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## Sensitivity of Climate Change Detection and Attribution to the Characterization of Internal Climate Variability

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#### ABSTRACT

The Intergovernmental Panel on Climate Change's (IPCC) "very likely" statement that anthropogenic emissions are affecting climate is based on a statistical detection and attribution methodology that strongly depends on the characterization of internal climate variability. In this paper, the authors test the robustness of this statement in the case of global mean surface air temperature, under different representations of such variability. The contributions of the different natural and anthropogenic forcings to the global mean surface air temperature response are computed using a box diffusion model. Representations of internal climate variability are explored using simple stochastic models that nevertheless span a representative range of plausible temporal autocorrelation structures, including the short-memory first-order autoregressive [AR(1)] process and the long-memory fractionally differencing process. The authors find that, independently of the representation chosen, the greenhouse gas signal remains statistically significant under the detection model employed in this paper. The results support the robustness of the IPCC detection and attribution statement for global mean temperature change under different characterizations of internal variability, but they also suggest that a wider variety of robustness tests, other than simple comparisons of residual variance, should be performed when dealing with other climate variables and/or different spatial scales.

#### 1. Introduction

At the center of the climate change debate is the question of whether global warming can be detected, and if that is the case, whether or not it can be attributed to anthropogenic causes. Optimal fingerprinting is a powerful method of detection and attribution of climate change (Hasselmann 1979, 1993; Hegerl et al. 1996) used widely in this area of research. In essence,

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optimal fingerprinting is a multiregression analysis that searches for the observed temperature record response to external drivers or forcings, such as changing levels of greenhouse gases, and aerosol loading (human induced), volcanic activity, and variations in solar radiation (naturally induced). A key input in the procedure of fitting this multiple regression model is an estimate of the internal variability of the climate system, against which the statistical significance of anthropogenic and natural signals must be compared. Hence, an accurate depiction of this variability is crucial for the robustness of the results.

In this work, we refer to internal variability as the characterization of the variations in the climate system that would occur in the absence of natural or anthropogenic

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forcings, solely due to the coupling of atmosphere, ocean, biosphere, and cryosphere dynamics. In most cases, global climate models (GCMs) are used to estimate climate internal variability because instrumental records are both too short to provide a reliable estimate and contaminated by the effects of external forcings. Typically, long GCM control simulations are employed for this purpose. This is such a key step in the process of detecting and attributing climate change that, in fact, for some authors (e.g., Huybers and Curry 2006), the debate surrounding global warming centers on the uncertainties in the structure and magnitude of the internal variability of the climate system.

Previous studies (Allen and Stott 2003; Huntingford et al. 2006) used increasingly sophisticated variations of the multiregression technique in order to quantify the statistical significance of the anthropogenic signal in temperature trends as simulated by a range of climate models. In these studies, long GCM control simulations are used to estimate internal variability on the temporal and spatial scales that are retained in the analysis. Although these authors are careful to attempt the inclusion of model uncertainty in the regression model and test the robustness of their results under changes in the amplitude of the estimated internal variability, it is not clear whether or not other aspects of the internal variability poorly represented by the climate models (Newman et al. 2009; DelSole and Shukla 2010; Klein et al. 1999) do bias statistical estimations of the significance of the anthropogenic signal in the observations.

In this paper, we investigate this question by assuming that the internal climate variability can be represented by a stochastic process that includes, apart from a white noise component, some information about more complex temporal correlations between different states of the climate system. We refer to this temporal correlation between different states as the memory of the system [also named climate persistence by some authors (Beran 1994; Percival et al. 2001). Understanding and characterizing the memory of the climate system is problematic because of the short length of the observational records when compared to the wide range of interconnected time scales. In fact, numerous explanations have been advanced regarding internal variability (e.g., Wunsch 2003; Mitchell 1976; Hays et al. 1976), but the full characterization of its properties and its interplay with external forcings remains elusive (Ghil 2014).

We use two different stochastic models to represent internal variability: a first-order autoregressive [AR(1)] model and a fractionally differencing (FD) model (Percival et al. 2001). These correspond to the two simplest stochastic models (minimal number of parameters) that can represent significantly different assumptions about the internal temporal structure of the system they describe. While the AR(1) model has the short memory characteristic of an exponentially decaying autocorrelation function, the FD model has the long memory associated to an algebraically decaying autocorrelation function. These two models have been considered before as two different but plausible (e.g., Hasselmann 1979; Vyushin and Kushner 2009) characterizations of the climate internal variability in terms of equally simple parametric models. In addition, choosing these simple models allows us to carry out a sensitivity analysis of detection and attribution to well-defined parameters whose change is easily understood in terms of memory or unresolved variability (white noise) in the climate system.

The paper is organized as follows. In section 2, we describe the data analyzed. We briefly discuss the detection and attribution approach as applied to the onedimensional climate model used in our study and to the two stochastic models, exploring the arguments to justify using each of them to represent internal climate variability. In section 3, we discuss how the significance of the anthropogenic signal depends on the model chosen to represent internal variability. We include an analysis of how consistent our estimates of internal variability are with the ones estimated from the Coupled Model Intercomparison Project, phase 3 (CMIP3), control simulations in order to evaluate whether or not the use of these control runs for detection and attribution can potentially bias the results. Section 4 is devoted to the conclusions.

We remark that our goal is to explore the sensitivity of the detection and attribution statistics to the representation of internal variability. Therefore, the main assumptions of detection and attribution of climate change, namely, that the forced responses can be linearly superimposed on internal variability and that there are no interactions between forced and unforced variability, are assumed to be valid.

#### 2. Data and method

We analyze the problem of the sensitivity of detection and attribution results to internal variability in the simplest case, that is, for the global mean surface air temperature as simulated by a one-dimensional climate model.

To estimate the temperature responses to individual forcings, we use the box diffusion model (BDM) described in Andrews and Allen (2008) and Allen et al. (2009), which can be written as

$$c\frac{dT}{dt} = F - \lambda T - \frac{c}{d_{\rm ml}}\sqrt{\frac{\kappa}{\pi}} \int_0^t \frac{dT(t')}{dt'} \frac{dt'}{\sqrt{(t-t')}}, \quad (1)$$

where *T* is the global mean temperature and *F* is the external forcing. In Allen et al. (2009), the heat capacity  $c = 7.22(W y/m^2 K)$  corresponds to the heat capacity of an ocean mixed layer of depth  $d_{ml} = 75$  m, assuming that the ocean covers 70% of the Earth's surface. Best estimates for the climate feedback parameter  $\lambda$  and effective ocean diffusivity  $\kappa$  are determined using the linear temperature trend attributable to the increase in greenhouse gases over the twentieth century on the basis of fingerprint attribution results (Stott et al. 2006), the effective heat capacity of the atmosphere–land–ocean system implied by the combination of observed surface warming (Brohan et al. 2006), and the total ocean heat uptake over the period 1955–98 (Levitus et al. 2005). This results in  $\kappa = 0.10[(mld)^2/y] = 562.5(m^2/y)$  and  $\lambda = 1.29(W/m^2 K)$ .

This BDM, with the specified parameters, can then be used to find the temperature responses  $T_i$  to different forcings: volcanic (VOL), solar (SOL), greenhouse gases (GHG), sulfates (SUL), and all anthropogenic forcings together (ANT). In this way, the temperature responses to individual forcings are computed without relying on GCMs.

Note that observed surface temperatures are used in the estimation of parameters in this model, albeit indirectly through the fingerprint results and estimates of effective heat capacity. The main impact of varying parameters in the model, however, is to change the magnitude of the responses to different forcings. The shape, or time evolution, of the response is primarily driven by the forcings themselves. In our subsequent analysis, we use only the temporal shape of the responses, not their magnitude, hence minimizing the risk of "double counting" of data.

The forcings time series required to estimate the corresponding temperature responses using the model in Eq. (1) are obtained from the CMIP, phase 5 (CMIP5), recommended datasets (see http://www.pik-potsdam.de/~ mmalte/rcps/; Meinshausen et al. 2011). To carry out the detection and attribution analysis, observed time series of annual global mean temperature are required. We use the observed data from the Hadley Centre/Climatic Research Unit, version 3 (HadCRUT3; see www.cru.uea. ac.uk/cru/data/temperature/), for the period 1850-2005 (Brohan et al. 2006), and version 4 (HadCRUT4; see www.metoffice.gov.uk/hadobs/hadcrut4/data/current/ download.html; Morice et al. 2012) to test the sensitivity of the results to the addition of the last 7 yr of observations up to 2012 (see section 3). Uncertainties in observed temperatures and estimates of forcings are ignored in this paper.

We additionally use the World Climate Research Programme (WCRP) CMIP3 multimodel archive of control simulations to study the internal variability simulated by the state-of-the-art climate models (Solomon et al. 2007). For completeness, we have used all the control simulations, regardless of drifts. We will comment on the effect of drifts in the control segments on the final results in section 3.

#### a. Detection and attribution

The detection of climate change is the process of demonstrating that climate has changed in some welldefined statistical sense, without providing a reason for that change. Attribution of causes of climate change is the process of establishing the most likely causes for the detected change with some defined level of confidence (Solomon et al. 2007). In this work, we aim to detect and attribute climate change by estimating the contribution to the observational record  $T_{obs}$  of each of the response temperatures  $T_i$  calculated using Eq. (1). In other words, we want to obtain the amplitudes  $\beta_i$  in the following expression:

$$T_{\rm obs} = \mathbf{T}\boldsymbol{\beta} + \boldsymbol{u}, \qquad (2)$$

where **T** is a matrix with n + 1 columns, including the *n* forced responses  $T_i$ , and a constant term to remove the mean. The variable *u* is a stochastic term that represents the internal climate variability with covariance matrix is given by  $\Omega = E(uu^{\dagger})$ . Under the assumption that *u* is multivariate normal (Allen and Tett 1999), the optimal scaling factors,  $\beta = (\beta_1, \beta_2, ..., \beta_{n+1})$  are given by (Kmenta 1971)

$$\hat{\boldsymbol{\beta}} = (\mathbf{T}^{\dagger} \boldsymbol{\Omega}^{-1} \mathbf{T})^{-1} \mathbf{T}^{\dagger} \boldsymbol{\Omega}^{-1} \boldsymbol{T}_{\text{obs}}$$
(3)

and their variance

$$V(\hat{\boldsymbol{\beta}}) = (\mathbf{T}^{\dagger} \Omega^{-1} \mathbf{T})^{-1}, \qquad (4)$$

where † is used to denote the transpose of a matrix.

In this work, following standard detection and attribution studies, we consider the following external forcings: greenhouse gases, sulfates, volcanic, and solar. It has long been recognized, however, that the detection and attribution results are sensitive to the omission of potentially important forcings and/or internal modes of variability. Likewise, if signals that have some degree of collinearity are included, this can affect the robustness of the results. This will be tested in section 3a by performing the detection and attribution study considering solar, volcanic, and all anthropogenic forcing together instead of separating greenhouse gases and sulfates into two different signals. The robustness of the detection and attribution statistics to separating other modes of internal variability such as ENSO or Atlantic multidecadal oscillation (AMO) from the noise u in Eq. (2) has been analyzed in Zhou and Tung (2013) and Imbers et al. (2013). In particular, in Imbers et al. (2013), the forced temperature responses to anthropogenic, solar, volcanic, and ENSO and/or AMO are obtained from a series of studies that use different statistical models to single out each forced temperature response. Using the same approach as in this paper, it is found that the ANT detection statistic is robust in all cases.

Typically, detection of anthropogenic climate and its attribution to external forcings requires defining spaceand time-dependent response patterns (Solomon et al. 2007; Stone et al. 2007). These patterns are obtained from GCM transient simulations. On the other hand, the spatiotemporal structure of internal variability in  $\Omega$  is estimated from averaging GCMs' control simulations over space, time, and model ensembles. These calculations are high dimensional and require sensible truncation of the space and time domain using techniques such as principal components analysis.

In this paper we use a simpler version of the detection and attribution approach since we analyze only the global mean surface temperature, introducing parametric models to characterize the global mean internal variability u explicitly as a stationary stochastic process. In other words, we formulate the detection and attribution problem as in Eq. (2), but with u as a function of stochastic parameters that are estimated simultaneously with the scaling factors  $\hat{\beta}$  using a minimum squared error algorithm.

The first challenge is to choose an adequate stochastic representation for the internal variability. The difficulties finding the appropriate stochastic model are due to the uncertainties in characterizing internal variability from the observational record, which, as discussed before, is contaminated by the external forcings and is too short relative to the long time scales potentially relevant to the current climate variability . In particular, in the observed record, it is not clear how to separate the decadal from centennial or even longer time scales (Percival et al. 2001). Given these uncertainties in the characterization of the internal climate variability, we choose to describe it using two models that span a wide range of plausible temporal autocorrelations (Vyushin and Kushner 2009). This choice is important to address the fact that GCM simulations do not necessarily capture all the modes of internal variability in the system, certainly not variability at longer time scales than centennial. We then choose stochastic processes that allow us to explore how the results of detection and attribution of climate change would change if the internal variability has either long or short memory and assume that this is a necessary (not sufficient) test to evaluate the robustness of the

results under a wide range of plausible characterizations of the memory of the climate system.

#### b. Short-memory process: AR(1)

The best known and simplest stochastic representation for discrete geophysical time series is the AR(1)model (Ghil et al. 2002; Bretherton and Battisti 2000). In the continuous time domain, the AR(1) process corresponds to diffusion, which, in turn, is the simplest possible mechanism of a physical process with inertia and subjected to random noise. In the context of climate, this model was first introduced by Hasselmann (1979) to describe the internal variability of the climate system under the assumption of time scale separation between oceanic and atmospheric dynamics. In this framework, the faster dynamics of the atmosphere can be modeled as white noise acting on the slower and damped dynamics of the ocean. Thus, the AR(1) is the simplest model that can explain the "weather" and the "climate" fluctuations as two components of the internal variability. Mathematically, the AR(1) is a stationary stochastic process that can be written as

$$u_t = a_1 u_{t-1} + a_0 \epsilon_t, \tag{5}$$

where  $E(u_t) = 0$ ,  $a_1$ , and  $a_0$  are parameters and  $\epsilon_t$  represents white noise, that is,  $E(\epsilon_t \epsilon_{t'}) = \delta_{tt'}$ . The autocovariance function of this process is determined by  $a_0$  and  $a_1$  as follows:

$$\omega_{\rm AR1}(\tau) = \frac{a_0^2}{1 - a_1^2} a_1^{|\tau|},\tag{6}$$

where  $\tau$  is the time lag. Notice that  $a_1$  controls the decaying rate of the autocorrelation function, and in that sense, we can associate it to the *memory* of the system. On the other hand,  $a_0$  is related to the amplitude of the white noise in the system. From Eq. (6), the covariance matrix  $\Omega$  results:

$$\mathbf{\Omega}_{i,j}^{\text{AR1}} = \frac{a_0^2}{1 - a_1^2} a_1^{|i-j|}.$$
(7)

Equation (5) models the memory of the process such that, at a given time *t*, the state of the system is a linear function of the previous state (t - 1) and some random noise with amplitude  $a_0^2$  jittering, thus moving the system away from equilibrium. The autocovariance of the process, Eq. (6), decays exponentially with time, so the system has always a much better memory of the near past than of the distant past. The variable  $a_1$  can take any value in the interval [0, 1),  $a_1 = 0$  represents the limit in which the system is purely white noise, and  $a_1 \rightarrow 1$  is the

extreme in which a system is dominated by inertia. In our case, we are characterizing annual global mean temper-

case, we are characterizing annual global mean temperature internal variability with this model, so we are trying to quantify the impact of the natural fluctuations in the year-to-year variation.

In the detection and attribution analysis, the parametric form of the covariance matrix, Eq. (7), is used to simultaneously determine the optimal scaling factors  $\beta_i$  in Eq. (3) and the parameters  $a_1$  and  $a_0$  of the climate noise in Eq. (5) following the Hildreth–Lu method (Kmenta 1971).

#### c. Long-memory process: FD

There is empirical evidence that the spectrum of global mean temperature is more complex than the spectrum of an AR(1) process (e.g., Huybers and Curry 2006). Different power-law behaviors have been identified in globally and hemispherically averaged surface air temperature (Bloomfield 1992; Gil-Alana 2005), station surface air temperature (Pelletier 1997), and temperature paleoclimate proxies (Huybers and Curry 2006). These findings suggest that in order to thoroughly test the sensitivity of the detection and attribution statements to the representation of internal variability, modeling it with other than a short-memory process such as the AR(1)model might be in order. We then alternatively assume that the global mean temperature internal variability autocorrelation decays algebraically, allowing for all time scales to be correlated. This long time correlation will clearly have an effect on the statistical significance of the anthropogenic signal [see Eq. (4)].

Long-memory models were motivated initially by hydrology studies (Hurst 1951, 1957) and have been employed to model paleoclimatic time series (e.g., Huybers and Curry 2006; Pelletier 1997). An spectrum corresponding to algebraic decaying correlations can be constructed for a prescribed range of frequencies as the sum of AR(1) processes or as solutions of more complex stochastic differential equations (Erland et al. 2011; Kaulakys et al. 2006; Granger 1980). Therefore, a plausible justification to use a long-memory process to represent the internal variability of the global mean temperature is that it could be thought as the result of the superposition of several diffusion processes [AR(1)].

Applying the law of parsimony, we choose a longmemory process with the same level of complexity as the AR(1) model. The FD model (Beran 1994; Percival et al. 2001; Vyushin and Kushner 2009; Vyushin et al. 2012) is defined as a stationary stochastic process with zero mean u such that

$$u_t = (1 - B)^{-o} \epsilon_t, \tag{8}$$

where *B* is the backshift operator, that is,  $Bu_t = u_{t-1}$  (Beran 1994). The model is fully specified by the pa-

(Derail 1994). The model is fully specified by the parameters  $\delta$  and the standard deviation  $\sigma_e$  of the white noise  $\epsilon_t$ . The autocovariance function is given by the equation

$$\omega_{\rm FD}(\tau) = \frac{\sigma_e^2 \sin(\pi\delta)\Gamma(1-2\delta)\Gamma(\tau+\delta)}{\pi\Gamma(\tau+1-\delta)}.$$
 (9)

As a result, the covariance matrix becomes

$$\mathbf{\Omega}_{ij}^{\text{FD}} = \frac{\sigma_e^2 \sin(\pi\delta)\Gamma(1-2\delta)\Gamma(|i-j|+\delta)}{\pi\Gamma(|i-j|+1-\delta)}.$$
 (10)

For large  $\tau$ , the autocorrelation function satisfies  $\lim_{\tau\to\infty} \omega_{\rm FD}(\tau) = |\tau|^{2\delta-1}$  (Beran 1994). From this expression, one can see that the autocorrelation decays algebraically, thus the name "long memory." Since  $\delta$  controls the decaying rate of the autocorrelation function, it can be associated to the *memory* of the system, while  $\sigma_e$  is characterizes the amplitude of the white noise.

Similarly to the AR(1) case, we use this covariance matrix, Eq. (10), and Eqs. (2) and (3) to simultaneously determine the scaling factors  $\beta_i$  and the parameters  $\delta$  and  $\sigma_e$  following the Hildreth–Lu method (Kmenta 1971).

#### 3. Results

#### a. Robustness of detection statistics

To test the robustness of the detection statistics, we find simultaneously the scaling factors  $\beta_i$  and the stochastic parameters of the internal variability u, using generalized linear regression to solve Eq. (2). Notice that when u is modeled as an AR(1) or an FD process, the noise covariance matrix  $\Omega$  in Eqs. (3) and (4) is given by Eqs. (7) or (10), respectively. The best estimates of the scaling and noise parameters are chosen as those that minimize the residual white noise in u (Kmenta 1971). Using the Akaike information criteria, we find that both models for u are equally skillful at representing the internal variability given the observational record used in our analysis.

Figure 1 shows the values of the optimal scaling factors with their 95% confidence intervals using the AR(1) (gray line) and the FD (black line) models, when  $T_{obs}$  is the HadCRUT3 global mean temperature record for the period 1850–2005. In the detection and attribution approach, a signal is detected when the corresponding scaling factor is different from 0 with 95% confidence, while the attribution of a signal requires confidence intervals that include one (Allen and Stott 2003; Allen and Tett 1999). When the scaling factors are larger or smaller



FIG. 1. The 95% confidence intervals of the scaling factors  $\beta_i$  derived from the multiregression of observed temperature changes onto the BDM estimates of the forced responses. The internal variability is represented by an AR(1) model (gray line) or an FD model (black line) for the period 1850–2005.

than one, the simulated forced responses are assumed to be over- or underestimated by the climate model used to simulate them.

Therefore, in order to test the robustness of the detection statistics, we need to evaluate the statistical significance of the scaling factors and the uncertainty in the determination of the stochastic models' parameters. A scaling factor  $\beta$  is defined as statistically significant if the null hypothesis ( $\beta = 0$ ) can be rejected with 95% confidence. A standard approach to find the confidence interval is to define the z score as z\_score =  $\beta i/V(\beta_i)^{1/2}$ ; if this quantity *i* sampled from, for instance, a *t* distribution with more than 60 degrees of freedom, the scaling factor  $\beta$  will result statistically significant with 95% confidence when the z score  $\geq 2$  (Kmenta 1971). In our analysis, because of the correlations present in the noise models, an estimation of the number of degrees of freedom is problematic. We use instead a Monte Carlo approach that allows a testing of the null hypothesis as follows. For each of the noise models [AR(1) or FD] we generate, using the optimal values of the models' parameters 1000 surrogate samples with the same length as the observed record (156 yr). We then replace  $T_{obs}$  in Eq. (2) by each of these surrogate series and perform the generalized linear regression with the four forced responses on the right-hand side of the equation, the aim of this exercise being to estimate the optimal values of the scaling factors  $\beta$  and the *u* parameters that best fit each of the surrogate series. We can then perform an empirical evaluation of the null hypothesis: for any given value of the z score or, equivalently, the size of the confidence interval, we aim to

find what is the proportion of cases where the scaling factor  $\beta$  is different from 0. In particular, the value of the *z* score that gives  $\beta$  different from 0 in, at most, 5% of the cases determines the 95% confidence interval. We find that for the GHG signal, the *z* score is 2.22 in the case of the AR(1) model and 2.45 in the case of the FD model. In addition, and since we expect that because of the stochastic nature of the noise models there will be some uncertainty in the determination of their parameters, the values of the noise model parameters estimated with this Monte Carlo approach provide an estimate of the uncertainty of the best fit noise model parameters when regressing the forced responses on  $T_{obs}$  in Eq. (2).

Figure 1 shows that for our detection model, the greenhouse gas signal is detected and attributed, the volcanic signal is only detected, and the solar signal is not detected nor attributed for both models of internal variability. In the case of the sulfates forcings, the result depends on the representation of the internal variability.

The robustness of the GHG signal detection can be analyzed using Fig. 2, when the internal variability is characterized by the AR(1) model or by the FD model in the top or bottom panels, respectively. The horizontal and vertical axes show the white noise amplitude and memory parameters, respectively, and the contour lines indicate the significance level of the scaling factor  $\beta_{GHG}$ . The diamond symbol shows the best fit of internal variability (for each model) when the observed record  $T_{obs}$ is the HadCRUT3 data for the period 1850-2005. The uncertainty in the estimation of the best fit, computed using the Monte Carlo approach, is shown as the gray cloud of points. It is clear that even when taking into account this uncertainty in the parameters, the significance of the detection of the greenhouse gas signal is not affected.

As expected, the significance of the greenhouse gas signal is lower when we represent the internal variability as an FD than as an AR(1) process. We find that both stochastic models' best fit have similar white noise amplitude, showing that statistically they are similarly good at explaining variability, given that this is the residual of the linear fit. The bigger difference between the two models arises in the memory parameter.

In the case of the AR(1),  $a_1$  is bounded between  $a_1 = 0.25$  and  $a_1 = 0.70$ , and the best estimate is  $a_1 = 0.53$ . In a short-memory process, we can translate these values into a decay time, which is a well-defined time scale given by  $\tau = -1/\ln(a_1)$  in units of years (Kmenta 1971). Using the range of values of  $a_1$  above, the uncertainty in the decay time remains below 10 yr. This means that, according to the AR(1) model, we can explain the fluctuations of internal variability by being affected mainly by the previous few years and some random white noise.



FIG. 2. (top) Significance of the GHG signal as a function of the two stochastic parameters of the AR(1) model:  $a_1$  in the y axis and  $a_0^2$  in the x axis. The best fit of the observed record is displayed (diamond), showing that the significance is much greater than 2.22 (thick blue contour line) even considering the uncertainty of the Monte Carlo experiment (cloud of gray points). Best fits of the CMIP3 control segments of the same length as the observed record are shown with numbers, where each number represents a GCM (1–22). A total of 33 non-overlapping segments were selected. (bottom) Significance of the GHG signal as a function of the two stochastic parameters of the FD model:  $\delta$  in the y axis and  $\sigma^2$  in the x axis. The best fit of the observed record is displayed (diamond), showing its significance is greater than 2.45 (thick blue contour line), even considering the uncertainty of the Monte Carlo experiment (cloud of gray points).

In the case of the FD model, the uncertainty in the estimation of  $\delta$  is much larger and spans almost all the allowed values from nearly white noise,  $\delta = 0.12$ , to  $\delta =$ 0.5, with a best estimate of  $\delta = 0.43$ . All these values are broadly consistent with the result in Huybers and Curry (2006). In particular, we find that there is a 10% probability of the estimated parameter corresponding to a nonstationary process (i.e.,  $\delta \rightarrow 0.5$ ). Using Eq. (10), we find that, for  $\delta$  close to the limiting value 0.5, the amplitude of the resulting variations would be inconsistent even with relatively high-variance reconstructions of paleoclimatic data over the past 1-2 millennia (Esper et al. 2012). The presence of poorly known forced responses on these time scales makes it difficult to use paleoclimate data as an explicit quantitative constraint in our analysis, but it does suffice to indicate that the relative stability of the climate of the Holocene would be unlikely if internal variability of the climate system were to conform to an FD process with very high values of  $\delta$ . Based on these arguments, we can ignore the values of  $\delta$ close to the nonstationary limit ( $\delta \rightarrow 0.5$ ). Furthermore, in the appendix, we explore how the estimation of the stochastic model parameters depends on the length of the time series considered and show that values of the parameters corresponding to nonstationary processes are likely to be an artifact of the short length of the time series.

For an algebraically decaying autocorrelation function, there is no associated time scale; therefore, a longmemory process does not have a decay time (Beran 1994). Nevertheless, to have an intuition about the time scales associated to particular values of  $\delta$ , one can calculate the time it takes for the autocorrelation function to reduce to 1/e of its initial value [in analogy with the efolding time for the AR(1) model]. For the best fit value of  $\delta = 0.43$ , for instance, this calculation gives a much longer time than the length of the observational record (156 yr). This suggests that, according to this model, in the 156-yr-long record all points are highly correlated. Overall, we find that, despite the very different time scales that are relevant for the AR(1) and FD characterizations of internal variability, the GHG signal detection statistics are robust for both models.

One interesting question that can be explored using our results is how wrong one would have to get the model parameters of the internal variability in order to change the detection statement of the greenhouse gas signal. In the case of the AR(1) model, we find that the greenhouse gas signal would become not statistically significant in a world in which higher values of  $a_1$  and/or  $a_0$  were needed to describe internal variability. In Fig. 2 (top), we see that, to loose statistical significance, one would have to increase the time correlation characterized by  $a_1$  to more than 0.8 or triple the white noise parameter  $a_0$ .

Thus, the detection statistics for the AR(1) model are very sensitive to the memory parameter and relatively less sensitive to the amount of white noise in the process. Thus, in terms of the global mean temperature internal variability as simulated by GCMs, our findings suggest that the relevant aspect that should be taken into account in a robustness test should be the models' ability to capture correctly the temporal correlations more than the total variance, which is in turn conditioned by their ability to capture the most relevant dynamical processes, their couplings, and feedback mechanisms.

For the FD process, we find a different result. In Fig. 2 (bottom), we can see that, for the estimated  $\sigma_e$ , there is no  $\delta$  for which the process has a greenhouse gas scaling factor that is not statistically significant. Thus, this suggests that the greenhouse gases detection results are robust under changes in the memory parameter. In fact, for very high values of  $\delta$ , one would still need to double the amplitude of the white noise to change the detection statistics. Results in the appendix suggest that, with a longer observational record, we would have estimated a smaller  $\delta$ , but also that the estimated white noise amplitude would not increase significantly. This suggests that if the observed record is relatively short to accurately characterize the memory in the FD model, the detection of the greenhouse gas signal would still be robust when the length of the record increases. In terms of the global mean temperature simulated by GCMs, our results using an FD model suggest that the emphasis should be placed on accurately depicting the amplitude of the white noise in order to be confident about the detection and attribution statistics.

In conclusion, our results suggests that, in the presumably more realistic case in which the internal variability of the global mean temperature is best characterized by a process whose temporal structure lies somewhere in between that of an AR(1) and an FD process, both its temporal correlation structure and the white noise amplitude are important for assessing the robustness of the signals.

To close this section, we include a brief discussion about the robustness of the detection results to the inclusion of the last 7 yr of observations (up until 2012) and the potential effect of the collinearity of the greenhouse gas and sulfates temperature responses. We used the HadCRUT4 dataset to include the last 7 yr of data in  $T_{obs}$ . Differences between the HadCRUT3 global mean temperature time series and the median of the HadCRUT4 global mean temperature time series result in slightly different values of the scaling parameters (see Table 1). Therefore, in order to ensure that the results are comparable, we use only HadCRUT4 data to analyze potential dependencies on the inclusion of

TABLE 1. Scaling factors  $\beta$  obtained from the linear regression when using HadCRUT4 observations for two time periods (1850–2005 and 1850–2012), and the forced temperature responses to VOL, SOL, GHG, and SUL forcings, or to VOL, SOL, and ANT forcings.

	AR(1) 1850–2005	AR(1) 1850–2012	FD 1850–2005	FD 1850–2012
VOL	0.46	0.48	0.51	0.53
SOL	2.26	2.03	1.14	0.99
GHG	0.94	0.71	0.91	0.66
SUL	2.47	1.44	2.04	0.93
VOL	0.54	0.52	0.55	0.53
SOL	0.98	1.24	0.58	0.83
ANT	0.76	0.71	0.81	0.73

the more recent observations and to the number of signals considered.

Figure 3 shows the results of this sensitivity analysis. We observe that if, instead of SUL and GHG signals, we only consider a single total ANT signal, the scaling factors for the latter are smaller than the GHG ones (see Table 1). However, the ANT signal remains detectable for both characterizations of internal variability. Similarly, when adding the last 7 yr of the observed record, the GHG and the ANT signals remain detectable for both noise models, but attribution is lost in the case of the GHG.

#### b. CMIP3 control runs

In this section, we use the same techniques as above to evaluate the control simulations used in the detection and attribution of climate change included in the Fourth Assessment Report (AR4) of the Intergovernmental Panel on Climate Change (IPCC). Our goal is to get some insight about the controls' potential limitations to estimate internal variability and how this might impact in the robustness of the detection and attribution statistics.

We take annual global mean temperature segments from the CMIP3 control simulations that have the same length as the observational record, 156 yr, and fit them to an AR(1) and an FD model. Thus, we characterize each control by a set of parameters:  $a_1$  and  $a_0^2$  when using an AR(1) model and  $\delta$  and  $\sigma_e^2$  for the FD model. The results are indicated in Fig. 2 by numbers representing different GCMs' control segments (see Table 2). In both cases, the spread of points is larger than the spread of the Monte Carlo experiment that characterizes the uncertainty in the estimation of the parameters of the internal variability for the observed record. Note that the number of control segments for each GCM depends on the available number of years of the control simulation in the CMIP3 database. We have taken segments of controls that are fully nonoverlapping and assume that they are independent realizations. Only in the case of the HadCM3 and CGCM3 models is the number of segments (identified by numbers 22 and 1, respectively, in both panels of Fig. 2) large enough to get some intuition about the uncertainty in the estimate of the parameters for those particular GCMs' controls. The spread of the points corresponding to each of these two models suggests that, had we had many more control segments, the uncertainty in the estimation of the parameters would have been given by a cloud of points with a similar spread as the uncertainty estimate for the parameters corresponding to the observational record (gray cloud), and that both uncertainty estimates would have had a significant overlap. However, there are other models for which this is not the case.

The control segments we are investigating are not identical to the ones used in the detection and attribution studies, as their intradecadal variability is typically smoothed (5-yr means) and segments with drift are discarded (Stone et al. 2007). The argument for smoothing the temporal variability of the control segments for the IPCC AR4 is that some modes of internal variability such as ENSO (with a 2–7-yr characteristic scale of variability) are often not properly depicted by all the GCMs, and this would subsequently introduce errors in the estimate of the covariance matrix. In addition, control segments with drifts are discarded attributing the drifts to numerical errors. In our case, the control segments with a drift (Stone et al. 2007) are few and correspond to those with the highest memory parameter values. In the case of the FD model, these are the segments with  $\delta = 0.5$  in Fig. 2 (bottom), and in the case of the AR(1) model, the  $a_1$ values are such that they all lie around the contour line for which the GHG scaling factor is not statistically significant (thick blue contour line).

Interestingly, we find in the appendix that there is a very high correlation between the estimates of  $a_1$  and  $\delta$ and the amplitude of white noise for any given control segment. From the point of view of our analysis, one reason for this is that both stochastic models can separate the same amount of correlated data from the white noise, and each model explains the dynamics with a different memory parameter according to the relevant covariance matrix. As a result, although the underlying physical assumptions are very different in these two models, we find that the numerical value of the autocorrelation function of both models are very similar for the first 156 yr, as expected.

To finish this section, we analyze the power spectra of the climate models' control runs and the observations. In Fig. 4, we show the power spectra of the CMIP3 models' control segments and the power spectra of the residuals from the best fit to  $T_{obs}$ , that is,  $T_{obs} - \hat{\beta}\mathbf{T}$ . The



FIG. 3. The 95% confidence intervals of the scaling factors  $\beta_i$  derived from the multiregression of observed temperature changes onto the BDM estimates of the forced responses to the signals (top) VOL, SOL, and ANT and (bottom) VOL, SOL, GHG, and SUL. The internal variability is represented by an AR(1) model (gray line) or an FD model (black line) for (left) the period 1850–2005 and (right) the period 1850–2012 using HadCRUT4.

latest residuals are the unexplained fluctuations of the climate in our model, after removing the temperature response to the forcings. The figure shows that the power spectra of the residuals are very similar independently of whether the internal variability is characterized as an AR(1) (thick gray line) or an FD process (black line). Since the power spectrum is the Fourier transform of the autocorrelation function, finding similar power spectra is equivalent to finding similar covariance matrices; hence, this figure is consistent with our previous findings about the similarity in magnitude of the autocorrelation functions of the fitted internal variability to the 156-yr observed record. It is clear that a much longer time series is required to appreciate more significant differences in the variability simulated by the two stochastic models.

We can also analyze the link between the ability of a GCM to model different modes of internal variability and the implications for the significance of detection and attribution. It is clear from Fig. 4 that some control segments display peaks corresponding to the ENSO signal with unrealistic high amplitudes, as shown by the high power at the 2–5-yr frequency range. However, Fig. 2 shows that most of these control segments fall in the area of the plots that correspond to a significant greenhouse gas signal. Consistently with the findings in Allen and Tett (1999), this analysis suggests that an accurate depiction of all modes of internal variability might not be required to ensure the robustness of the detection statistics under our detection model.

Finally, our analysis points toward the need to develop a wider range of techniques to assess the robustness of detection and attribution of climate change. The "consistency test" described in Allen and Tett (1999) is equivalent to look at the power spectra of GCM runs

TABLE 2. CMIP3 general circulation models used partly on the IPCC AR4	The order on the table is the same as the numbering in
Figs A1 and A2	

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Model	Full model name	Institute
CGCM3	Canadian Centre for Climate Modelling and Analysis (CCCma) Coupled Global Climate Model, version 3	CCCma, Canada
CGCM3.1(T63)	CCCma Coupled Global Climate Model, version 3.1 (T63 spatial resolution)	CCCma, Canada
CNRM-CM3	Centre National de Recherches Météorologiques (CNRM) Coupled Global Climate Model, version 3	Météo-France/Centre National de Recherches Météorologiques (CNRM), France
CSIRO-Mk3.0	Commonwealth Scientific and Industrial Research Organisation (CSIRO), Mark 3.0	CSIRO Atmospheric Research, Australia
GFDL-CM2.0	Geophysical Fluid Dynamics Laboratory (GFDL) Climate Model, version 2.0	U.S. Department of Commerce/National Oceanic and Atmospheric Administration (NOAA)/GFDL, United States
GFDL-CM2.1	GFDL Climate Model, version 2.1	U.S. Department of Commerce/NOAA/GFDL, United States
GISS-AOM	Goddard Institute for Space Studies (GISS) Atmosphere–Ocean Model	GISS, United States
GISS-AOM		
GISS-EH	GISS Model EH	GISS, United States
GISS-ER	GISS ER	GISS, United States
FGOALS-g1.0	Flexible Global Ocean–Atmosphere–Land System Model gridpoint, version 1.0	LASG/Institute of Atmospheric Physics, China
FGOALS-g1.0 FGOALS-g1.0		
INM-CM3.0	Institute of Numerical Mathematics (INM) Coupled Model, version 3.0	INM, Russia
IPSL-CM4	L'Institut Pierre-Simon Laplace (IPSL) Coupled Model, version 4	IPSL, France
MIROC3.2(hires)	Model for Interdisciplinary Research on Climate 3.2, high-resolution version	Center for Climate System Research (University of Tokyo), NIES, and Frontier Research Center for Global Change (JAMSTEC), Japan
ECHO-G	ECHAM and the global Hamburg Ocean Primitive Equation	Meteorological Institute of the University of Bonn, Germany; Meteorological Research Institute of KMA, South Korea; and Model and Data Group
ECHAM5/MPI-OM	ECHAM5/Max Planck Institute Ocean Model	Max Planck Institute for Meteorology, Germany
MRI-CGCM2.3	Meteorological Research Institute (MRI) Coupled Global Climate Model, version 2.3	MRI, Japan
CCSM3	Community Climate System Model, version 3	National Center for Atmospheric Research (NCAR), United States
PCM1	Parallel Climate Model 1	NCAR, United States
UKMO-HadCM3	Met Office Hadley Centre Coupled Model, version 3	Met Office Hadley Centre, United Kingdom

and compare their (typically) decadal internal variability with the decadal internal variability retained in the residuals of the fit to the observed record. The aim of this test is mainly to discard the possibility of overattributing climate change to the anthropogenic signal only because climate models underrepresent decadal variability. However, studying just the amplitude (or power) of internal variability in Fig. 4 does not give us information about all the possible impacts that a model imperfection might have on the detection and attribution statistics. Thus, there is a need to develop techniques that provide a way to evaluate the impact of specific modes of variability and their interactions, and not just their amplitude, on the detection and attribution of climate change. Many interesting studies have been developed recently (e.g., DelSole et al. 2011), but more work is needed. One advantage of our method is that it does not require the depiction of modes of internal variability accurately, but instead, we can test different assumptions and hypotheses about the internal variability structure by assuming that it can be represented by different physically plausible stochastic models. The generalization of this approach taking into account spatial patterns of variability is work in progress.

#### 4. Conclusions

The IPCC very likely statement that anthropogenic emissions are affecting the climate system is based on the statistical detection and attribution methodology,



FIG. 4. Spectra from the individual GCM control simulations (gray), and the spectra of the residuals of the linear fit to  $T_{obs}$ :  $T_{obs} - \hat{\beta}\mathbf{T}$ , when the internal variability is modeled as an AR(1) (thick gray line) and an FD (black line) process. We use a logarithmic scale in the horizontal axis (period) and the vertical axis (spectral density).

which in turn is strongly dependent on the characterization of internal climate variability as simulated by GCMs.

The understanding of the internal climate variability has been identified as one of the hardest geophysical problems of the twenty-first century (e.g., Ghil 2001). One of the barriers we face to advance our understanding is the lack of long enough reliable observational records. We are then left with the problem of having to characterize internal natural variability with a relatively short observational record that is in fact contaminated by natural and anthropogenic forcings. The alternative to that is to use control simulations of GCMs, with the limitations in this case imposed by the fact that many aspects of the internal variability are poorly represented by the climate models (Newman et al. 2009; DelSole and Shukla 2010; Klein et al. 1999). The way in which these inaccuracies might bias the statistical significance of the detection and attribution results is hard to identify.

In this paper, we test the robustness of the detection and attribution statements in the case of global mean surface air temperature, under different representations of such variability. We use two different physically plausible stochastic models to represent the internal climate variability and investigate the impact of these choices on the significance of the scaling factors in the detection and attribution approach. The two simple stochastic models are chosen to span a wide range of plausible temporal autocorrelation structures and include the shortmemory first-order autoregressive [AR(1)] process and the long-memory fractionally differencing (FD) process. We find that, independently of the representation chosen, the greenhouse gas signal remains statistically significant under the detection model employed in this paper. Thus, our results support the robustness of the IPCC detection and attribution statement for global mean temperature change.

Our results also emphasize the need to apply a wider variety of test to assess the robustness of detection and attribution statistics. Previous studies carried out a "residual consistency test," which is used to assess the GCMs' simulated variability on the scales that are retained in the analysis (Allen and Tett 1999), and tests involving doubling the amplitude of the simulated variability (Tett et al. 1999). However, in the past, variations in the correlation (and hence the memory) of the data have not been taking into account in the sensitivity tests. In the context of our study, the residual consistency test mentioned above is equivalent to exploring the sensitivity of the detection of the greenhouse gas signal to variations in the amplitude of the white noise (i.e., shifts on the horizontal direction only in both the top and bottom panels of Fig. 2). We see that for the AR(1) process, this consistency test is not very helpful, and a more appropriate robustness test should include constraining the values of the correlation parameter. For an FD process, however, the consistency test adequately explores the robustness of the results, as varying the amplitude of the white noise can change their significance.

We conclude by emphasizing that in this study, headline attribution conclusions for GHG and total anthropogenic forcings were found to be insensitive to the choice between two representations of internal variability that were deliberately chosen to span a broad range of behaviors. Nevertheless, we did find that the significance of detection results were affected by the choice of a shortmemory versus a long-memory process, indicating a need for checks on not only the variance but also the autocorrelation properties of internal variability when detection and attribution methods are applied to other variables and regional indices.

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FIG. A1. AR(1) results of estimating (top)  $a_1$  and (bottom)  $a_0^2$  as a function of the length of the control segment sampled from the 1000-yr-long HadCM3 control run.

#### APPENDIX

#### **Estimating the Stochastic Parameters**

We use a HadCM3 control simulation of 1000 yr to assess how the uncertainty of the stochastic parameters depends on the length of the segment, and we refer to this as a finite size effect. We estimate the stochastic parameters from the same control simulation, but increase its length by 20 yr in each step, starting from 99 yr. We do this for both stochastic models considered in this paper, the AR(1) and FD models. In Figs. A1 and A2, the horizontal axis shows the length of the segment and the vertical axis shows the estimated parameter. Figure A1 shows the result for the AR(1) model; in this case, the estimated  $a_1$  oscillates around a fixed value from the beginning. Figure A2 shows the results for the FD model; in this case,  $\delta$  decreases its value until the segment is reaching a length of 300 yr. Given that the observed record is of 156 yr and that the best estimate of the white noise amplitude is larger than what we found for the long HadCM3 control run, we can expect an overestimation of



FIG. A2. FD results of estimating (top)  $\delta$  and (bottom)  $\sigma_e$  as a function of the length of the control segment sampled from the 1000-yr-long HadCM3 control run.



FIG. A3. (top) Correlation between the memory parameter of both stochastic models,  $\delta$  values (vertical axis) vs  $a_1$  values (horizontal axis), obtained from the CMIP3 control segments considered in our analysis. (bottom) As in the top panel, but for the white noise parameter of both stochastic models,  $\sigma_e$  (vertical axis) vs  $a_0^2$  (horizontal axis). Each color corresponds to a different GCM.

the  $\delta$  parameter in the observed 156 yr. Thus, we expect that the 10% probability of  $\delta$  being such that  $\delta > 0.5$  for the Monte Carlo estimation of uncertainty would decrease if we had a longer record.

We also investigated the correlation between the memory parameters and the white noise parameters when fitting an AR(1) and an FD stochastic model to the CMIP3 control segments. Figure A3 (top) shows a very high correlation between  $a_1$  and  $\delta$ ; each color represents a different GCM. Figure A3 (bottom) shows a very high correlation between  $a_0^2$  and  $\sigma_e$ .

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