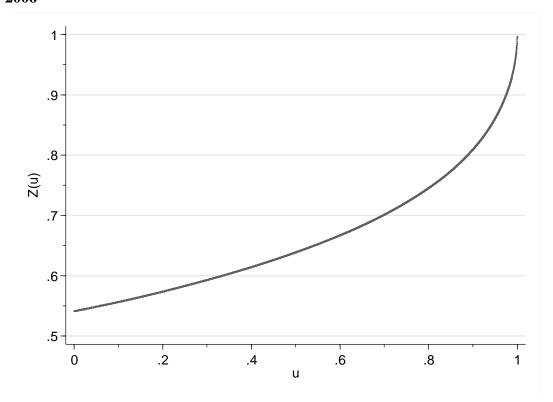


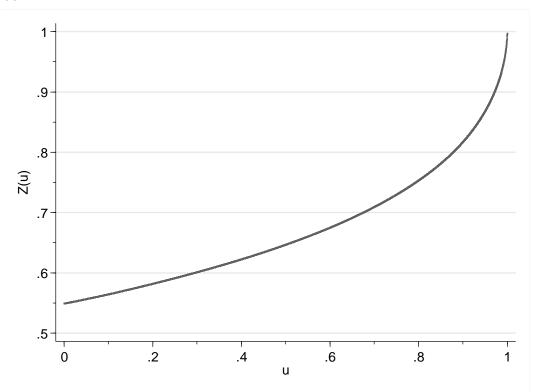


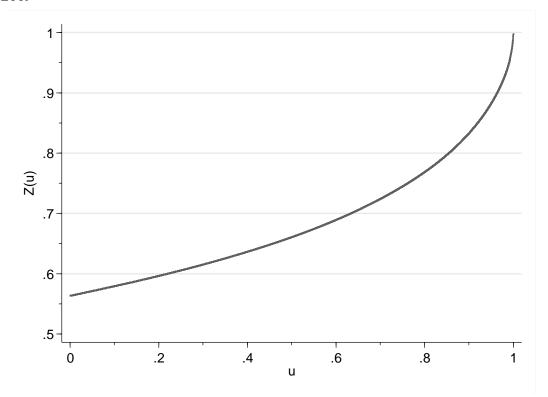


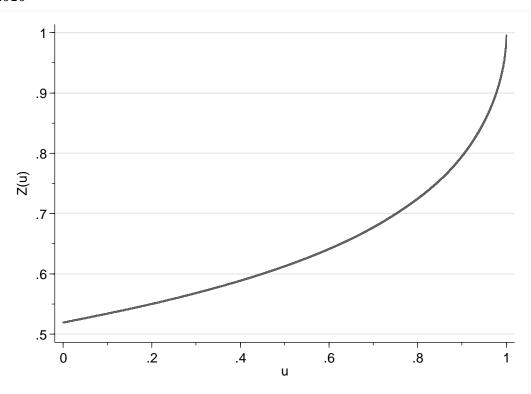






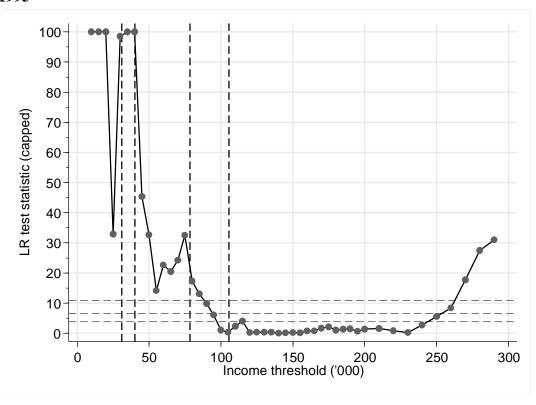


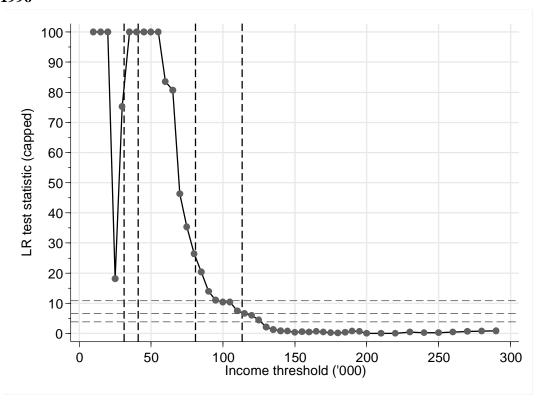




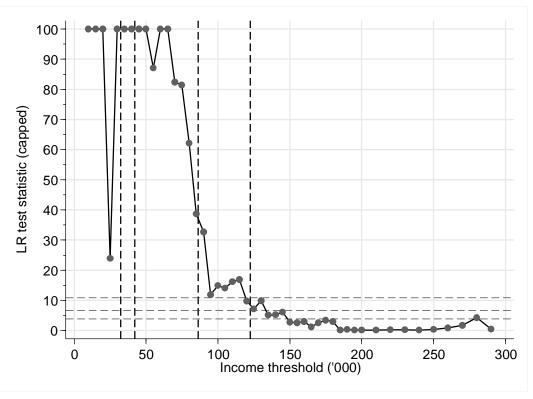
Vertical dashed lines show (from left to right) p90, p95, p99, p99.5

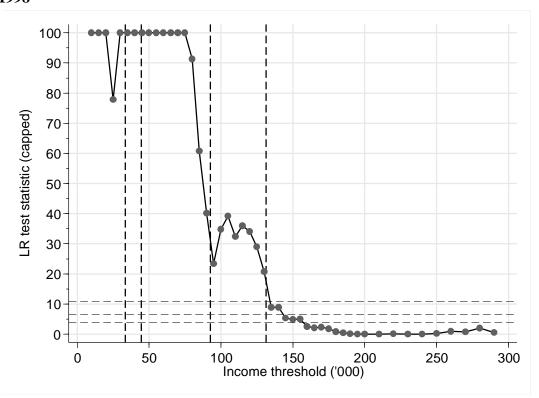
1995



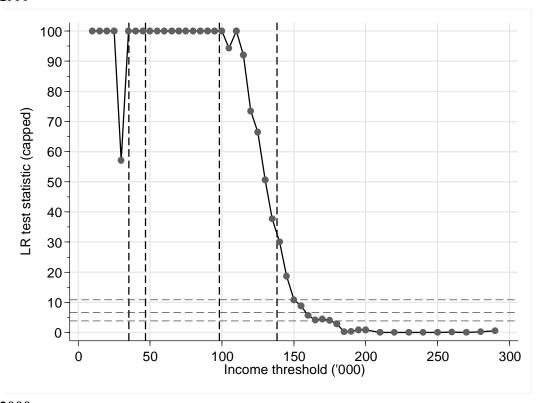


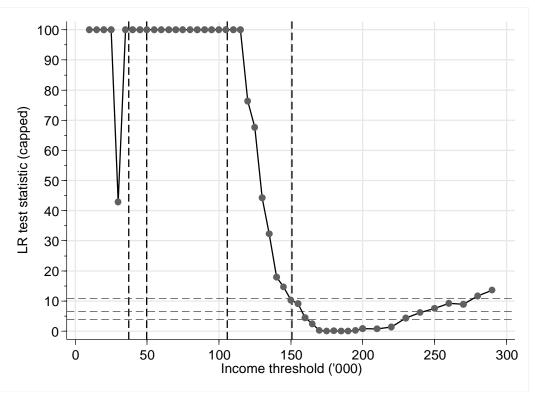
1997



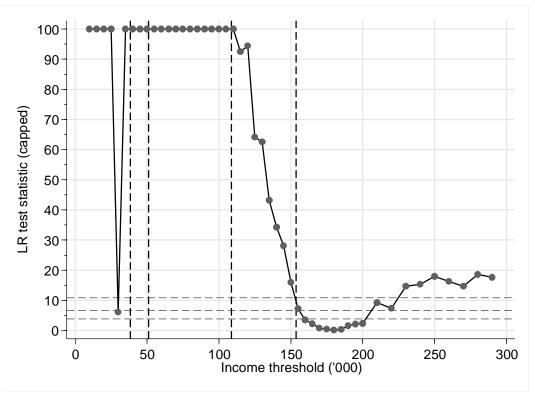


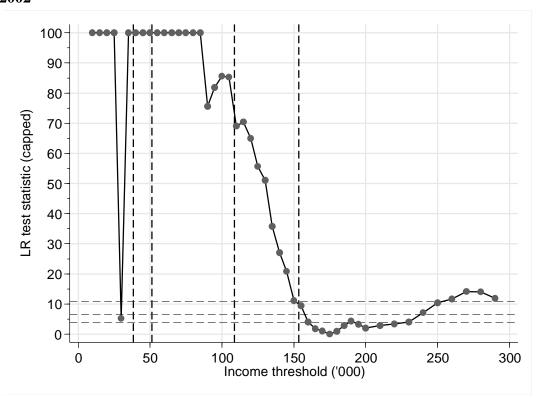
1999



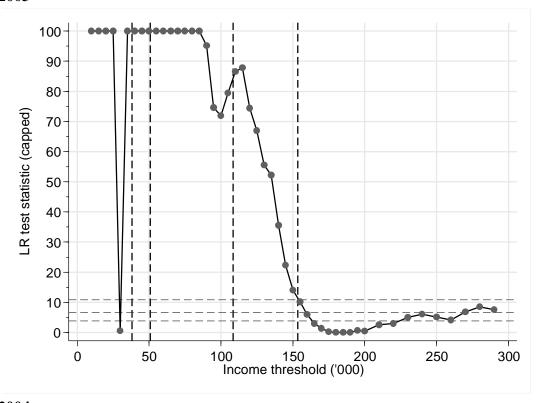


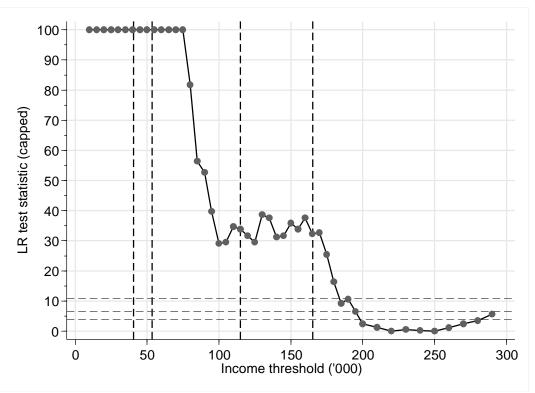
2001



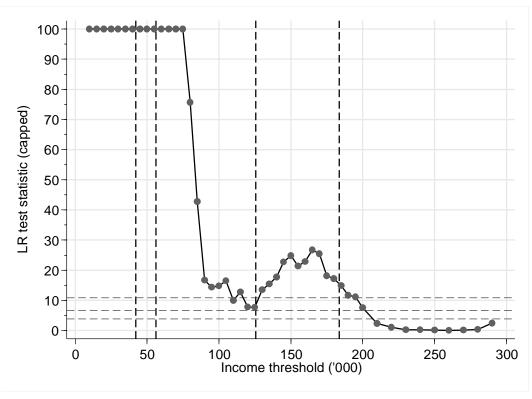


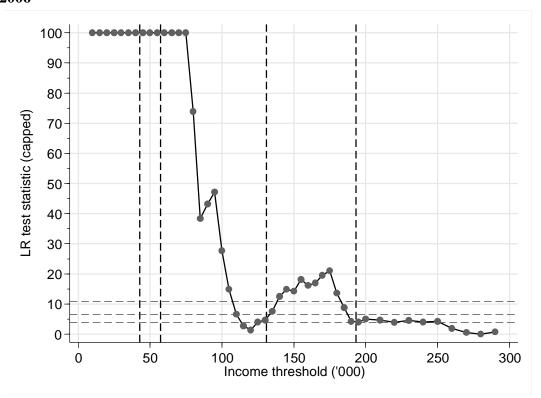
2003



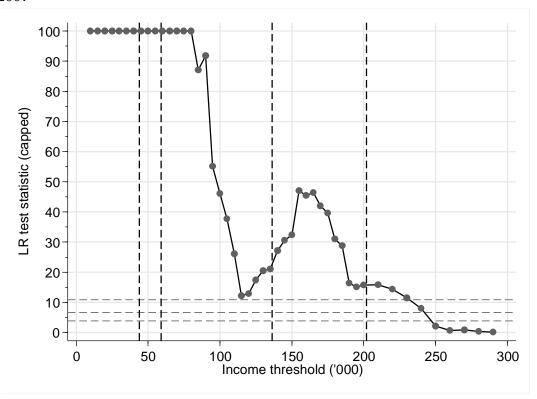


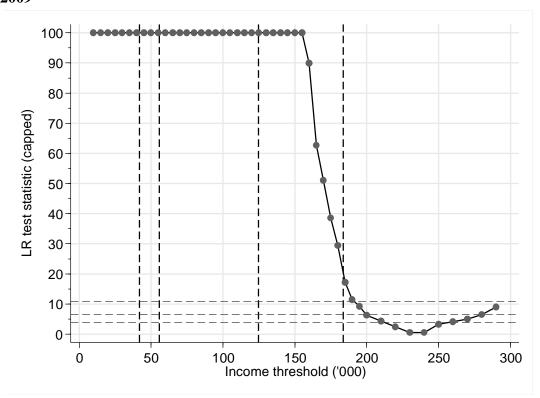
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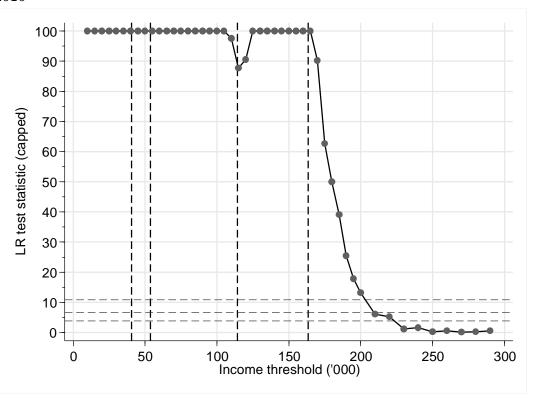




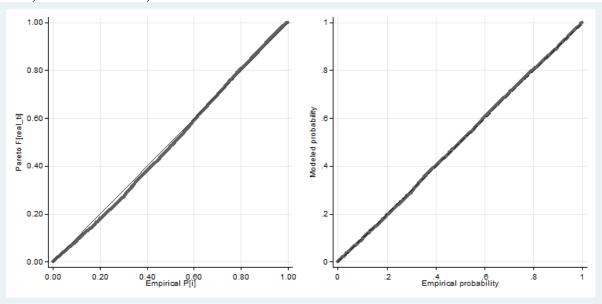
2007

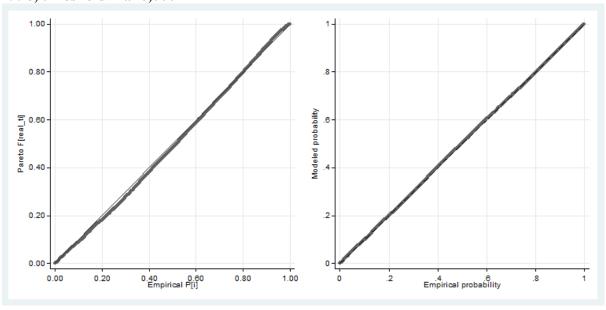




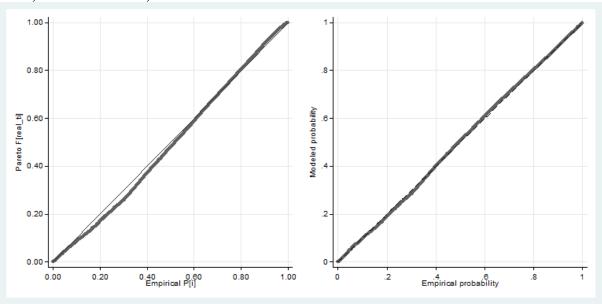


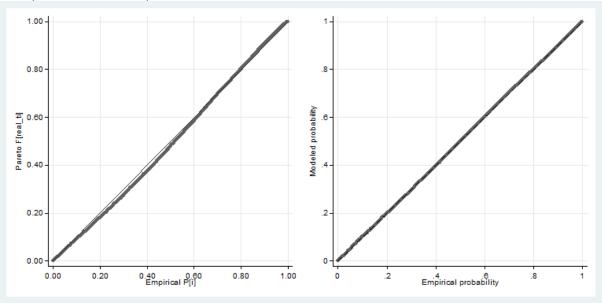
1995, threshold = £40,000



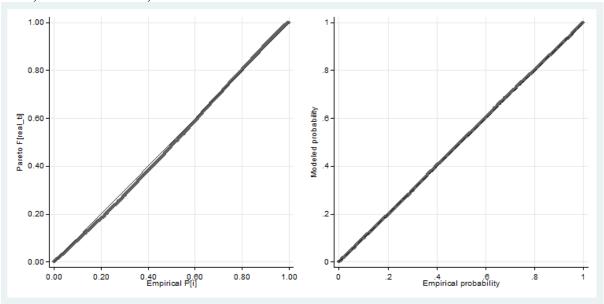


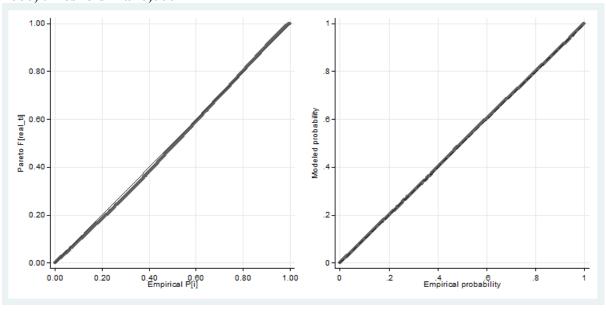
1997, threshold = £40,000



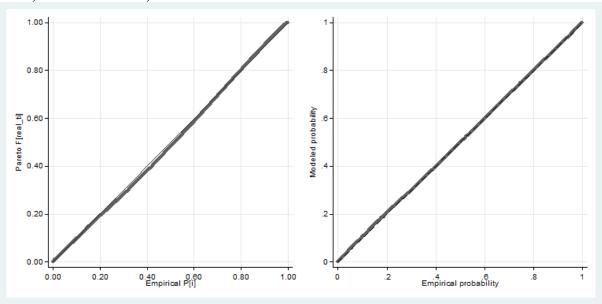


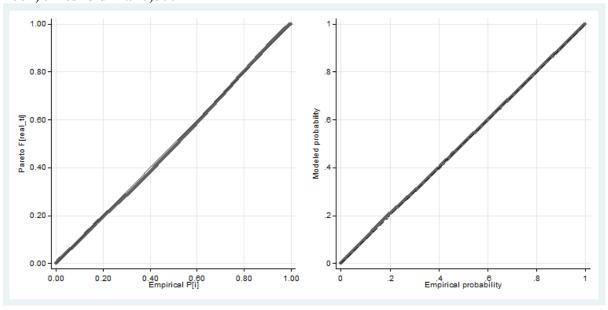
1999, threshold = £40,000



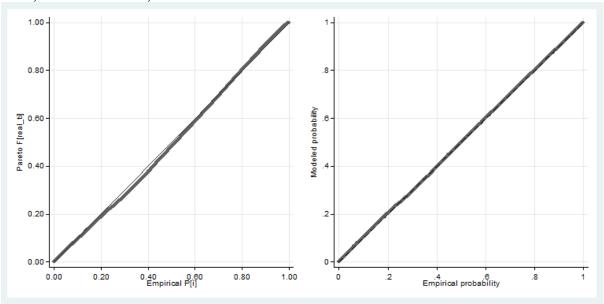


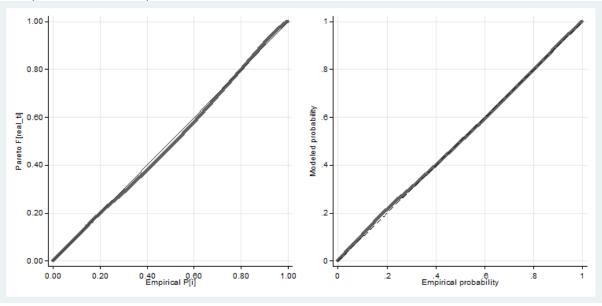
2001, threshold = £40,000



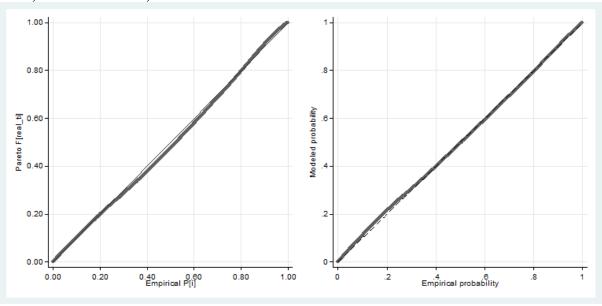


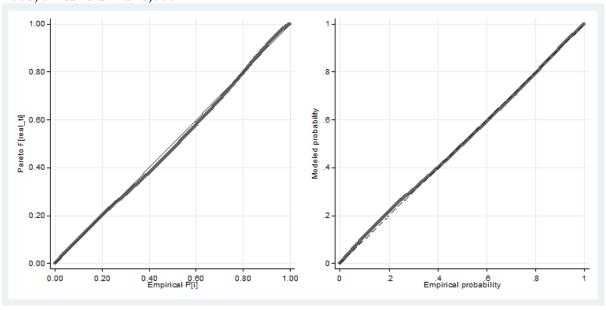
2003, threshold = £40,000



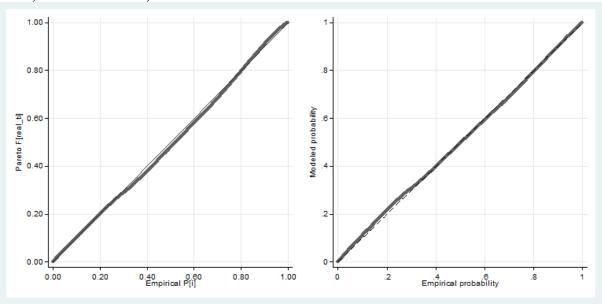


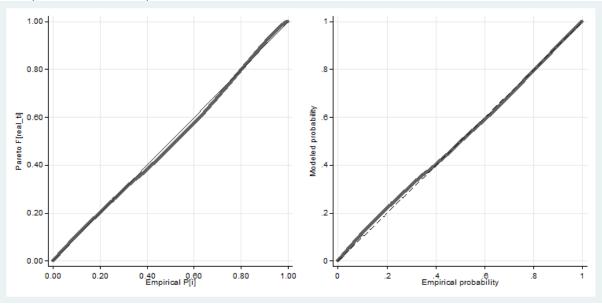
2005, threshold = £40,000

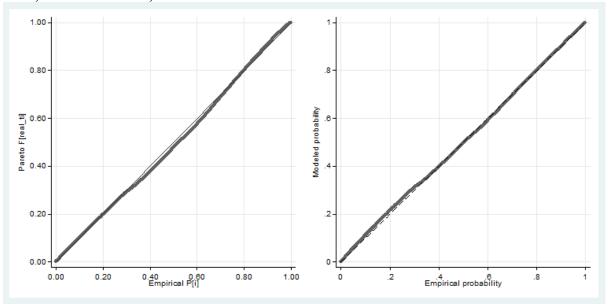




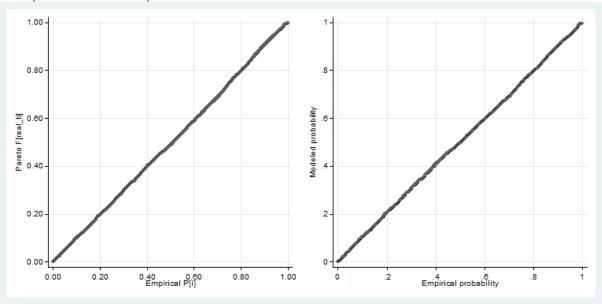
2007, threshold = £40,000

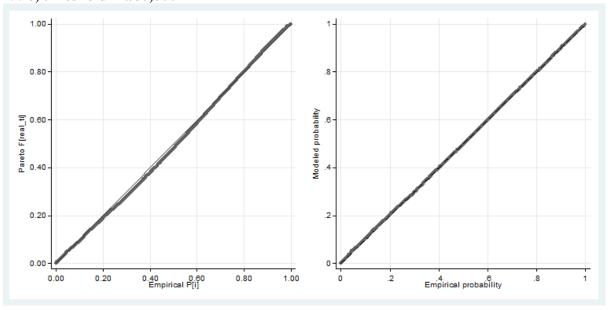




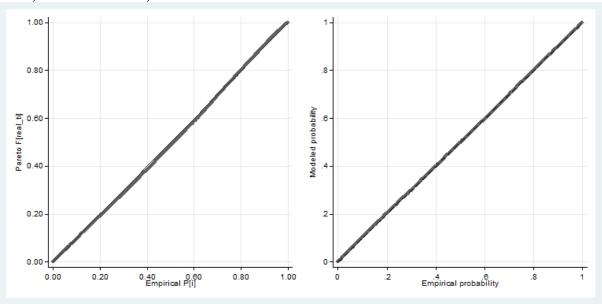


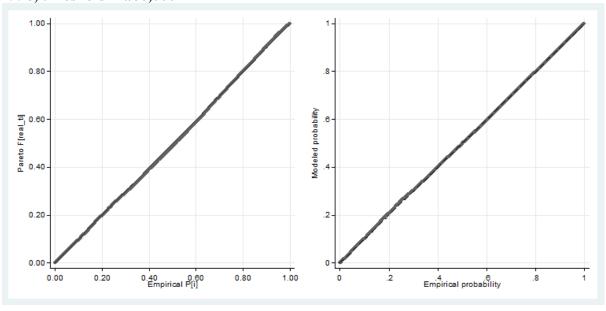
1995, threshold = £60,000



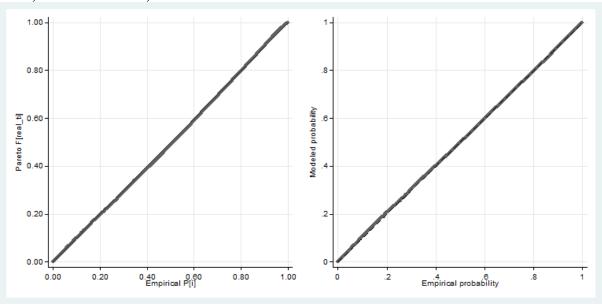


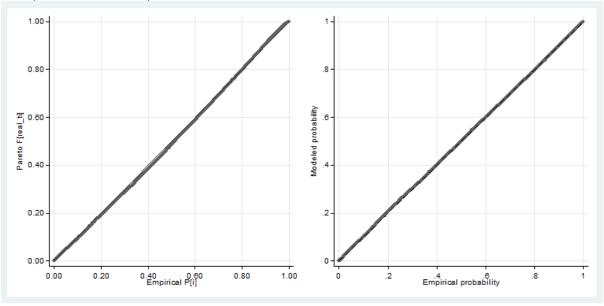
1997, threshold = £60,000



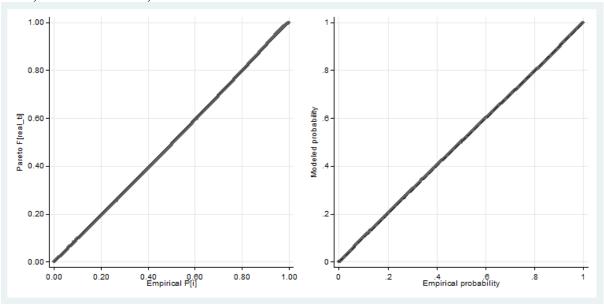


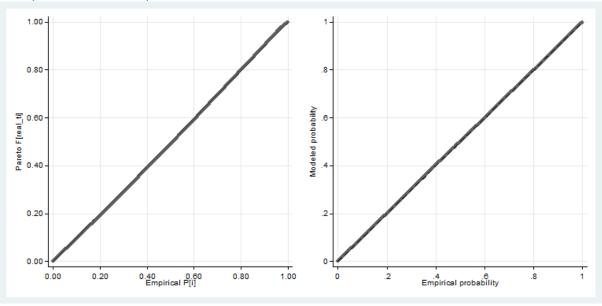
1999, threshold = £60,000



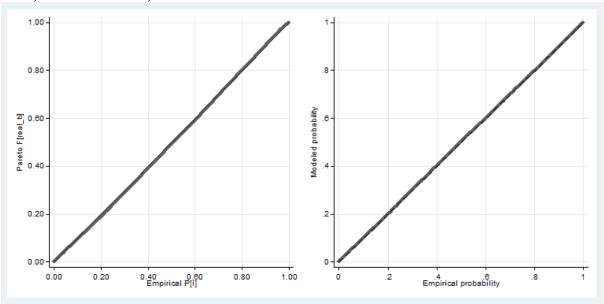


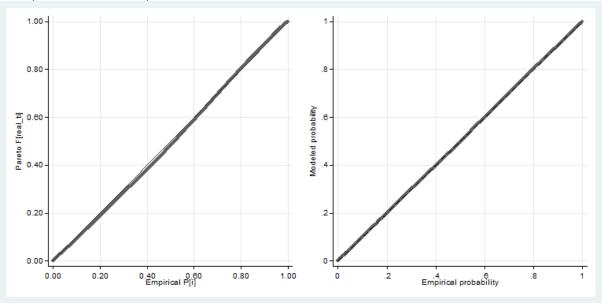
2001, threshold = £60,000



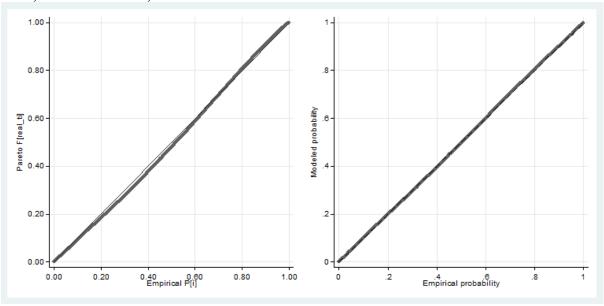


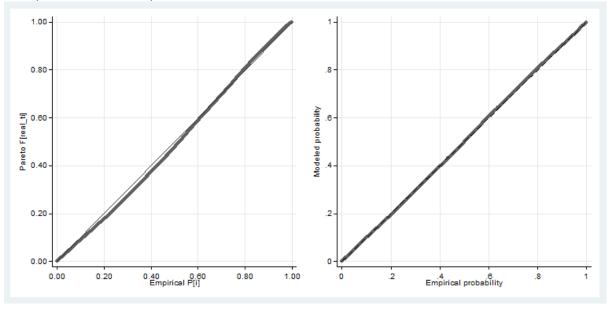
2003, threshold = £60,000



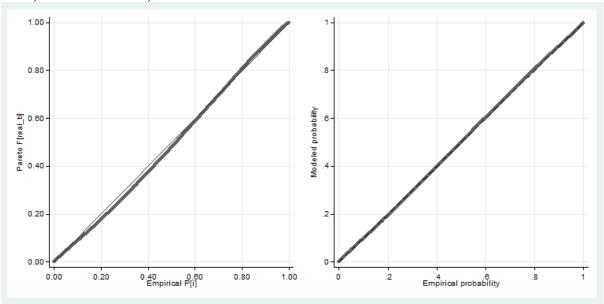


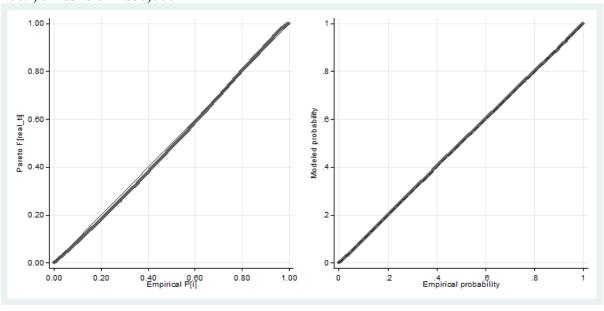
2005, threshold = £60,000

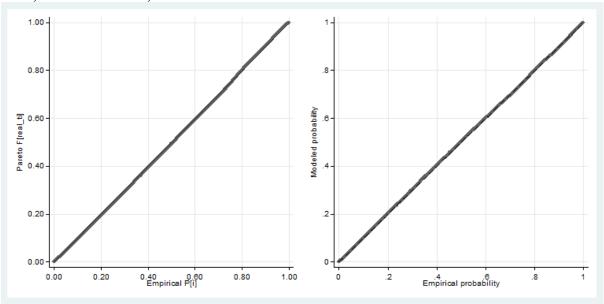




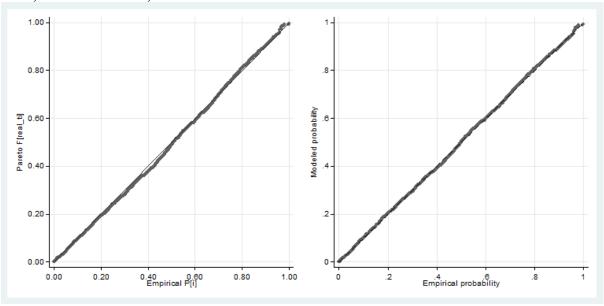
2007, threshold = £60,000

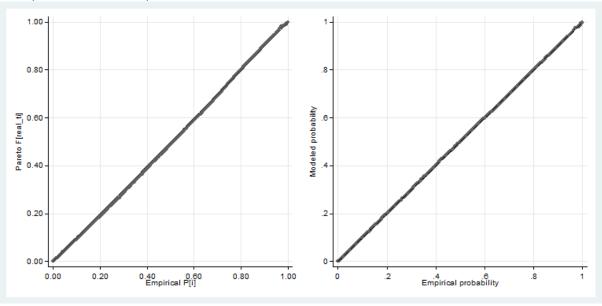




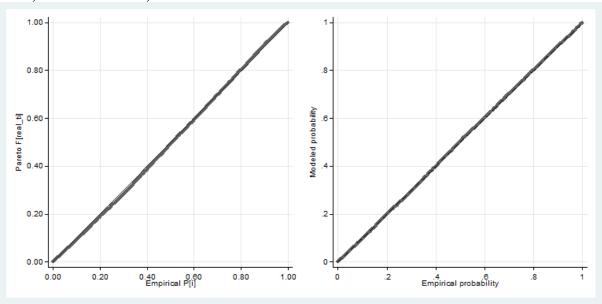


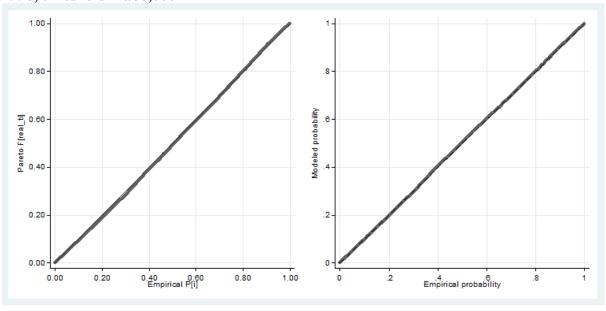
1995, threshold = £80,000



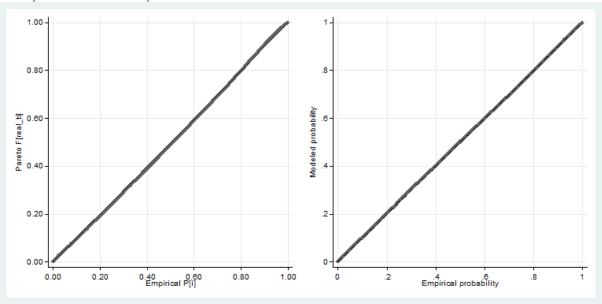


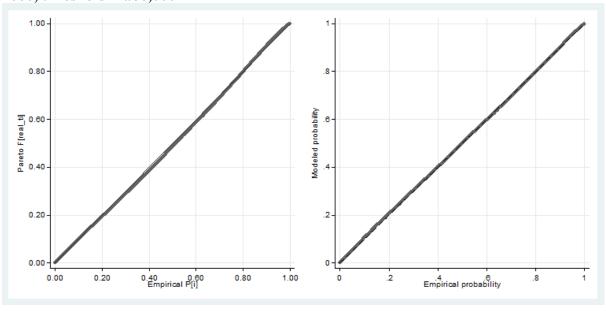
1997, threshold = £80,000



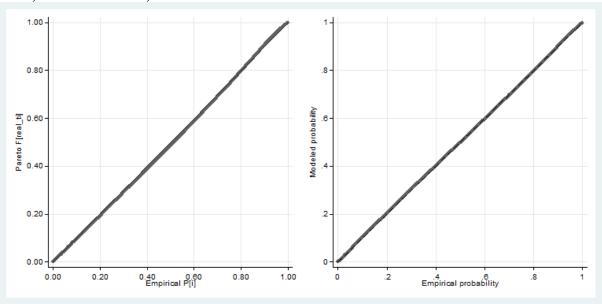


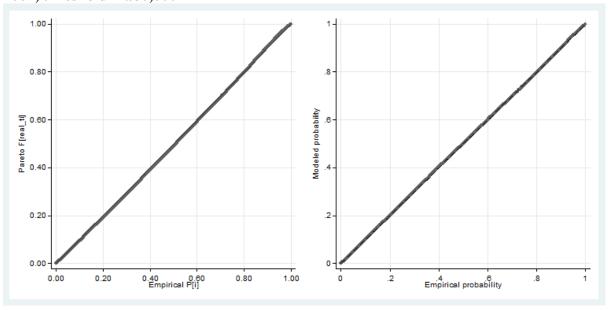
1999, threshold = £80,000



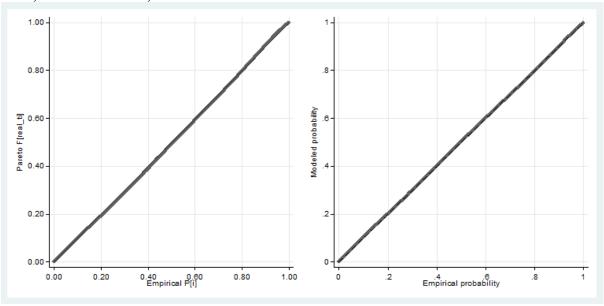


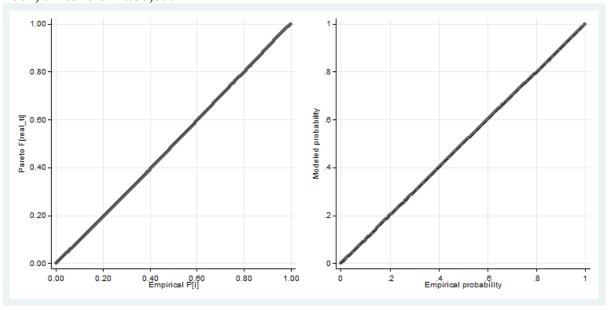
2001, threshold = £80,000



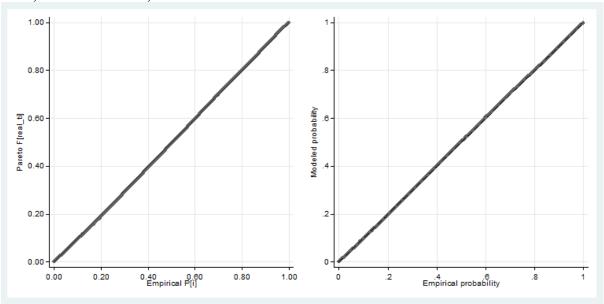


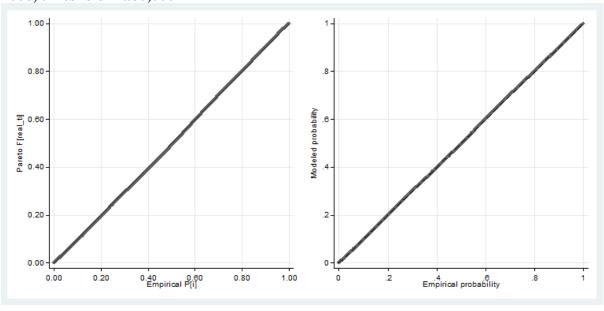
2003, threshold = £80,000



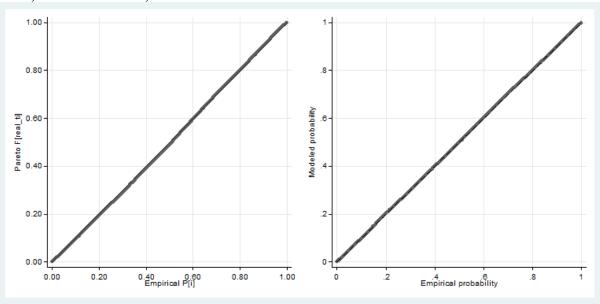


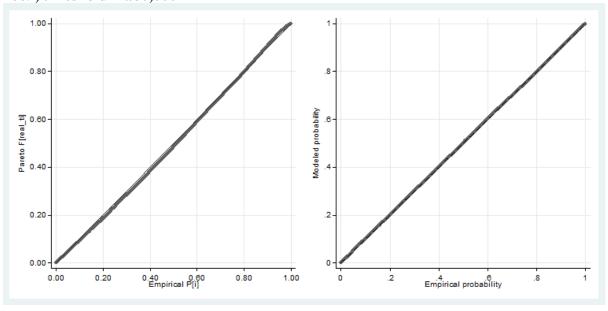
2005, threshold = £80,000

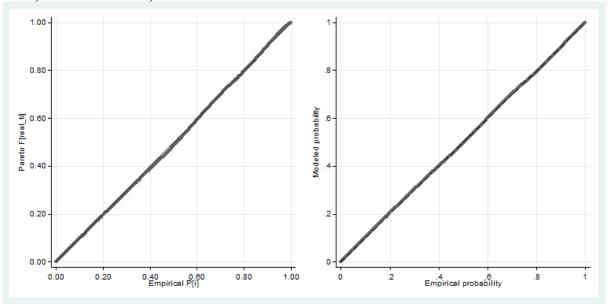




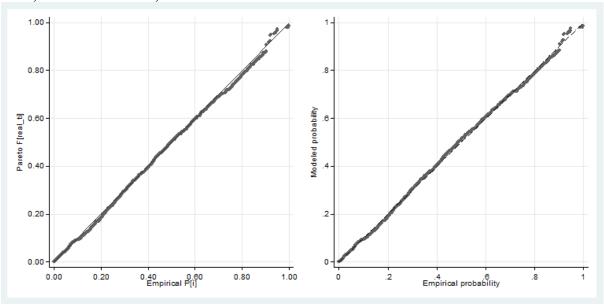
2007, threshold = £80,000

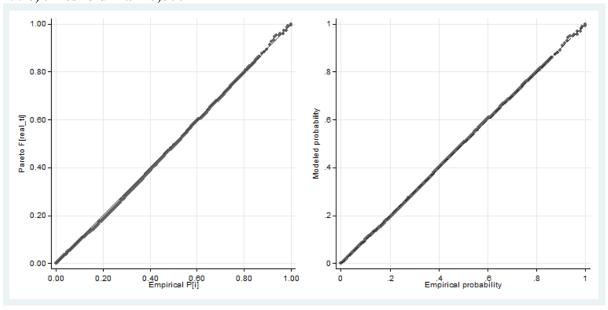




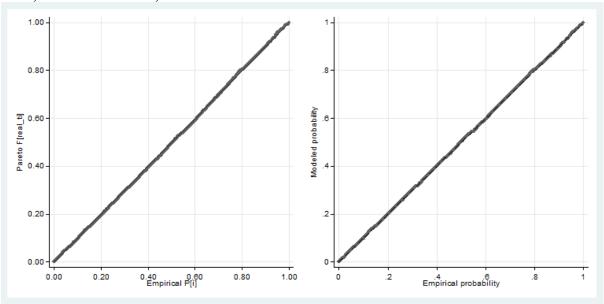


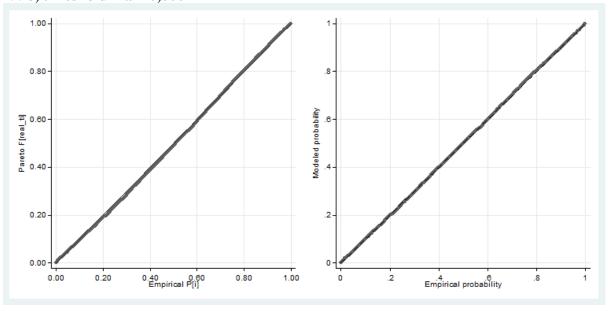
1995, threshold = £120,000



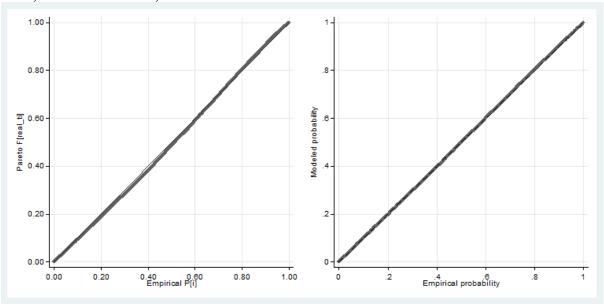


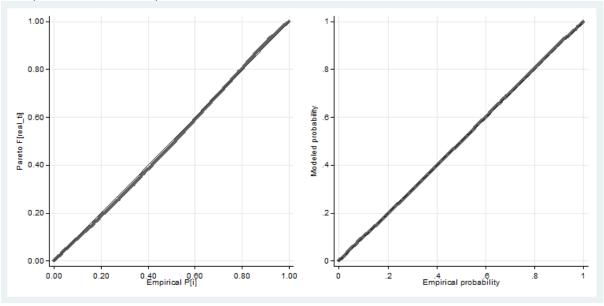
1997, threshold = £120,000



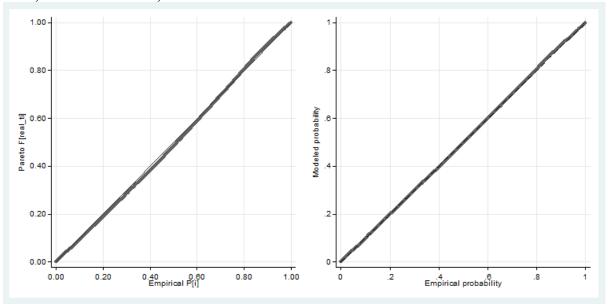


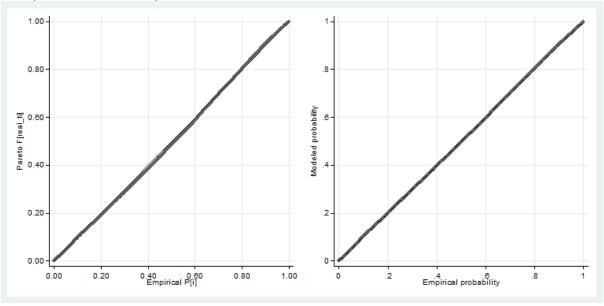
1999, threshold = £120,000



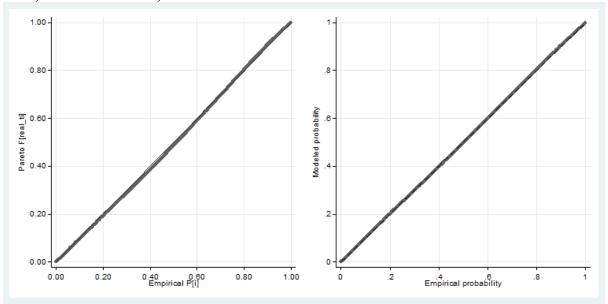


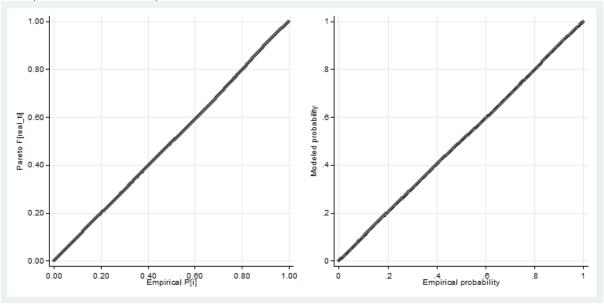
2001, threshold = £120,000



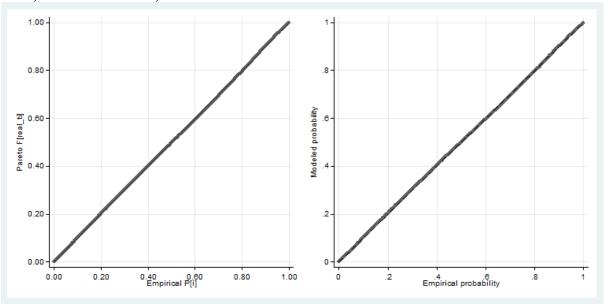


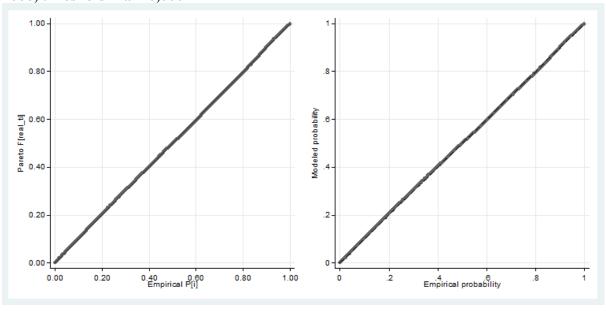
2003, threshold = £120,000



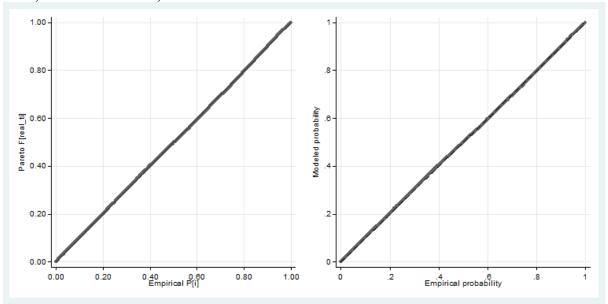


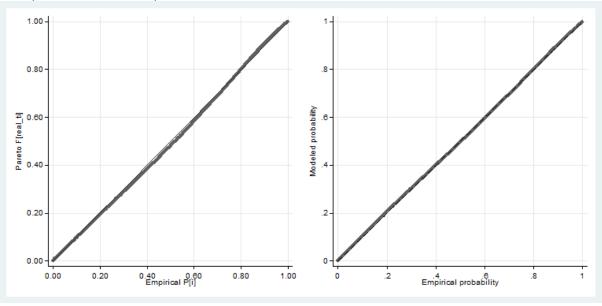
2005, threshold = £120,000

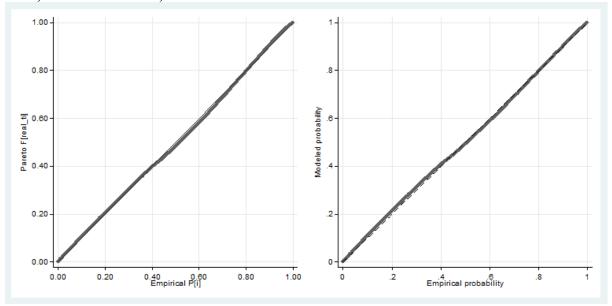




2007, threshold = £120,000



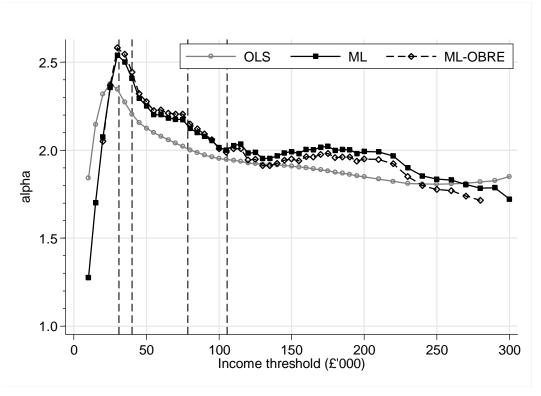


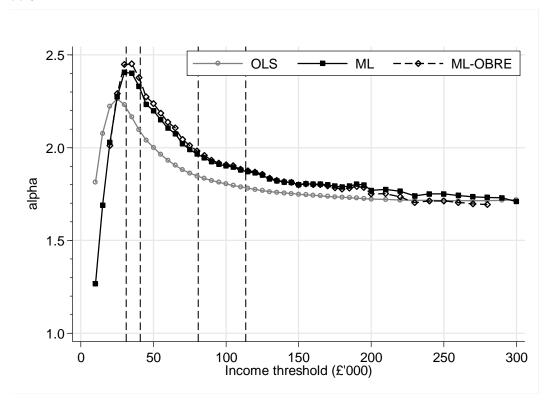


Vertical dashed lines show (from left to right): p90, p95, p99, and p99.5 (pareto10, 12, 13)

Pareto I

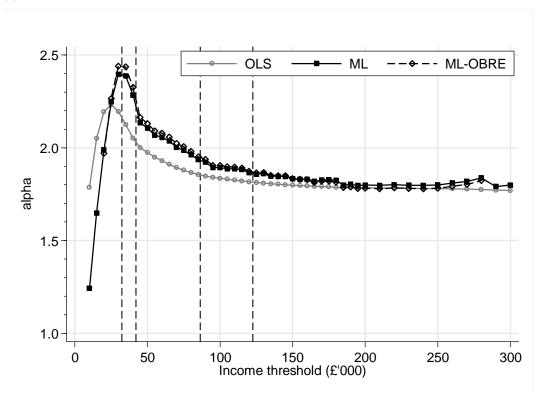
1995

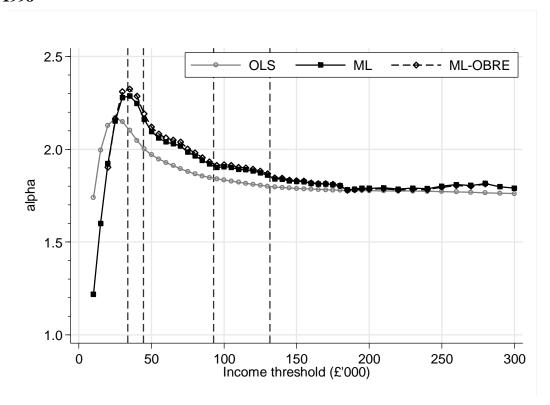




Vertical dashed lines show (from left to right): p90, p95, p99, and p99.5 (pareto10, 12, 13)

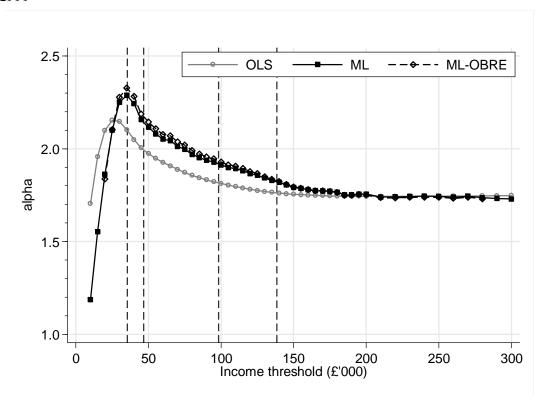
1997

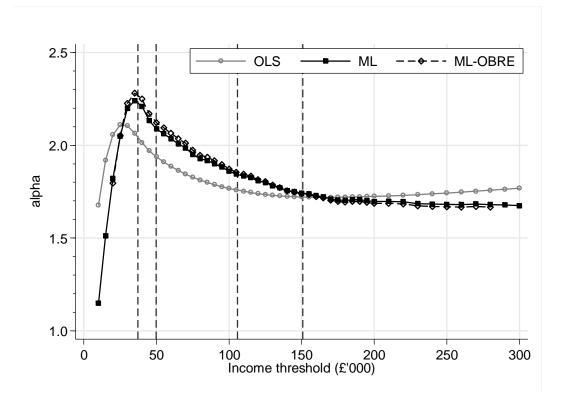




Vertical dashed lines show (from left to right): p90, p95, p99, and p99.5 (pareto10, 12, 13)

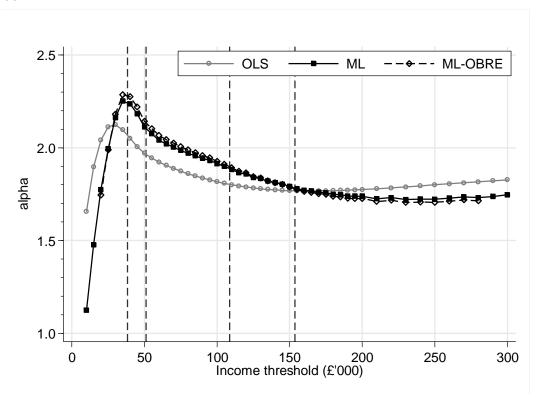
1999

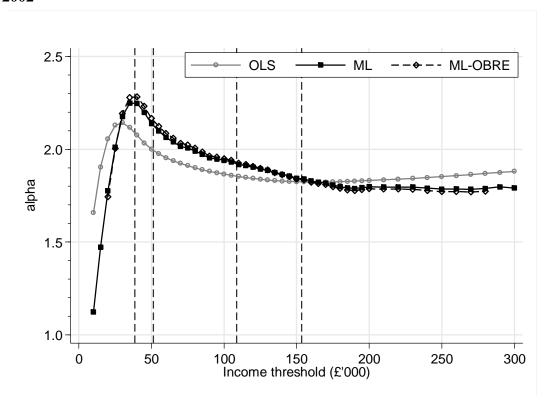




Vertical dashed lines show (from left to right): p90, p95, p99, and p99.5 (pareto10, 12, 13)

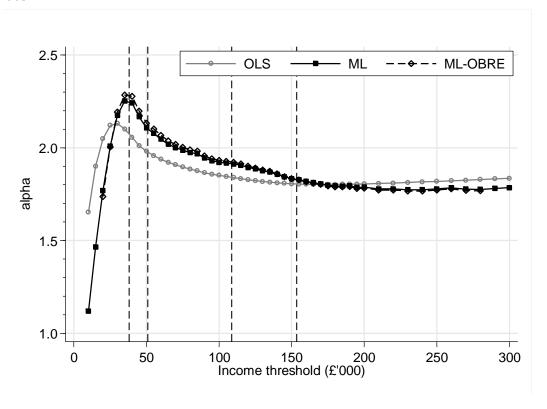
2001

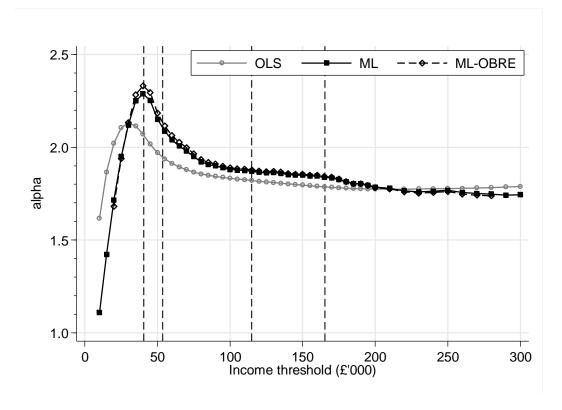




Vertical dashed lines show (from left to right): p90, p95, p99, and p99.5 (pareto10, 12, 13)

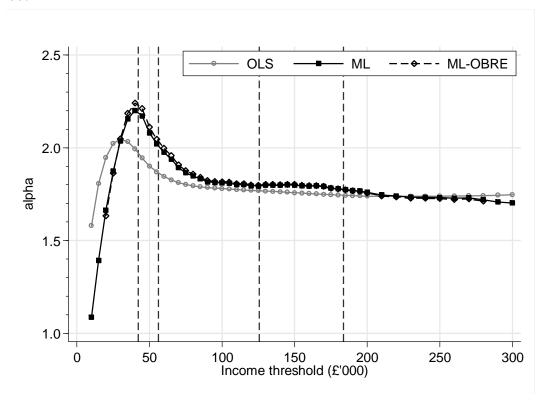
2003

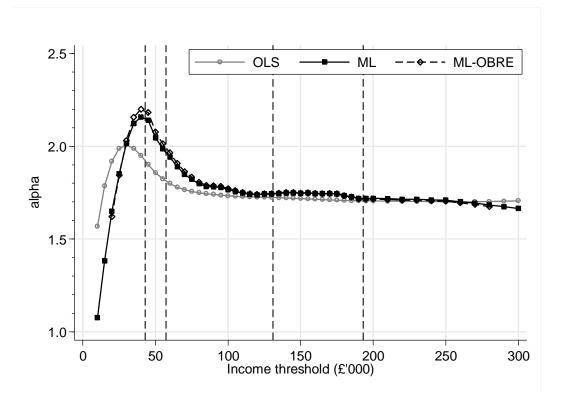




Vertical dashed lines show (from left to right): p90, p95, p99, and p99.5 (pareto10, 12, 13)

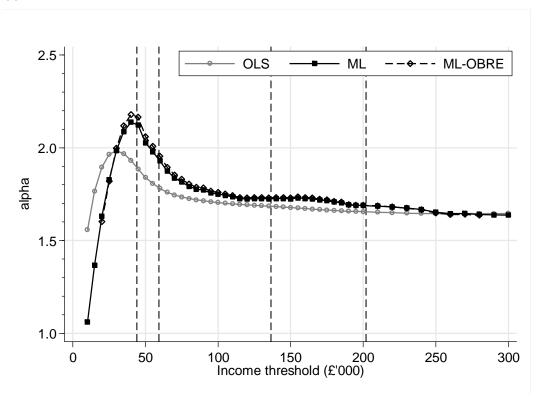
2005

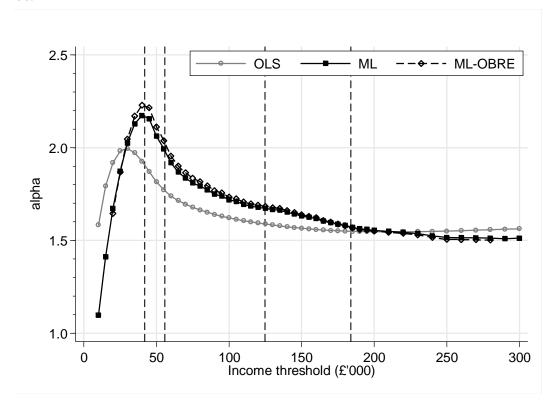




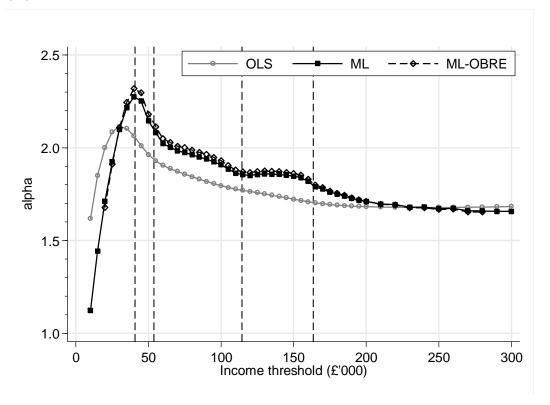
Vertical dashed lines show (from left to right): p90, p95, p99, and p99.5 (pareto10, 12, 13)

2007



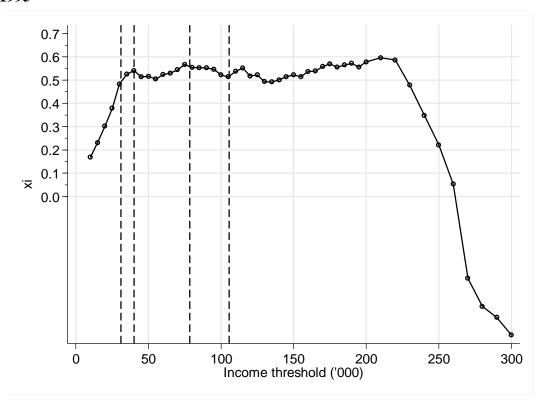


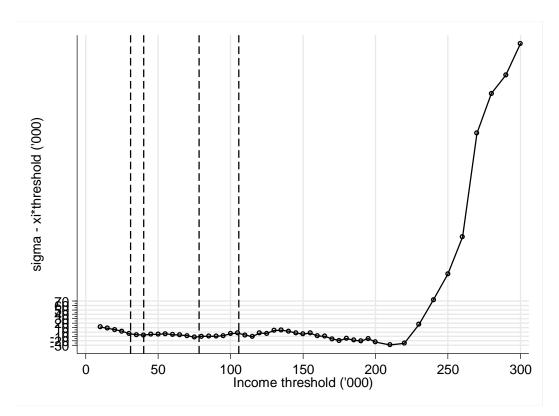
Estimates of Pareto I and II parameters, by estimator, threshold, and year Vertical dashed lines show (from left to right): p90, p95, p99, and p99.5 (pareto10, 12, 13)



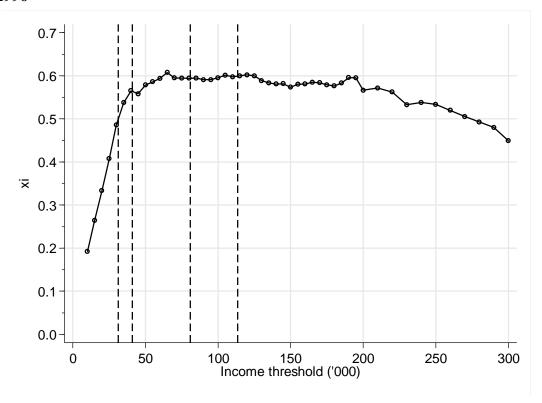
Vertical dashed lines show (from left to right): p90, p95, p99, and p99.5 (pareto10, 12, 13)

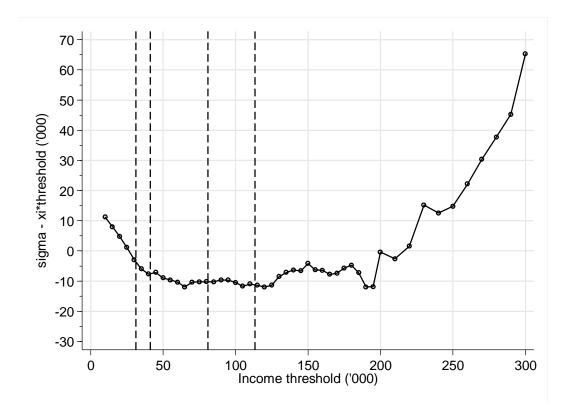
Pareto II (Generalized Pareto)



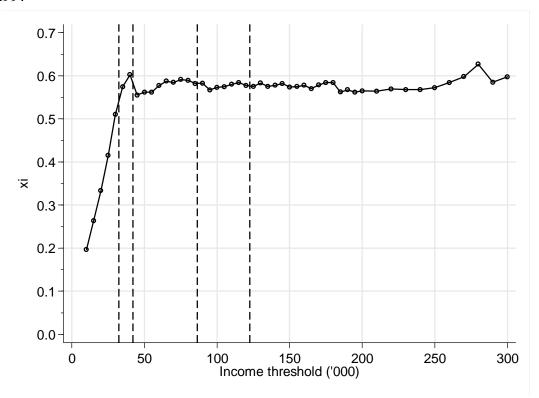


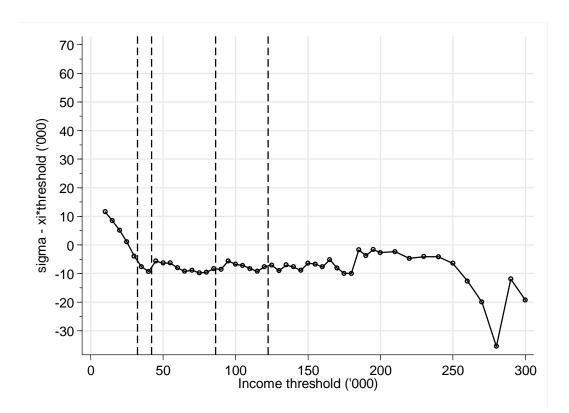
Vertical dashed lines show (from left to right): p90, p95, p99, and p99.5 (pareto10, 12, 13)



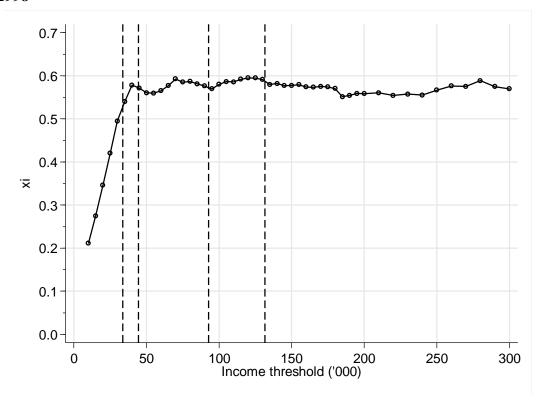


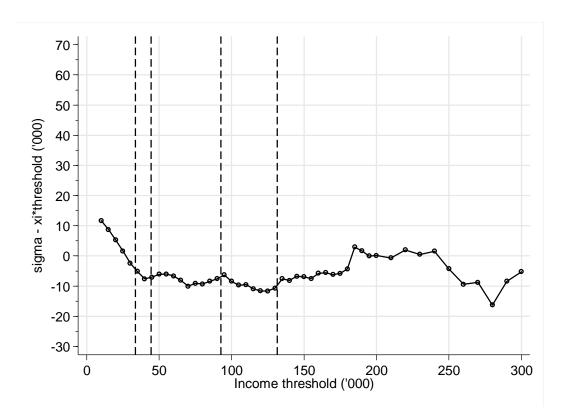
Vertical dashed lines show (from left to right): p90, p95, p99, and p99.5 (pareto10, 12, 13)



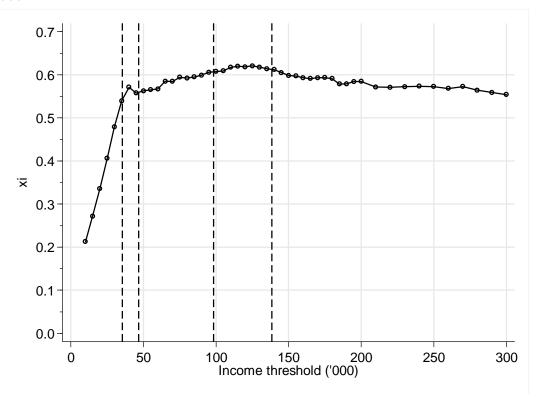


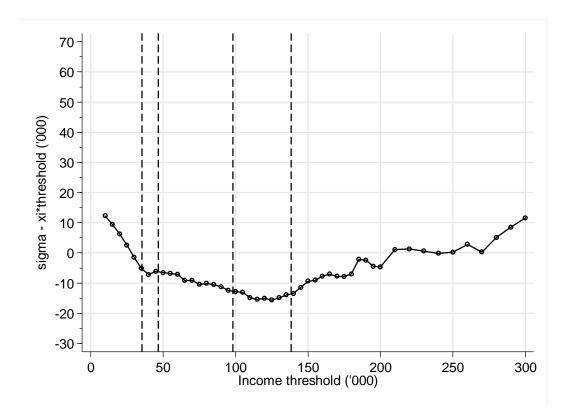
Vertical dashed lines show (from left to right): p90, p95, p99, and p99.5 (pareto10, 12, 13)



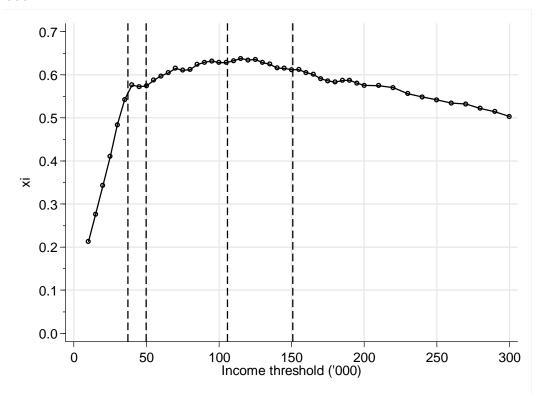


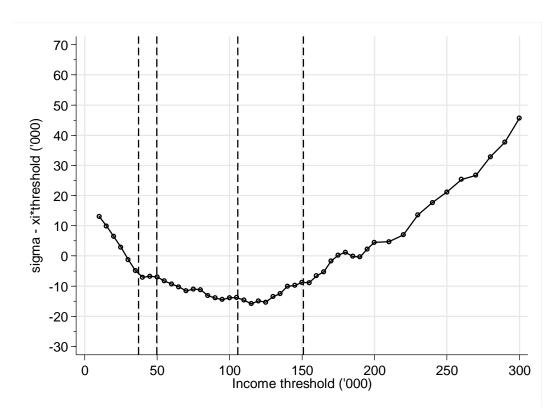
Vertical dashed lines show (from left to right): p90, p95, p99, and p99.5 (pareto10, 12, 13)



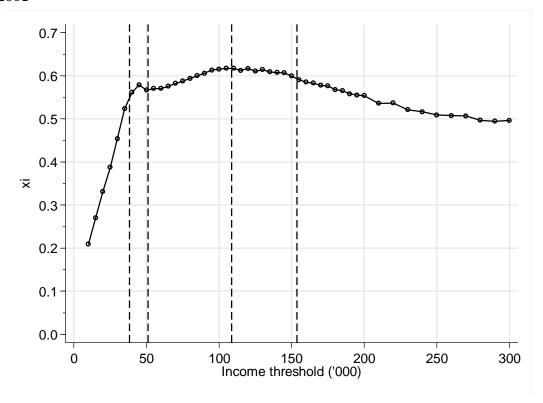


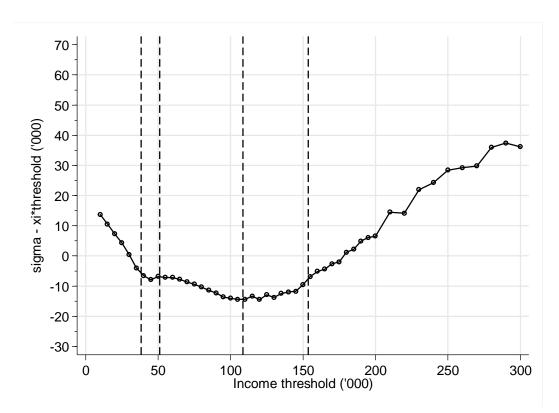
Vertical dashed lines show (from left to right): p90, p95, p99, and p99.5 (pareto10, 12, 13)



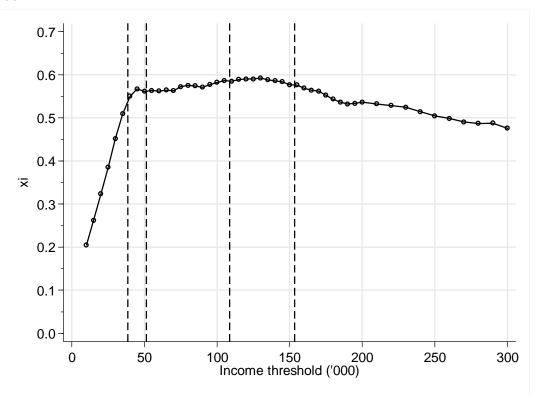


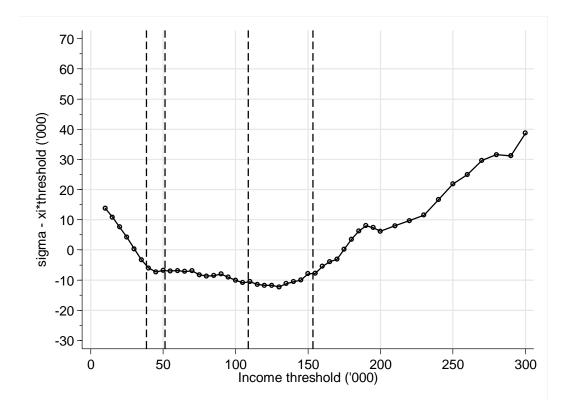
Vertical dashed lines show (from left to right): p90, p95, p99, and p99.5 (pareto10, 12, 13)



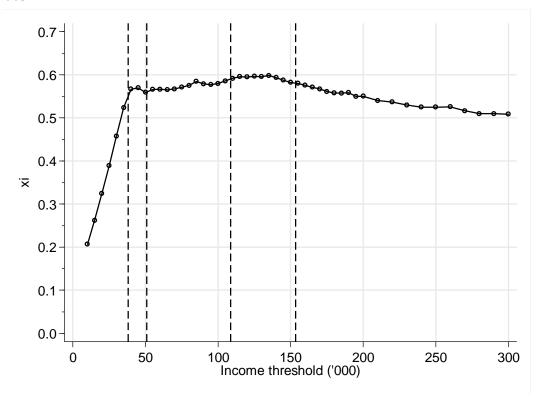


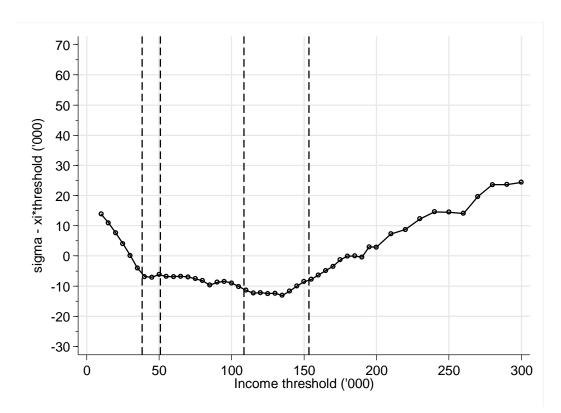
Vertical dashed lines show (from left to right): p90, p95, p99, and p99.5 (pareto10, 12, 13)



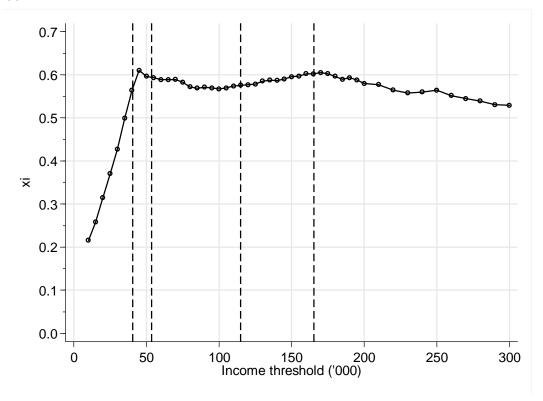


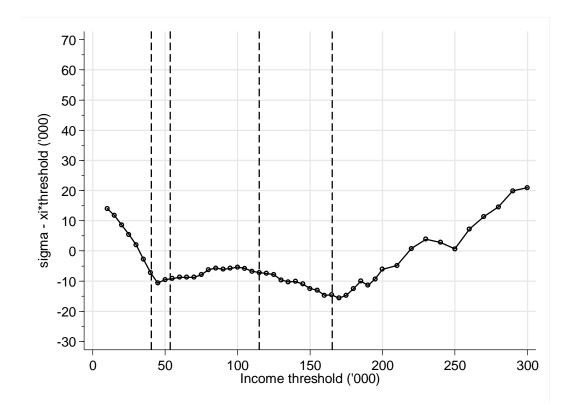
Vertical dashed lines show (from left to right): p90, p95, p99, and p99.5 (pareto10, 12, 13)



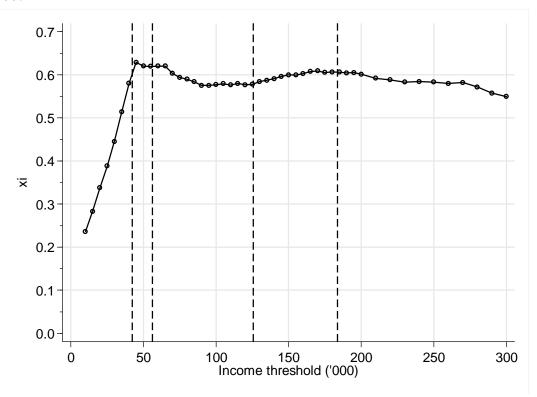


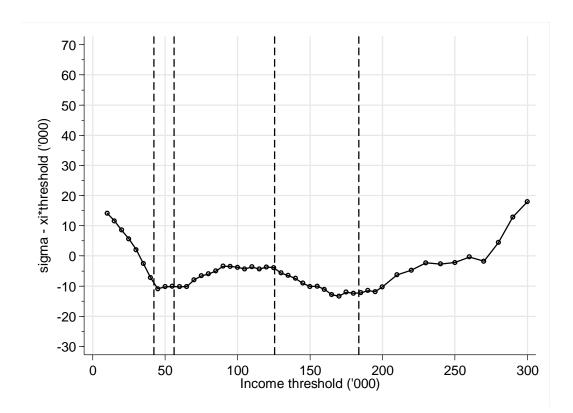
Vertical dashed lines show (from left to right): p90, p95, p99, and p99.5 (pareto10, 12, 13)



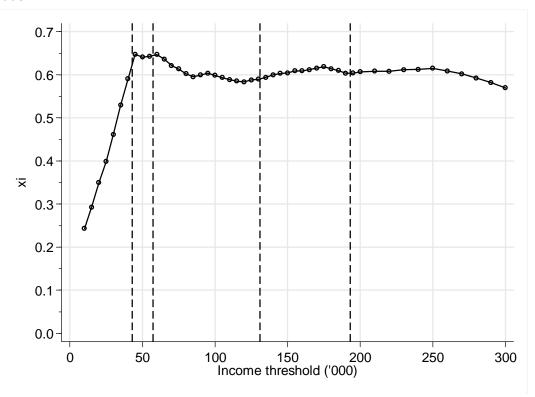


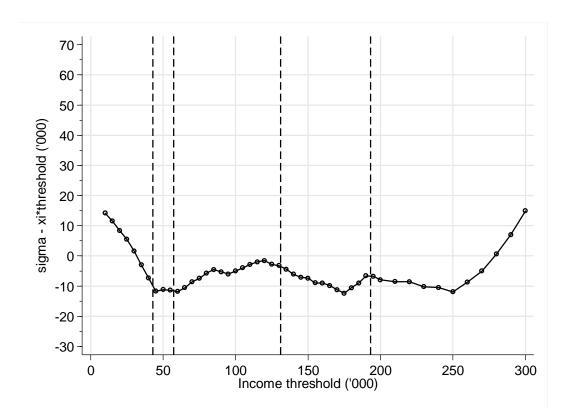
Vertical dashed lines show (from left to right): p90, p95, p99, and p99.5 (pareto10, 12, 13)



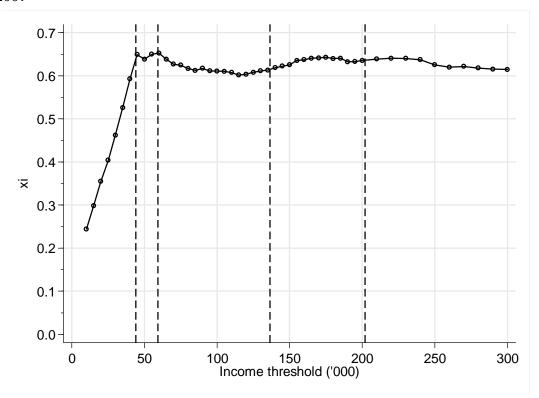


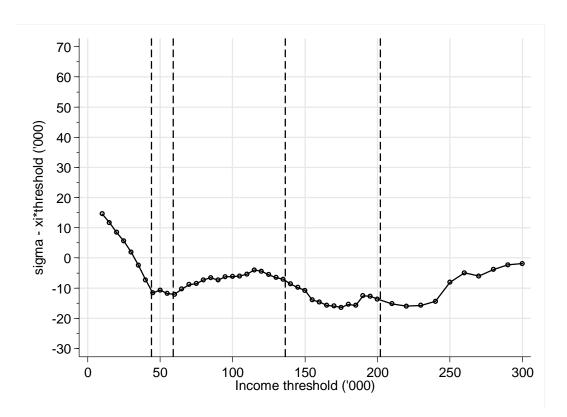
Vertical dashed lines show (from left to right): p90, p95, p99, and p99.5 (pareto10, 12, 13)



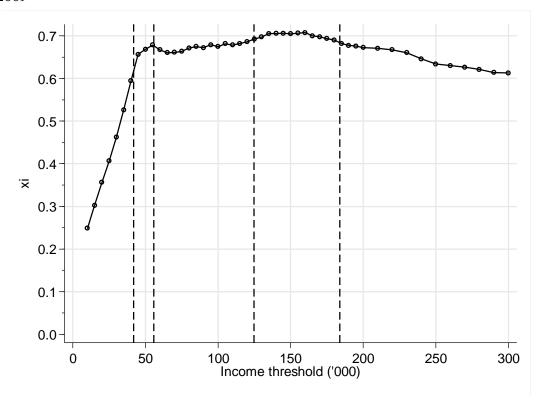


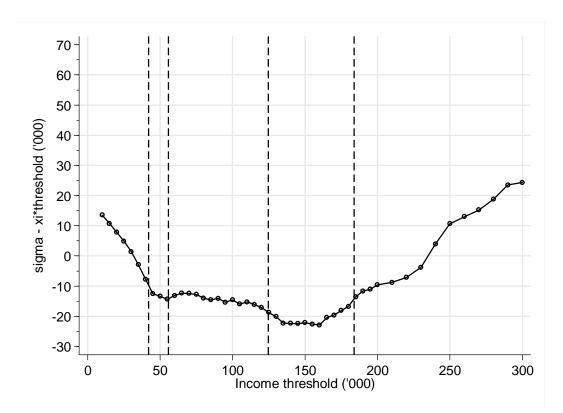
Vertical dashed lines show (from left to right): p90, p95, p99, and p99.5 (pareto10, 12, 13)



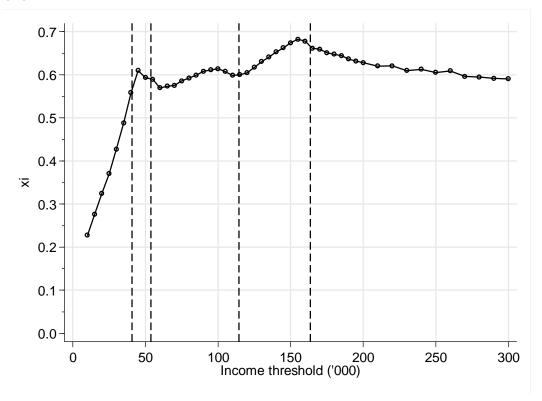


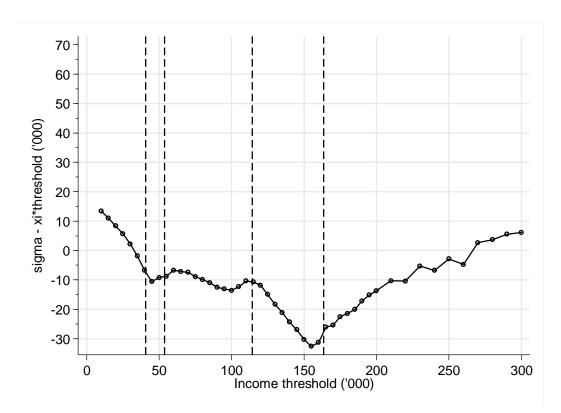
Vertical dashed lines show (from left to right): p90, p95, p99, and p99.5 (pareto10, 12, 13)





Vertical dashed lines show (from left to right): p90, p95, p99, and p99.5 (pareto10, 12, 13)





Here follow:

- (1) Tax data estimates
- (2) Survey data estimates
- (3) Combined data estimates
- (3a) Combined data estimates: figures (in same format as Figure 10)

Statistics derived from tax return data (SPI) can be identified by their suffixes:

"ml": Pareto I, ML estimator

"mlo": Pareto I, ML-OBRE estimator

"gpd": Pareto II, ML estimator

"np": non-parametric estimator

Estimates derived from the survey data (HBAI, non-SPI-adjusted), all non-parametric, can be identified by their suffixes:

"100": poorest 100%
"99": poorest 99%
"95": poorest 95%
"90": poorest 90%

TAX DATA ESTIMATES

Tax data: Pareto I and Pareto II models: estimates of parameter and SEs (threshold = p99 in the survey)

year	P_R	alpha_ml	se_alph~l	alpha	se_alpha	Хĺ	se_xi	sig	se_sig
1995	.0085792	2.114052	.1610938	2.13713	.0302296	.5578981	.1210882	36159.08	1580.968
1996	.008958	1.941077	.1106777	1.953106	.0237158	.5911263	.0878998	40597.05	1630.992
1997	.0092068	1.922345	.0644815	1.937097	.0144499	.5825368	.0542783	43944.39	1339.272
1998	.0093161	1.901082	.0444537	1.911827	.01212	.5701846	.0426144	48218.54	962.4487
1999	.0104736	1.926562	.0385267	1.94353	.010403	.6076952	.0352471	45540.21	707.3513
2000	.0098838	1.841782	.0368198	1.851902	.0101842	.6300222	.033269	52864.86	826.1099
2001	.0105668	1.895889	.0327147	1.906846	.0096336	.6161801	.0292421	50943.27	757.7493
2002	.0110572	1.934508	.032749	1.943498	.0097998	.5852064	.0293267	49929.41	664.6404
2003	.011684	1.919675	.0308324	1.929457	.0093381	.5791096	.0284916	49280.36	638.3967
2004	.0113858	1.877548	.0352881	1.885559	.0088971	.5731952	.0337069	54887.98	737.5891
2005	.0131511	1.806126	.0332827	1.811509	.0083703	.5794456	.0327035	58364.29	747.9828
2006	.0136039	1.747885	.0292037	1.751142	.0077817	.588789	.0292206	61837.9	722.4963
2007	.0142837	1.733676	.0283335	1.740903	.0073744	.6068791	.0275526	62273.52	689.8105
2009	.0118367	1.687349	.0262883	1.699297	.0074722	.6794235	.0278293	61522.91	673.331
2010	.0114712	1.874162	.0096601	1.892035	.0079147	.6023272	.0087243	53142	425.3513

Tax data: Pareto I and Pareto II models: estimates of parameter and SEs (threshold = p95 in the survey)

year	P_R	alpha_ml	se_alph~l	alpha	se_alpha	xi	se_xi	sig	se_sig
1995	.0349138	2.279984	.0662971	2.304698	.0192333	.5070741	.0567215	18653.35	562.1927
1996	.0341588	2.212221	.0543265	2.251051	.016354	.5660636	.044089	19138.83	385.5171
1997	.0359085	2.111353	.0303254	2.136568	.0117075	.5546948	.0263121	20964.23	358.2605
1998	.0370005	2.092855	.0208853	2.117316	.0095908	.5605036	.0192076	22168.79	321.0485
1999	.0408321	2.105451	.0185803	2.134624	.0083306	.5618327	.0165027	22191.23	288.6397
2000	.0434905	2.076405	.0172942	2.109816	.0079736	.5853383	.0151656	22965.56	269.4211
2001	.0428005	2.079124	.0145701	2.1075	.0069765	.5715815	.0135066	23987.99	222.5532
2002	.0436872	2.101361	.0141596	2.12654	.0068907	.5617445	.0134007	23712.9	195.8426
2003	.0424477	2.078119	.013984	2.102025	.0067782	.5645915	.0135475	24147.96	197.6735
2004	.045103	2.078425	.01557	2.104867	.0059277	.5925306	.0149922	23962.17	196.6042
2005	.0500392	2.010589	.0154738	2.035572	.0055749	.6206832	.0151286	24598.67	198.8592
2006	.0525945	1.975508	.0140596	2.00178	.0051725	.6439652	.0136899	24629.75	184.4339
2007	.0564673	1.968754	.0136294	1.997438	.0049032	.6514286	.0131492	24522.2	175.9459
2009	.0477972	1.967872	.0131282	2.009235	.0056849	.6783192	.0127761	24192.06	209.7331
2010	.0485559	2.095737	.0061848	2.128459	.0057145	.5953258	.0046749	22974	139.5351

Tax data: Pareto I and Pareto II models: estimates of parameter and SEs (threshold = p90 in the survey)

year	P_R	alpha_ml	se_alph~l	alpha	se_alpha	xi	se_xi	sig	se_sig
1995	.0691512	2.485901	.0476557	2.528681	.0177262	.5234771	.0362594	12615.95	302.6853
1996	.0656919	2.389046	.0402604	2.440527	.0152448	.5588147	.0303443	13397.08	278.5533
1997	.0704028	2.361521	.0267146	2.410876	.0114455	.6046395	.0186198	13070.18	259.8923
1998	.0736046	2.280277	.0186757	2.320734	.0092436	.5776901	.0134352	14533.85	236.7898
1999	.0784177	2.262013	.0165632	2.301965	.0080251	.5720381	.0121477	15101.62	225.8878
2000	.0825183	2.205624	.0144234	2.246422	.0076205	.577918	.0111061	16094.19	203.4729
2001	.0813434	2.223621	.0125648	2.262344	.0064534	.5728109	.0095682	16575.5	174.8562
2002	.0842385	2.235875	.0108814	2.270374	.0061525	.5555899	.0089394	16546.56	131.9748
2003	.0798965	2.221256	.0108645	2.256219	.0060503	.5750315	.0091686	16594.54	132.5893
2004	.0898392	2.278487	.0116492	2.322265	.0052906	.5893388	.0094923	15934.14	115.237
2005	.0972577	2.196848	.0115848	2.238672	.0049804	.6120697	.0098175	16503.35	117.6843
2006	.0975634	2.152272	.0108552	2.194793	.0046516	.6301144	.0092303	16940.74	114.365
2007	.1064382	2.131012	.0102924	2.173568	.0044181	.6218958	.0088186	17108.16	109.6708
2009	.0966601	2.179464	.0096267	2.238696	.0050993	.6327745	.0080159	16274.68	105.4642
2010	.0979533	2.2774	.0054083	2.321593	.0050355	.5717461	.003275	15703.49	77.03366

Tax data: Pareto model and non-parametric estimates of mean among the richest $100*P_R$ % and their income share (threshold = p99 in the survey) [NB income shares of Rich depend on P_R and survey estimates of the mean of non-Rich, shown later in appendix]

year	P_R	mean_mlo	mean_gpd	mean_np	se_mean~o	se_mean~d	se_mean~p	S_R_mlo	S_R_gpd	S_R_np
1995	.0085792	156670.8	165150.9	158323.1	1948.854	21064.17	13025.7	7.607906	7.986809	7.681977

1996	.008958	174471.5	184431.2	179533.8	2222.78	20465.06	14000.19	8.404487	8.841833	8.627304
1997	.0092068	186030.3	195260	190278.6	1480.853	12709.63	9183.695	9.008408	9.413278	9.19521
1998	.0093161	200975.8	208037.8	207181	1397.287	10000.22	9597.822	9.48213	9.782721	9.746362
1999	.0104736	197855.3	212137	207898.1	1122.426	9530.946	8189.784	10.07361	10.72278	10.53109
2000	.0098838	231325.4	249299.6	237453.9	1493.285	12061.17	8091.73	10.61583	11.34709	10.86651
2001	.0105668	222344.8	238468.4	228594.3	1238.702	9327.533	6884.204	10.61446	11.29723	10.88035
2002	.0110572	213263.7	223903.5	217793.3	1139.751	7795.354	6100.091	10.70578	11.18018	10.90836
2003	.011684	208325	217440.2	213571	1084.766	7202.349	6287.896	10.85227	11.27357	11.09523
2004	.0113858	228608.5	235968.9	233074.8	1218.097	9291.77	8131.193	11.30617	11.62786	11.50165
2005	.0131511	241493.3	246962.1	243684	1375.028	10001.14	8211.785	13.46539	13.72846	13.57096
2006	.013604	256232.9	260289.5	256858.2	1515.886	10018.38	8300.686	14.53834	14.73459	14.56865
2007	.0142837	261478.8	269689.7	266924.2	1494.96	10569.23	8455.183	15.45302	15.86131	15.72423
2009	.0118367	275611.5	305333.4	289375.5	1733.068	15692.08	10813.05	13.62552	14.8763	14.20928
2010	.0114712	226552.6	240444.9	237673.2	1062.407	2490.087	3508.254	11.55242	12.17457	12.05115

Tax data: Pareto model and non-parametric estimates of mean among the richest $100*P_R$ % and their income share (threshold = p95 in the survey) [NB income shares of Rich depend on P_R and survey estimates of the mean of non-Rich, shown later in appendix]

year	P_R	mean_mlo	mean_gpd	mean_np	se_mean~o	se_mean~d	se_mean~p	S_R_mlo	S_R_gpd	S_R_np
1995	.0349137	80554.7	83444.33	82856.27	515.2545	3609.17	3581.2	16.58459	17.07791	16.97799
1996	.0341588	85688.55	91727.57	91568.84	497.6064	3932.708	4006.27	16.52408	17.48502	17.46004
1997	.0359085	90390.54	95162.36	95004.66	435.7874	2365.043	2557.139	17.83467	18.60106	18.57596
1998	.0370005	95669.81	100926.6	101244.9	387.8547	1800.121	2541.855	18.71842	19.54591	19.59548
1999	.0408321	96070.52	101710.2	102429.3	330.4416	1559.793	2213.287	19.74078	20.66021	20.77593
2000	.0434905	100847.3	108431.9	108048.9	343.4195	1694.147	1978.992	21.05144	22.28192	22.22069
2001	.0428005	104130.1	110712.6	110239.5	311.2445	1470.08	1805.728	20.81193	21.84023	21.76721
2002	.0436872	102690.8	108508.1	107818.8	295.374	1377.423	1643.956	20.99965	21.92839	21.81948
2003	.0424476	104229.2	110104.4	109622	304.9838	1438.175	1821.406	20.4253	21.33105	21.25746
2004	.045103	106393.3	114654.1	112948	271.1832	1838.786	2170.315	21.50003	22.78896	22.52624
2005	.0500392	110387.9	121008.3	117731.8	291.9376	2242.777	2291.413	24.0441	25.76145	25.23997
2006	.0525945	112101.7	125278.5	120702.1	289.148	2336.351	2275.275	25.20766	27.35999	26.62666
2007	.0564673	112157.6	126357.3	122341.9	276.0276	2344.964	2267.789	26.76992	29.17049	28.50776
2009	.0477972	113158.8	132044.5	127767	317.2386	2597.254	2797.313	23.48839	26.37457	25.7401
2010	.0485559	102564.4	111148.8	110504	244.0201	485.5498	856.3663	22.71786	24.1599	24.05346

Tax data: Pareto model and non-parametric estimates of mean among the richest $100*P_R$ % and their income share (threshold = p90 in the survey) [NB income shares of Rich depend on P_R and survey estimates of the mean of non-Rich, shown later in appendix]

year	P_R	mean_mlo	mean_gpd	mean_np	se_mean~o	se_mean~d	se_mean~p	S_R_mlo	S_R_gpd	S_R_np
1995	.0691512	58806.33	62025.57	61553.76	269.6673	1622.162	1868.256	24.89174	25.90144	25.75516
1996	.0656919	62732.61	67394.13	67497.27	272.0257	1732.144	2140.528	24.25465	25.59565	25.62478
1997	.0704028	63766.82	70376.04	68854.54	214.5684	1223.284	1347.415	25.69912	27.62687	27.192
1998	.0736046	67273.27	72700.43	72395.7	202.8829	808.5192	1306.276	27,12538	28.68594	28,60009

Approach C estimates, by threshold, with graphs of trends at the end (pareto 14); 1999 .0784177 69087.77 74362.52 74414.87 184.9931 727.389 1178.527 28.15536 2000 .0825183 72761.04 78501.73 78481.57 198.0265 756.7242 1068.388 29.65939 2001 .0813434 75009.84 80655.31 80370.66 169.5012 664.2412 974.1547 29.38112 2002 .0842385 73916.98 78592.4 78457.22 157.6766 590.5917 871.2386 29.93278 2003 .0798965 75311.94 80981.04 80350.22 160.7672 668.1057 985.3011 28.69084 2004 .0898392 74571.41 81261.06 80611.07 128.4845 734.7617 1108.295 30.74842

.0972577 77156.92 85233.45 84008.57 138.577 900.1124 1199.984 33.39111 35.64064 35.3093 2005 2006 .0975634 79604.52 89134.7 87512.29 141.2073 968.2331 1246.013 34.05813 36.64152 36.21612 2007 .1064382 79149.23 87981.98 87586.04 137.0898 894.8082 1222.138 36.25751 38.73636 38.62938 2009 .0966601 76925.5 86881.66 87701.7 141.4567 806.3739 1397.995 33.01443 35.75938 35.97547 2010 .0979533 72086.18 77704.49 78298.05 118.3061 200.5599 429.7935 32.74108 34.41469 34.58665

29.66726

31.26777

30.90894

31.23472

30.19834

32.60737

29.68194

31.26225

30.83349

31.19776

30.03375

32.43114

Tax data: Pareto model and non-parametric estimates: Gini among the richest 100*P_R %, SE(Gini); tax data (threshold = p99 in the survey)

```
gini_mlo
                   gini_gpd
                               gini np
                                         se_gini~o se_gini~d se_gini~p
year
1995
       .3054124
                   .3434142
                               .3144873
                                          .0056394
                                                      .0732738
                                                                 .0427343
       .3440906
                   .3821193
                               .3650996
                                          .0056158
                                                      .0599495
                                                                 .0411213
1996
       .3479235
                   .3803295
                               .3640029
                                          .0034983
                                                      .0354961
                                                                 .0261172
1997
1998
        .354151
                   .3771464
                               .3745846
                                          .0030403
                                                      .0266204
                                                                 .0262927
1999
       .3463731
                   .3930254
                               .380599
                                          .0024962
                                                      .0244879
                                                                 .0221673
                                          .0027862
2000
       .3698494
                   .4183659
                              .3891325
                                                                  .018145
                                                      .0251481
       .3554049
2001
                   .4022064
                               .3761665
                                          .0024337
                                                      .0209443
                                                                  .0166525
2002
       .3463809
                   .3799885
                               .3624798
                                          .0023516
                                                      .0191831
                                                                  .0157493
       .3497832
                   .3789697
                               .3676875
                                           .002285
2003
                                                      .0182886
                                                                  .0167222
2004
       .3608651
                   .3819696
                               .3742975
                                          .0023172
                                                      .0215185
                                                                  .0195203
2005
       .3812402
                   .3955823
                              .3874516
                                          .0024331
                                                      .0215328
                                                                  .0182169
2006
        .399635
                   .4093939
                               .4015009
                                          .0024856
                                                      .0199333
                                                                  .0171775
2007
       .4029322
                   .4216229
                              .4156713
                                          .0023945
                                                      .0198886
                                                                  .0164527
       .4169108
                   .4759566
                               .4469829
                                          .0025976
                                                      .0244471
                                                                  .018722
2009
2010
       .3591863
                   .3976407
                               .3906763
                                          .0020422
                                                      .0056809
                                                                  .0086046
```

Tax data: Pareto model and non-parametric estimates: Gini among the richest 100*P_R %, SE(Gini); tax data (threshold = p95 in the survey)

```
gini_mlo
                  gini_gpd
                               gini_np se_gini~o se_gini~d se_gini~p
year
       .2770547
                   .3037658
                              .2987593
                                          .0029527
                                                     .0272153
                                                                 .0271069
1995
       .2855428
                                          .0026668
1996
                   .3353189
                              .3342152
                                                     .0257469
                                                                 .0267482
1997
       .3055175
                   .3422907
                              .3412394
                                          .0021856
                                                     .0147889
                                                                 .0163554
       .3091542
1998
                   .3471917
                              .3492747
                                          .0018333
                                                     .0107062
                                                                 .015546
       .3058807
                   .3462314
                              .3508723
1999
                                          .0015589
                                                     .0092058
                                                                 .0133336
2000
       .3105944
                   .3610539
                              .3588559
                                          .0015384
                                                     .0091707
                                                                 .0110062
2001
       .3110419
                   .3540559
                              .3513153
                                          .0013499
                                                     .0078739
                                                                 .0100201
```

```
2002
       .3074009
                   .3467033
                               .3425396
                                           .0013023
                                                       .0076048
                                                                   .0094274
2003
        .312105
                   .3509152
                                .348074
                                           .0013205
                                                       .0077804
                                                                    .010253
2004
       .3115523
                   .3644193
                               .3547632
                                           .0011507
                                                       .0093954
                                                                   .0117457
2005
       .3256116
                   .3885343
                               .3713869
                                           .0011821
                                                       .0104633
                                                                   .0115079
2006
       .3329382
                   .4072108
                                .384547
                                           .0011467
                                                       .0102371
                                                                   .0109423
2007
       .3339036
                   .4128501
                               .3934216
                                           .0010933
                                                        .010094
                                                                   .0106184
       .3312938
                    .430923
                               .4117908
                                           .0012479
                                                       .0105271
                                                                   .0123294
2009
2010
       .3070388
                   .3636219
                               .3598456
                                           .0010774
                                                       .0026348
                                                                   .0048076
```

Tax data: Pareto model and non-parametric estimates: Gini among the richest $100*P_R \%$, SE(Gini); tax data (threshold = p90 in the survey)

```
gini mlo
                   gini gpd
                                gini np
                                          se gini~o
                                                     se gini~d se gini~p
year
       .2464656
                   .2890843
                                           .0021536
                                                                   .0201293
1995
                               .2836135
                                                       .0170911
                                .313723
1996
        .257662
                   .3126413
                                           .0020242
                                                       .0162325
                                                                   .0204607
1997
       .2616601
                   .3366484
                               .3218432
                                           .0015673
                                                       .0108702
                                                                   .0124256
1998
       .2746145
                   .3328262
                               .3299924
                                           .0013942
                                                       .0070237
                                                                   .0115752
1999
        .2774748
                   .3323129
                               .3327698
                                           .0012357
                                                       .0062016
                                                                   .0101002
        .2862997
                   .3415607
                               .3414138
                                           .0012493
                                                       .0059803
                                                                   .0084948
2000
2001
        .283713
                   .3370788
                               .3347417
                                           .0010389
                                                       .0051123
                                                                   .0076662
2002
       .2824262
                   .3279836
                               .3268512
                                           .0009815
                                                       .0046838
                                                                   .0071255
       .2847025
                   .3383912
                               .3331644
2003
                                           .0009808
                                                       .0050997
                                                                   .0078365
2004
       .2743838
                   .3384849
                               .3331642
                                           .0007966
                                                       .0055726
                                                                   .0088229
2005
       .2875758
                   .3596169
                               .3502815
                                           .0008238
                                                       .0063067
                                                                   .0088905
       .2950213
2006
                    .375088
                               .3635042
                                           .0008097
                                                       .0063374
                                                                   .0086909
2007
       .2987629
                   .3731775
                               .3704197
                                           .0007887
                                                       .0059282
                                                                   .0084355
2009
        .2875718
                   .3730876
                                .379119
                                           .0008434
                                                        .005465
                                                                   .0096246
2010
        .274485
                   .3304022
                               .3355382
                                           .0007588
                                                       .0016115
                                                                   .0035431
```

Tax data: Pareto model and non-parametric estimates: MLD among the richest $100*P_R %$, SE(MLD); tax data (threshold = p99 in the survey)

```
year
        ge0_mlo
                    ge0_gpd
                                 ge0_np
                                          se_ge0_~o se_ge0_~d se_ge0_np
1995
        .1630389
                    .217282
                               .1684216
                                           .0058205
                                                                   .0469774
1996
        .2054452
                   .2691835
                               .2308747
                                            .006523
                                                                   .0528787
1997
        .2099224
                    .266396
                               .2285402
                                           .0041094
                                                                   .0337731
        .2173044
                   .2614269
                               .2447563
1998
                                           .0036366
                                                                    .036755
1999
       .2081053
                   .2893426
                                .253087
                                           .0029189
                                                                   .0313797
2000
       .2365117
                   .3329697
                               .2596926
                                           .0034858
                                                                   .0253388
       .2188069
2001
                   .3065211
                               .2434956
                                           .0029216
                                                                   .0229737
       .2081145
                   .2697532
2002
                               .2267408
                                           .0027499
                                                                   .0209576
                                           .0026987
2003
       .2121128
                    .266479
                               .2343417
                                                                   .0227853
2004
       .2254138
                   .2710199
                               .2424991
                                           .0028259
                                                                   .0268511
```

```
2005
       .2509941
                   .2907401
                              .2583794
                                          .0031432
                                                                  .0255687
2006
       .2753729
                   .3127077
                              .2767462
                                          .0033784
                                                                  .0251991
2007
       .2798748
                   .3350168
                              .2980914
                                          .0032841
                                                                  .0249359
2009
       .2994156
                   .4419066
                              .3439819
                                          .0037004
                                                                  .0307121
2010
       .2233713
                    .297654
                              .2662505
                                          .0024785
                                                                  .0132066
```

Tax data: Pareto model and non-parametric estimates: MLD among the richest $100*P_R %$, SE(MLD); tax data (threshold = p95 in the survey)

```
ge0 mlo
                    ge0 gpd
                                ge0 np
                                         se qe0 ~o se qe0 ~d se qe0 np
year
       .1350818
                    .166626
                               .1585496
                                          .0027753
1995
                                                                  .0311939
1996
       .1431763
                   .2058809
                              .2017504
                                          .0025798
                                                                  .034325
1997
       .1631473
                   .2114191
                               .2073442
                                          .0022565
                                                                  .0214905
1998
       .1669239
                   .2177577
                               .2180434
                                          .0019147
                                                                  .0217018
       .1635226
                   .2169992
                              .2211212
1999
                                          .0016113
                                                                  .0186683
2000
       .1684314
                   .2374165
                              .2297816
                                          .001614
                                                                  .0153269
2001
       .1689013
                   .2274825
                              .2194398
                                          .0014183
                                                                 .0138488
       .1650977
                    .217839
2002
                               .2081922
                                          .0013526
                                                                 .0127265
       .1700201
                   .2228814
                              .2149935
                                          .001392
2003
                                                                 .0141118
2004
       .1694379
                   .2428998
                              .2231789
                                          .0012109
                                                                  .0163757
2005
       .1845605
                   .2769366
                              .2428646
                                          .0012992
                                                                  .0164365
       .1927029
                   .3055029
2006
                              .2599788
                                          .0012885
                                                                  .0161618
2007
       .1937893
                   .3145581
                              .2734098
                                          .0012321
                                                                  .015991
2009
       .1908597
                   .3457932
                              .3018139
                                          .0013953
                                                                 .0195336
       .1647218
                   .2422952
2010
                               .2319466
                                          .0011178
                                                                  .0071567
```

Tax data: Pareto model and non-parametric estimates: MLD among the richest $100*P_R \%$, SE(MLD); tax data (threshold = p90 in the survey)

```
ge0 mlo
                    ge0 gpd
                                         se qe0 ~o se qe0 ~d se qe0 np
                                 qe0 np
year
1995
       .1078295
                   .1549367
                               .1466852
                                          .0018135
                                                                   .023404
1996
        .1174575
                   .1814751
                               .1818338
                                          .0017768
                                                                  .0260218
1997
       .1209924
                   .2128299
                               .1890867
                                          .0013957
                                                                   .016185
1998
        .1327977
                   .2044127
                               .1985364
                                          .0012995
                                                                  .0159264
1999
        .1354769
                   .2030479
                               .2020825
                                          .0011632
                                                                  .0139498
2000
       .1439094
                    .213646
                               .2113586
                                          .0012115
                                                                    .01171
       .1414117
                   .2082812
                               .2027446
2001
                                          .0009988
                                                                   .010496
       .1401772
                   .1963152
                               .192992
2002
                                          .0009396
                                                                  .0095672
       .1423646
2003
                   .2100056
                               .2001443
                                          .0009461
                                                                  .0107198
       .1325828
                               .2021878
2004
                   .2125305
                                          .0007419
                                                                   .012105
       .1451496
                   .2393892
                              .2217228
2005
                                          .0008023
                                                                  .0124923
2006
       .1524909
                   .2606301
                               .2381978
                                          .0008082
                                                                  .0125754
2007
       .1562483
                   .2566667
                               .2483471
                                          .0007969
                                                                  .0123932
```

```
    2009
    .1451457
    .2587453
    .2641096
    .0008214
    . 0146127

    2010
    .132677
    .2012096
    .2069788
    .0007069
    . 0051116
```

Tax data: Pareto model and non-parametric estimates: Theil among the richest $100*P_R \%$, SE(Theil); tax data (threshold = p99 in the survey)

year	gel_mlo	ge1_gpd	ge1_np	se_ge1_~o	se_ge1_~d	se_ge1_np
1995	.2484504		.2239827	.0109391		.0644242
1996	.3317514		.3732583	.0133669	•	.0899333
1997	.3409663		.357114	.0084946	•	.0632853
1998	.3563347		.415646	.0076248	•	.0905943
1999	.3372167		.4308738	.0060125	•	.0778595
2000	.3973471		.4109592	.0075776	•	.0543522
2001	.3594896		.3871077	.0061434	•	.0548116
2002	.3372355		.3577004	.0056644	•	.0505689
2003	.3455037		.3762938	.0056023	•	.0527927
2004	.3734696		.3923422	.0060169	•	.0605882
2005	.4292523		.4197822	.0070164	•	.0586319
2006	.4848777	•	.4596834	.0078761	•	.0660984
2007	.4954144		.5117994	.0077167	•	.0677345
2009	.5421128		.600757	.008992	•	.0874639
2010	.3691292		.4449106	.005257	•	.0414407

Tax data: Pareto model and non-parametric estimates: Theil among the richest $100*P_R \%$, SE(Theil); tax data (threshold = p95 in the survey)

```
gel_mlo
                   gel_gpd
                                gel_np se_gel_~o se_gel_~d se_gel_np
year
        .197483
                              .2302815
                                         .0049025
                                                                .0562968
1995
       .2119147
                              .3416048
                                         .0046418
                                                                .0735728
1996
       .2486543
                              .3412075
                                         .0042419
                                                                .0492886
1997
1998
       .2557822
                              .3805847
                                         .0036284
                                                                .0632589
1999
         .24936
                              .3900273
                                         .0030315
                                                                .0547237
                                         .0030684
2000
       .2586436
                              .3904677
                                                                .0399822
2001
       .2595372
                              .3681855
                                         .0026989
                                                                .0386248
2002
       .2523283
                              .3431315
                                         .0025533
                                                                .035173
2003
       .2616688
                              .3591827
                                         .0026552
                                                                .0384055
       .2605589
                              .376606
2004
                                         .002307
                                                                .0442051
        .289827
                            .4126986
2005
                                         .0025538
                                                                .0442555
2006
       .3059646
                            .4518899
                                         .0025748
                                                                .0484498
       .308138
2007
                            .4923144
                                         .0024674
                                                                .0496636
       .3022883
                                         .0027778
2009
                              .5673997
                                                                .0648812
2010
       .2516191
                              .4079681
                                         .0021084
                                                                .0268149
```

Tax data: Pareto models and non-parametric: estimates: Theil among the richest 100*P_R %, SE(Theil); tax data (threshold = p90 in the survey)

year	ge1_mlo	ge1_gpd	ge1_np	se_ge1_~o	se_ge1_~d	se_ge1_np
1995	.1508662	•	.2197679	.0029998		.0473592
1996	.1669855		.3129517	.0030102		.0618038
1997	.1730002		.3181325	.002385		.0408789
1998	.1934589		.3506664	.0022834		.0504378
1999	.1981813		.3602051	.0020566		.0442391
2000	.2132349		.3665609	.0021835		.0332759
2001	.2087459		.3465109	.0017901		.031576
2002	.2065366		.3236651	.0016792		.0284392
2003	.2104556		.3397191	.0016993		.0315792
2004	.1930813		.3492759	.001303		.035752
2005	.2154732		.3871073	.00145		.0366512
2006	.2288503		.4253711	.0014847		.0404455
2007	.2357809		.4590642	.0014759		.0413343
2009	.2154662		.5150243	.0014845	•	.0528829
2010	.1932468		.3717209	.0012418		.0207152

Tax data: non-parametric estimates: HSCV among the richest 100*P_R %, SE(SCV); (threshold = p99 in the survey)

```
ge2_np se_ge2_np
year
1995
     .3703653 .1119796
      2.553078 1.068631
1996
1997
     1.609383 .5912639
     2.457971 1.326763
1998
      2.450336 1.14099
1999
2000 1.545045 .5096064
2001 1.662092 .7344644
     1.46042 .6613069
2002
2003 1.522263 .5258301
2004
     1.610249 .5806384
2005 1.802406 .6680321
2006 2.406135 1.107318
2007 3.023111 1.326159
2009 4.192604 2.127515
2010 2.026619 .6967632
```

```
Approach C estimates, by threshold, with graphs of trends at the end (pareto 14);
Tax data: non-parametric estimates: HSCV among the richest 100*P_R %, SE(SCV); (threshold = p95 in the survey)
    year
             ge2 np se ge2 np
    1995
            .4732059
                     .154803
    1996
            2.74252 1.096368
    1997
           1.833767
                     .6364387
    1998
           2.780726 1.462337
    1999
           2.777043
                    1.260713
     2000
          1.912189 .5951119
     2001
          1.958515 .8098394
           1.69013 .7083473
     2002
     2003
          1.765383 .5785629
          1.927185
     2004
                    .6621051
           2.23813 .7891974
     2005
           3.045173 1.345713
     2006
     2007
           3.881392 1.656142
     2009
           5.593761 2.805344
     2010
           2.425711
                     .7907994
Tax data: non-parametric estimates: HSCV among the richest 100*P_R %, SE(SCV); (threshold = p90 in the survey)
             ge2_np se_ge2_np
    year
           .4943735
    1995
                     .1599499
    1996
            2.69334 1.064673
    1997
           1.855051
                       .62982
           2.811559
    1998
                     1.45893
    1999
           2.815917
                    1.262346
     2000
          1.988952
                     .6061137
     2001
           2.016029
                     .8118414
     2002
           1.731156 .7023242
     2003
          1.821363 .5827562
           1.980654
     2004
                     .6665972
           2.347095
     2005
                     .8118706
     2006
           3.207164
                    1.397407
     2007
           4.106353 1.735639
     2009
            5.97191 2.985444
     2010
           2.478532
                    .7903417
```

SURVEY DATA ESTIMATES

```
Survey data: Mean incomes (and SEs), poorest 100% 99% 95% 90% in survey (HBAI no_spi)
```

year	mean_100	mean_99	mean_95	mean_90	se_me~100	se_mea~99	se_mea~95	se_mea~90
1994	17568.84	16247.06	14424.05	12935.52	108.7958	66.63673	52.30388	44.79353
1995	17710.32	16464.41	14657.58	13181.87	95.9942	65.27045	51.71943	44.63707
1996	18538.32	17187.34	15309.6	13774.5	121.3486	68.33523	54.44384	47.08815
1997	18923.65	17460.8	15510.47	13962.58	113.5129	72.93839	57.1982	49.29964
1998	19664.83	18041.53	15961.72	14359.92	146.5929	78.164	60.08782	51.64522
1999	20279.88	18694.7	16627.54	15000.79	129.3617	75.48351	58.4411	50.38337
2000	21758.89	19443.25	17196.16	15520.13	246.9471	82.2681	62.35143	53.89151
2001	22240.14	19996.4	17716.19	15963.92	368.3678	81.9846	62.33885	53.3261
2002	21568.29	19888.21	17648.29	15916.24	129.1392	78.04877	60.23559	51.80199
2003	21966.77	20231.44	18000.59	16253.87	137.6665	78.61457	60.87997	52.18654
2004	22426.24	20654.14	18348.18	16577.8	133.8744	81.61338	62.44443	53.7698
2005	22970.71	20681.77	18368.74	16581.99	414.9853	80.98448	62.77187	54.05857
2006	22716.45	20773.34	18464.66	16662.82	155.5964	87.59673	67.0558	57.34881
2007	22617.67	20730.44	18361.62	16574.89	154.3692	89.82967	68.16478	58.42841
2008	23517.89	21061.79	18678.15	16861.51	606.0826	92.54469	70.56518	60.24641
2009	23017.63	20928.21	18502.72	16701.05	180.0382	91.6692	68.81789	58.71284
2010	22138.77	20128.06	17806.01	16080.47	165.6817	86.42778	65.01446	55.71654
2011	21301.97	19622.54	17351.86	15658.85	157.8365	102.2405	72.4127	60.25822
2012	21129.72	19420.89	17237.61	15613.27	175.2743	95.18062	72.70496	63.28411

Survey data: Gini coefficient (and SEs), poorest 100% 99% 95% 90% in survey (HBAI no_spi)

year	gini 100	gini 99	gini 95	gini 90	se gi~100	se gin~99	se gin~95	se gin~90
1994	.472323	.4391356	.4065409	.3857156	.0025595	.0012603	.0011326	.0011489
1995	.463222	.4321555	.3997137	.3789609	.0021399	.001236	.0011115	.0011279
1996	.4630767	.4304282	.398096	.3774397	.0028988	.0012436	.0011264	.0011422
1997	.4652113	.4300135	.3958455	.3749504	.0024285	.0013241	.0011741	.0011849
1998	.4699149	.4318592	.3953609	.3737798	.0033113	.0013765	.001193	.001201
1999	.4563874	.4197488	.3844032	.362718	.002792	.0012888	.0011154	.0011172
2000	.4764894	.4237607	.3856301	.3645655	.0055104	.0013732	.0011598	.0011666
2001	.4726044	.4229882	.3857013	.3634131	.0084824	.0013266	.0011368	.0011387
2002	.4556557	.4191605	.3823379	.3599685	.0025654	.0012871	.0011283	.001134
2003	.4522397	.4146416	.3786189	.3563949	.0027911	.0012633	.0011049	.0011105
2004	.451385	.4137261	.3763697	.3540265	.0025624	.001308	.0011285	.001134
2005	.4657283	.4160367	.3791531	.3569149	.0094399	.0012942	.0011388	.0011494
2006	.4558289	.4143978	.3776759	.3549412	.0030107	.00139	.0012054	.0012152
2007	.4569121	.4169575	.3783844	.3559613	.0029592	.0014498	.001243	.0012518

Approach C estimates, by threshold, with graphs of trends at the end (pareto 14); 2008 .4679517 .4153965 .3774598 .355032 .0135159 .0014692 .0012728 .0012836 2009 .4590352 .414584 .3743414 .351203 .0035715 .0014857 .0012647 .001269 2010 .4580632 .4134066 .3734187 .3503199 .0034063 .0014563 .0012406 .0012503 2011 .4469958 .4090377 .3678748 .3431162 .0031719 .0018079 .0014205 .0014182 2012 .4462832 .4069328 .3679185 .34591 .0037592 .0016767 .0014532 .0014674 Survey data: MLD (and SEs), poorest 100% 99% 95% 90% in survey (HBAI no spi) ge0 100 ge0_99 ge0 95 qe0 90 se qe0~00 se qe0 99 se qe0 95 se qe0 90 year .0035871 .0036475 1994 .4969565 .4448276 .4006435 .3745283 .0054016 .0036828 .4272833 .0035797 1995 .4747472 .3843256 .3590096 .0046725 .0035971 .0035141 1996 .4790595 .42893 .3866238 .3619172 .0059842 .0037961 .003736 .003819 .4233427 1997 .4774522 .3787588 .3539031 .0051463 .0037943 .0036948 .0037654 .4805134 .4207649 1998 .3728894 .347151 .0065848 .0037965 .0036577 .0037194 1999 .4213244 .3655647 .3197096 .005058 .0027277 .2932615 .0025128 .0024972 2000 .4631009 .3778259 .3282733 .3026329 .0102552 .0029838 .0027376 .0027349 2001 .458056 .3781143 .3297572 .3030414 .0159411 .0029147 .0026927 .0026866 2002 .4265866 .3714052 .3242906 .297941 .0046978 .0028221 .002627 .0026202 .4179406 .3612774 .3157693 .2898809 .0050713 .0027819 .0026013 .0026012 2003 2004 .4190383 .3627216 .3159965 .2905196 .0047054 .0029172 .0027272 .0027355 2005 .4488186 .3700412 .3235898 .2980318 .0175593 .0029716 .0028022 .0028142 2006 .4279332 .3651884 .319093 .2931317 .0031005 .0029006 .002907 .0054905 2007 .4344676 .3739877 .3255582 .3001172 .0054694 .0032935 .0030772 .0030906 2008 .4599358 .376112 .3288922 .3038459 .0252607 .0034626 .0032708 .0032958 .4375291 .3694542 .3195554 .0065587 2009 .2939922 .003401 .0031819 .0032025 2010 .429448 .3610908 .3114119 .2856084 .00618 .0031452 .0029056 .0029087 2011 .4079798 .3518671 .3016068 .2749273 .0057902 .0037732 .0034014 .00341 2012 .4111338 .3530922 .3058012 .2818496 .0067128 .0037038 .0034716 .0034913 Survey data: Theil coefficient (and SEs), poorest 100% 99% 95% 90% in survey (HBAI no_spi) se ge1~00 se ge1 99 se ge1 95 se ge1 90 year gel 100 ge1 99 ge1 95 ge1 90 .4144205 .0107548 .0019112 .0014773 1994 .3202805 .2704902 .2444596 .0015339 1995 .3908314 .3097924 .2611008 .2356814 .0067953 .0018404 .0014762 .0014222 1996 .3993823 .3070809 .2589458 .2337766 .0148014 .0018362 .0014897 .0014352 1997 .4025891 .3074812 .2561327 .2308487 .0074576 .0019656 .0015391 .0014757 1998 .4268303 .3110523 .2553305 .2291471 .0156527 .0020726 .0015629 .0014919 .3956642 .2916681 .2397054 .2140793 .0114663 .0018624 .0014021 1999 .0013268 2000 .4978181 .2992969 .2417646 .2168843 .0322911 .0020311 .001467 .0013976 .5114286 .2980739 .242203 .21585 .073371 .0014347 .0013575 2001 .0019468 2002 .3918648 .2923957 .2382627 .2121447 .0014115 .0013395 .0087857 .0018537 2003 .3930174 .2852631 .2332013 .2075343 .0112301 .0017939 .0013701 .0013013 2004 .3877697 .2851863 .2308694 .2053042 .0085443 .0018679 .0013931 .0013238

Approach C estimates, by threshold, with graphs of trends at the end (pareto 14); 2005 .5024381 .2883504 .2346063 .2089942 .0856763 .0018495 .0014174 .0013532 2006 .4045244 .2860975 .2327275 .2066422 .0108688 .001989 .0014905 .0014187 2007 .401395 .2908952 .2340048 .2082963 .0098258 .0021045 .0015448 .0014721 2008 .5302129 .2888031 .2333733 .2078357 .1269576 .0021162 .0015836 .0015133 2009 .4237711 .2885957 .229237 .2030157 .0145881 .0021497 .0015551 .001475 2010 .4230374 .2865068 .2278205 .2016953 .0138805 .0020971 .0015152 .0014405 .3829484 .281124 .2212614 .1936216 .0105618 .0026761 .0017106 2011 .0016095 2012 .3839085 .2770038 .221145 .1967897 .0138443 .0023497 .0017597 .001685 Survey data: Half Squared Coefficient of Variation, GE(2) (and SEs), poorest 100% 99% 95% 90% in survey (HBAI no_spi) ge2_99 se ge2~00 se ge2 99 se qe2 95 se qe2 90 ge2 100 ge2_95 ge2 90 year 1994 .8257974 .354761 .2708966 .2354188 .1253902 .0027133 .0016951 .0015191 1995 .645525 .3425754 .2611488 .2268152 .0473049 .0026017 .0016178 .0014522 .8625702 .3385621 1996 .2586074 .2246478 .2486128 .0025553 .0016292 .0014618 1997 .6974645 .3421382 .2552415 .2208847 .040231 .0028237 .0016835 .0014974 1998 1.034494 .3514183 .2556981 .2199998 .1942446 .0030724 .001719 .0015143 1999 .8393157 .3271122 .2406055 .2064352 .1196628 .0027047 .0015464 .0013577 2.260654 .3405344 .2414693 .2082268 .5673445 .003063 .0016034 .0014183 2000 2001 6.382292 .3379169 .2425138 .2067916 3.753239 .0028972 .0015744 .0013758 2002 .7398049 .3290322 .2379725 .2025414 .0639681 .0026723 .0015332 .0013434 2003 .871011 .3193993 .2331922 .0025466 .1987943 .1070736 .0014815 .0013029 2004 .7469031 .3215204 .2301449 .1956907 .0557357 .0027102 .0014965 .0013117 2005 7.426051 .3239304 .2336284 .1989975 5.621798 .0026434 .0015188 .0013406 .862484 .3219229 .2322933 2006 .1970586 .0811135 .0028968 .0016007 .0014102 .7764937 .3299067 .2325905 .1976771 .0583485 .0031267 .0016513 .0014516 2007 2008 10.10986 .3255871 .2313047 .1965393 8.788145 .0030831 .0016766 .0014753 2009 1.084875 .3300335 .2277553 .1919303 .1527846 .0032134 .0016564 .0014378 1.09438 .3272814 .2268171 .0031293 .0016146 2010 .1913613 .1474963 .0014136 .3234162 .221305 .0018151 2011 .743455 .1835307 .0746583 .0042953 .0015554 2012 .7690785 .3128728 .2185574 .1858407 .108897 .003363 .0018445 .0016299 COMBINED DATA ESTIMATES Combined data (tax and survey) estimates: Means (threshold = p99 in the survey)

Mall mlo Mall gpd Mall np year 17667.27 17740.02 17681.45 1995 1996 18596.3 18685.52 18641.65 1997 19012.79 19097.77 19051.91 19745.78 19811.57 1998 19803.58 1999 20571.16 20720.74 20676.34 2000 21537.45 21715.11 21598.02

```
Approach C estimates, by threshold, with graphs of trends at the end (pareto 14);
     2001
            22134.57
                        22304.95
                                    22200.61
     2002
             22026.4
                        22144.05
                                    22076.48
     2003
            22429.13
                        22535.63
                                    22490.42
            23021.86
                        23105.67
                                    23072.71
     2004
     2005
            23585.69
                        23657.61
                                     23614.5
     2006
            23976.53
                        24031.71
                                    23985.04
            24169.21
                        24286.49
     2007
                                    24246.99
     2009
            23942.82
                        24294.63
                                    24105.74
     2010
                22496
                        22655.37
                                    22623.57
Combined data (tax and survey) estimates: Means (threshold = p95 in the survey)
            Mall mlo
                        Mall gpd
                                    Mall np
     year
             16958.3
                        17059.18
     1995
                                   17038.65
     1996
            17713.66
                        17919.95
                                   17914.53
     1997
            18199.29
                        18370.64
                                   18364.98
     1998
            18910.96
                        19105.47
                                   19117.25
     1999
            19871.36
                        20101.64
                                       20131
            20834.19
                        21164.05
                                    21147.39
     2000
     2001
            21414.75
                        21696.49
                                    21676.24
     2002
            21363.55
                        21617.69
                                    21587.58
            21660.79
     2003
                        21910.19
                                    21889.71
     2004
            22319.27
                        22691.86
                                    22614.91
     2005
             22973.3
                        23504.74
                                    23340.79
                         24082.5
     2006
            23389.46
                                    23841.8
            23658.03
                        24459.85
                                    24233.11
     2007
     2009
             23027.02
                         23929.7
                                    23725.25
     2010
            21921.53
                        22338.35
                                    22307.04
Combined data (tax and survey) estimates: Means (threshold = p90 in the survey)
            Mall mlo
                        Mall qpd
                                     Mall np
     year
            16336.85
                        16559.47
                                    16526.84
     1995
     1996
            16990.65
                        17296.87
                                   17303.65
     1997
            17468.94
                        17934.25
                                   17827.13
     1998
            18254.58
                        18654.05
                                   18631.62
            19242.16
                        19655.79
     1999
                                    19659.9
            20243.56
     2000
                        20717.27
                                    20715.61
     2001
            20766.91
                        21226.13
                                    21202.98
            20802.14
                        21195.99
     2002
                                    21184.6
                        21425.34
     2003
             20972.4
                                    21374.94
     2004
             21787.9
                         22388.9
                                     22330.5
     2005
            22473.37
                        23258.88
                                    23139.75
```

Approach C estimates, by threshold, with graphs of trends at the end (pareto 14); 23575.14 2006 22803.63 23733.43 2007 23235.19 24175.34 24133.19 2009 22522.35 23484.71 23563.98 2010 21566.41 22116.74 22174.89 Combined data (tax and survey) estimates: Gini coefficient and between-group Gini (threshold = p99 in the survey) G_mlo G_gpd G_np GB_mlo GB_gpd year GB_np 1995 .4635513 .4657528 .4639826 .0674999 .0712889 .0682406 1996 .4660671 .4686185 .4673679 .0750868 .0794603 .077315 1997 .4688395 .4712043 .4699313 .0808772 .0849259 .0827453 1998 .473086 .4748367 .4746251 .0855052 .0885111 .0881475 1999 .4641395 .4680108 .4668685 .0902625 .0967542 .0948373 2000 .4716938 .4760194 .4731787 .0962745 .1035871 .0987813 .4700716 .4741232 2001 .4716515 .0955779 .1024055 .0982367 2002 .4665582 .4693954 .4677714 .0960006 .1007446 .0980264 2003 .4626068 .465149 .4640739 .0968387 .1010517 .0992683 .4649119 .4668542 2004 .4660928 .1016759 .1048928 .1036307 .477459 .4790488 .1215028 .1241335 2005 .4780977 .1225585 .4819032 .4830937 .4820877 .1317794 .1337419 .1320825 2006 .1429587 2007 .4886256 .4910962 .4902672 .1402466 .1443294 .478947 .4864964 2009 .4824725 .1244185 .1369263 .1302561 2010 .4659827 .469741 .4689959 .104053 .1102745 .1090403 Combined data (tax and survey) estimates: Gini coefficient and between-group Gini (threshold = p95 in the survey) G_mlo GB_mlo G_gpd GB_gpd GB_np year G_np 1995 .4543183 .4575554 .4569014 .1309324 .1358656 .1348664 .4536565 .4599621 .459799 1996 .131082 .1406914 .1404416 .4630322 1997 .4579634 .4628669 .1424383 .1501021 .1498511 1998 .4617901 .4672842 .4676127 .1501837 .1584586 .1589543 .4549628 1999 .4612223 .4620086 .1565757 .16577 .1669272 2000 .4610763 .4694976 .4690802 .1670239 .1793287 .1787164 2001 .4604463 .4674718 .4669746 .1653188 .1756017 .1748715 2002 .4579822 .464375 .4636279 .1663093 .1755968 .1745076 .4530074 .4592525 .4587468 2003 .1618055 .170863 .1701271 .4640244 .4622001 2004 .4550429 .1698973 .1827867 .1801594 2005 .4678978 .4799767 .4763221 .1904018 .2075752 .2023605 2006 .4715123 .4867799 .4815961 .1994822 .2210055 .2136722 2007 .477724 .4949121 .4901837 .211232 .2352376 .2286103 .4635308 2009 .4838179 .4793687 .1870867 .2159485 .2096038 2010 .4565831 .4667588 .4660097 .1786228 .1930432 .1919787

Approach C estimates, by threshold, with graphs of trends at the end (pareto 14); Combined data (tax and survey) estimates: Gini coefficient and between-group Gini (threshold = p90 in the survey) year G mlo G apd G np GB mlo GB apd GB np 1995 .448957 .4564277 .4553542 .1797662 .1898632 .1884004 1996 .4480722 .4579046 .4581174 .1768547 .1902646 .190556 1997 .4503004 .4646723 .4614529 .1865884 .2058659 .2015172 1998 .4554734 .4672198 .4665779 .2132548 .1976492 .2123962 1999 .4494206 .4610904 .4612026 .203136 .2182549 .2184017 2000 .4563595 .4688694 .4688273 .2140757 .2301596 .2301043 2001 .4550109 .4668828 .4663009 .2124678 .2277461 .2269915 2002 .4531839 .46342 .4631323 .2150893 .2281087 .2277391 .4473753 .4591452 .4578691 .2070119 .222087 .2204411 2003 2004 .4483678 .4633034 .4619003 .217645 .2362345 .2344721 2005 .4606078 .4789814 .4762992 .2366533 .2591487 .2558353 .4852055 2006 .4640407 .4817491 .243018 .2688518 .2645978 2007 .4704146 .491175 .4902895 .2561369 .2809254 .2798555 2009 .4551767 .4776365 .4793996 .2334842 .2609337 .2630946 .4508021 .4645844 2010 .4659903 .2294575 .2461936 .2479132 Combined data (tax and survey) estimates: MLD and between-group MLD (threshold = p99 in the survey) L_mlo LB_mlo year L_gpd L_np LB_gpd LB_np 1995 .4762005 .480323 .4769587 .0511841 .0548413 .0518961 .4849565 .4898164 1996 .4873637 .0580284 .0623173 .0602078 1997 .4847484 .489282 .4867671 .0633707 .0673843 .0652179 1998 .4866759 .4900915 .4895717 .0678064 .070811 .0704465 1999 .4348551 .4422211 .4399079 .0709396 .0774547 .0755212 .4542472 .4626758 .4570264 .077818 2000 .0852932 .0803681 .4525674 .4604222 .0761364 .0830644 2001 .4555143 .0788225 2002 .4454822 .4509524 .447727 .0758826 .0806712 .0779214 2003 .4354116 .4402836 .4381098 .075877 .0801138 .0783155 .4423144 2004 .4461065 .4444951 .0811562 .0844289 .0831423 2005 .467543 .4708159 .4687421 .0990674 .1018176 .1001694 2006 .4731927 .4757859 .4735329 .109226 .1113114 .1095476 2007 .4899141 .4951009 .4930929 .1172707 .1216699 .1201893 .472682 2009 .4877432 .4794142 .1040568 .1174314 .1102614 .4429634 2010 .4501919 .4485602 .0834524 .0898287 .0885573 Combined data (tax and survey) estimates: MLD and between-group MLD (threshold = p95 in the survey)

LB_np

.090051

LB_gpd

.0910084

year

1995

L_mlo

.4619308

L_gpd

.4677332

L_np

.4664939

LB_mlo

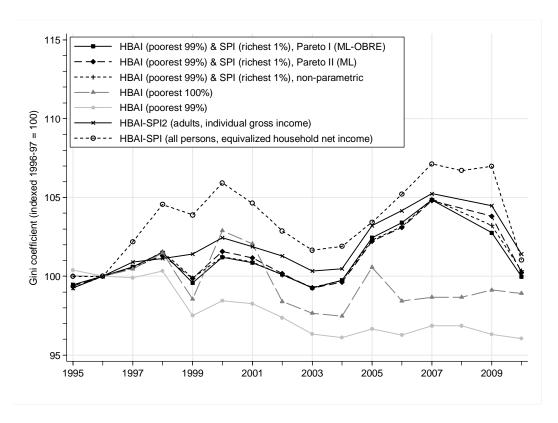
.0863073

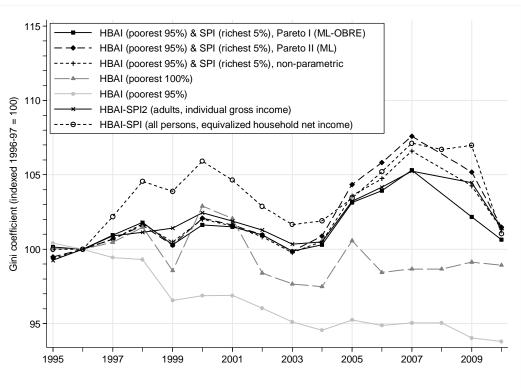
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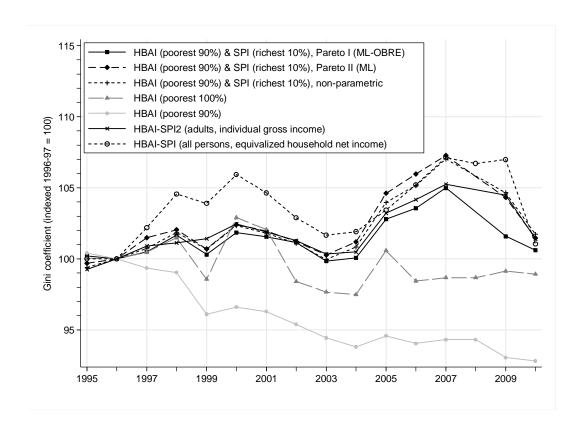
Approach C estimates, by threshold, with graphs of trends at the end (pareto 14); 2001 .4586726 .4682822 .1540798 .1605211 2002 .4490657 .4562163 .1518696 .1566969 2003 .4417379 .4509963 .1499374 .1556332 2004 .4584501 .4655118 .1632824 .1680009 2005 .5068599 .5083229 .1995365 .2021359 2006 .5368554 .5340071 .2218586 .2226205 .5607189 .5707525 .2382193 .2451218 2007 2009 .5398196 .5648244 .2166809 .2318728 2010 .4644972 .4862355 .1684455 .1806392 Combined data (tax and survey) estimates: Theil and between-group Theil (threshold = p95 in the survey) T mlo T apd T np TB mlo TB qpd TB np year .1367988 1995 .3873488 .399426 .1435578 1996 .3899024 .4285385 .1387281 .1551604 1997 .4092895 .4396783 .1544906 .1677421 1998 .4210593 .4614742 .1656442 .1815996 .1680383 1999 .4096497 .457465 .1865288 .4257922 .4763707 .1804743 .2015632 2000 2001 .4248226 .4658311 .179012 .1962052 2002 .4199902 .4545569 .1787738 .1934124 2003 .4126235 .4484146 .1736076 .1884328 2004 .4192195 .4640104 .1819669 .2003121 2005 .4553958 .5089023 .2075122 .2293455 2006 .4693946 .5354087 .2182057 .2443255 2007 .4848503 .5708519 .2310001 .2632088 2009 .4529904 .565032 .2065948 .2487516 2010 .4230736 .4848856 .1898465 .2137334 Combined data (tax and survey) estimates: Theil and between-group Theil (threshold = p90 in the survey) year T mlo T apd T np TB mlo TB apd TB np 1995 .3722211 .402344 .1576516 .1707611 1996 .3754482 .4332132 .1578715 .1791481 1997 .3822703 .4441222 .1662881 .1895393 1998 .3983943 .4661478 .202246 .1789278 .4623459 .2048936 1999 .3906119 .1810087 2000 .4083539 .481603 .192552 .2179264 2001 .4053435 .470694 .1915808 .2145567 2002 .4023989 .4586729 .1919328 .2117364 .2060703 2003 .393415 .4533047 .1850425 2004 .3906173 .4670285 .1890715 .2150327 2005 .42054 .5115795 .2093824 .2396947

2006	.4330982	•	.5395249	.2188924	•	.2536675
2007	.4473491		.572543	.2290876		.2673767
2009	.4123406		.567657	.2052145		.2523947
2010	.3965979		.4866246	.1976687		.2261232

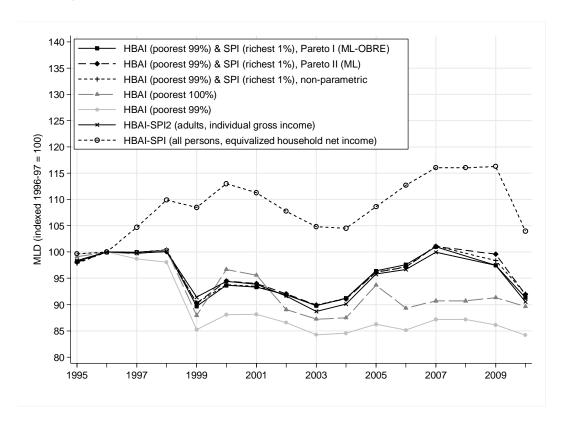
Gini coefficient (indexed 1996/97 = 100), by threshold

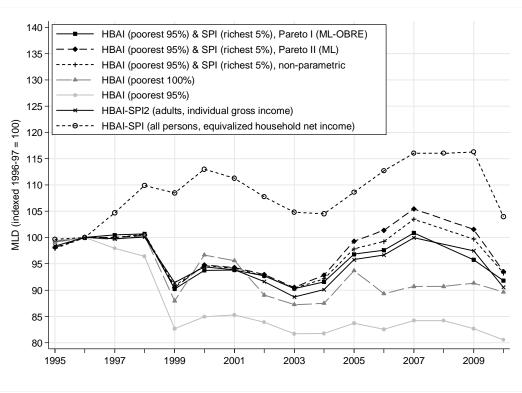


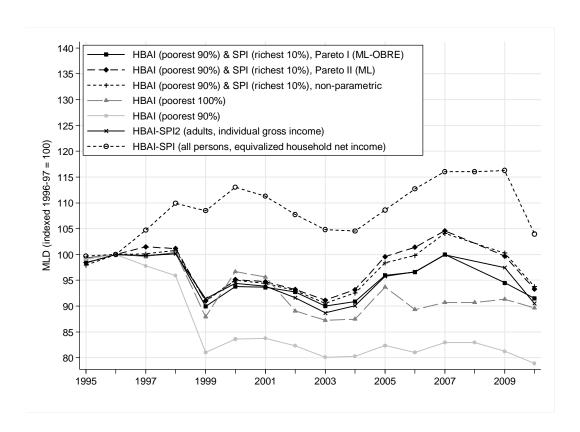




Mean Logarithmic deviation (indexed 1996/97 = 100), by threshold







Theil coefficient(indexed 1996/97 = 100), by threshold

