

# Emissions Trading with Transaction Costs

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## Abstract

We develop an equilibrium model of emissions permit trading in the presence of fixed and proportional trading costs in which the permit price and firms' participation in and extent of trading are endogenously determined. We analyze the sensitivity of the equilibrium to changes in the trading costs and firms' allocations, and characterize situations where the trading costs depress or raise permit prices relative to frictionless market conditions. We calibrate our model to annual transaction data in Phase II of the EU ETS (2008-2012) and find that trading costs in the order of 10 k€ per annum plus 1 € per permit traded substantially reduce discrepancies between observations and theoretical predictions for firms' behavior (e.g. autarkic compliance for small and/or long firms). Our simulations suggest that ignoring trading costs leads to an underestimation of the price impacts of supply-curbing policies, this difference varying with the incidence on firms.

**Keywords** Emissions trading, Transaction costs, Policy design and evaluation, EU ETS.

**JEL codes** D22, D23, H32, L22, Q52, Q58.

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*«Failure to account explicitly for bounded rationality, uncertainty, and informational, contractual and policing costs inherent in all air pollution problems weakens the applicability of [the] conclusions about the allocative efficiency properties of alternative control instruments.»*

— Thomas D. Crocker (1972)

*«Since standard economic theory assumes transaction costs to be zero, the Coase Theorem demonstrates that the Pigovian solutions are unnecessary in these circumstances. Of course, it does not imply, when transaction costs are positive, that [...] regulation or taxation [...] could not produce a better result than relying on negotiations between individuals in the market. [...] My conclusion: let us study the world of positive transaction costs.»*

— Nobel Memorial Prize Lecture, Ronald H. Coase (1992)

## 1 Introduction

Stemming from the seminal works of Coase (1960), Crocker (1966) and Dales (1968) and later formalized by Montgomery (1972), emissions trading has become pivotal in the environmental and climate change mitigation regulatory toolbox.<sup>1</sup> Purportedly, comparative advantages of this instrument include cost effectiveness, modest information requirements for the regulator and a political-economy lever by means of the initial distribution of emissions permits. The collective optimum can in principle be decentralized via the market price: given a total supply of permits, the same price level emerges in equilibrium and abatement efforts are rerouted to firms with lowest marginal abatement costs irrespective of their initial allocation as a result of market participants' endeavor to ferret out least-expensive abatement sources.

As two of the concept's founding fathers recognize in the opening quotes, however, a variety of barriers to trading – usually grouped under the notion of transaction costs – can drive a wedge between theoretical and practical market outcomes. In practice, indeed, frictions of various types are acknowledged to be pervasive as the empirical literature on permit markets attests (e.g. Carlson et al., 2000; Gangadharan, 2000; Hahn & Stavins, 2011; Jaraitė-Kažukauskė & Kažukauskas, 2015; Venmans, 2016; Karpf et al., 2018; Naegel, 2018; Cludius & Betz, 2020) and, more generally, there are costs associated with trading in financial markets (e.g. Gârleanu & Pedersen, 2013; Dávila & Parlato, 2021, and references therein). We corroborate these findings with a descriptive analysis of trading and compliance patterns in the second phase of

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<sup>1</sup>Medema (2020) offers an excellent overview of the historical context and impacts of the Coase theorem. See also Deryugina et al. (2020) for a recent review of its applications to environmental problems.

the EU Emissions Trading System (2008–12) that suggests the existence of transaction costs. This echoes one conclusion of [Hintermann et al. \(2016\)](#) who review the literature on market and price behaviors in EU ETS Phase II, i.e. transaction costs impinge on price formation and may explain persisting differentials in marginal abatement costs across firms.

Yet, surprisingly, the prevalence of transaction costs and their implications for market outcomes as well as for policy design, evaluation and implementation are largely ignored in the theoretical literature on permit markets, with only a few exceptions discussed below.<sup>2</sup> In this paper, we seek to remedy this gap. Specifically, we incorporate trading costs in an otherwise archetypal permit trading model to formally study how they impact the market equilibrium. We also calibrate the model to observed transactions in EU ETS Phase II to offer an illustration based on a relevant real-world example. As we shall see, not only is such a framework better equipped to conduct finer-grained ex-post analyses of firms’ trading and compliance behaviors, but it also constitutes a more realistic basis for ex-ante assessments of supply-side management policies, a regular feature in the hybrid ETSs of today.

We articulate three contributions to the literature. To motivate our analysis further, we begin by exploring the universe of annual transactions in EU ETS Phase II, our policy environment in this paper. Data is available at the account (installation) level but we consider the firm as the relevant decision-making unit for our analysis and we concentrate on inter-firm trading.<sup>3</sup> To aggregate the data at the firm level and remove intra-firm permit reallocations, we develop a consolidation methodology matching each installation to a parent company building on an iterative search procedure for duplicates in the accounts’ information fields. We then utilize the consolidated dataset to scrutinize firms’ annual trading and compliance behaviors. The consolidation methodology and the description of observed firms’ market behavior constitute our first contribution to the empirical literature on the EU ETS.

We find evidence of autarkic compliance and signs of impaired trading, i.e. some gains from trade go unrealized at both the extensive and intensive margins, see [Ellerman et al. \(2010\)](#), [Martin et al. \(2015\)](#) and [Schleich et al. \(2020\)](#) for similar descriptive results. At the extensive margin, about a third of firms did not trade at all on a yearly basis. Autarkic firms are mostly small (in terms of size of emissions or number of installations) representing 9% of regulated emissions and often hold excess permits (w.r.t. realized emissions). At the intensive margin,

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<sup>2</sup>In a related context, see [Dixit & Olson \(2000\)](#) and [Anderlini & Felli \(2006\)](#) for formal analyses of Coasean bargaining in the presence of transaction costs.

<sup>3</sup>A firm typically owns several regulated polluting sites and can redistribute allocated permits across sites based on realized emissions, i.e. it can possibly achieve compliance without effectively trading on the market. Here, we implicitly assume that the costs of intra-firm transfers are negligible compared to those of inter-firm trading. In our dataset, intra-firm transfers represent 27% of all cross-account flows in Phase II.

active firms engaged in trading rather infrequently (typically a few times per year) and only for large enough volumes, suggesting that marginal abatement costs are not equalized across firms in equilibrium. Stifled trade at both margins points us to the prevalence of both fixed and variable transaction costs (see also [Stavins, 1995](#); [Singh & Weninger, 2017](#)).<sup>4</sup>

Our second contribution to the literature is theoretical in nature. We enrich a standard static and deterministic permit trading model by introducing both fixed and proportional trading costs. The fixed cost impacts firms' decisions to take part in the market (extensive margin) while the proportional cost further affects firms' trading choices by driving a wedge between their marginal abatement costs (intensive margin). In our equilibrium framework, the permit price and firms' participation in and extent of trading are determined endogenously, and they depend on the given trading costs and firms' characteristics (i.e. abatement costs and permit allocations, where we let some firms be initially overallocated).<sup>5</sup> Importantly, this framework enables us to study when a market equilibrium exists and if so, how it is achieved.

Tracking trading cost impacts through buyer-seller interactions and resulting market prices, we can analyze the sensitivity of the market equilibrium to changes in the trading costs and firms' initial allocations. While an increase in trading costs always reduces cost effectiveness and the volume of trade, its price effects are ambiguous and non-monotonic in general as they depend on its relative impacts on the supply and demand sides of the market. As a rule, we find that trading costs are conducive to higher price levels when the (theoretical) frictionless market price is 'low', and vice versa. Similarly, the price increase following a reduction in the total number of permits can be amplified or dampened in the presence of trading costs. This hinges on a distribution effect (the overall impact on net permit demand, holding the price constant) and a price effect (the relative price elasticity of net permit demand with vs. without trading costs) which are generally countervailing. To gain additional insight into the market impacts of trading costs, we illustrate our results with analytical and numerical examples for different distributions of the firms' characteristics.

The benchmark framework to analyze the impacts of transaction costs in permit markets has been developed by [Stavins \(1995\)](#) and extended by [Montero \(1998\)](#).<sup>6</sup> Crucially, however, this

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<sup>4</sup>In practice, fixed entry costs can comprise exchange membership fees and resources invested in operating a trading desk, monitoring the market and defining a trading strategy. Variable trading costs can comprise search, information, brokerage, intermediation and consultancy costs inter alia.

<sup>5</sup>As in the related literature (e.g. [Stavins, 1995](#); [Singh & Weninger, 2017](#)) we take trading costs as exogenously given. See [Liski \(2001\)](#) for microfoundations and a formal treatment of trading costs endogenously arising and evolving over time as a function of the market size and the initial distribution of permits.

<sup>6</sup>Specifically, [Montero \(1998\)](#) offered an extension of [Stavins'](#) analysis in the form of uncertainty on trade approval and provided further insights with numerical simulations. Moreover, [Cason & Gangadharan \(2003\)](#) used a laboratory experiment to test (and confirm) the main results implied by [Stavins'](#) theory.

is not an equilibrium framework and the market price is taken as exogenously fixed. That is, [Stavins](#) and [Montero](#) study the impacts of trading costs on an individual firm’s emission and trading choices at the margin but do not formally characterize the market price impacts nor how firms self-select into costly trading in the first place as we do in this paper. As a result, our framework sometimes leads to different results, e.g. market outcomes are sensitive to the initial allocation of permits even with constant marginal trading costs. More recently, [Singh & Weninger \(2017\)](#) have developed a similar equilibrium framework in the presence of fixed or proportional trading costs, alternatively.<sup>7</sup> But in their model, firms are ex-ante identical and differ only in idiosyncratic productivity shocks – the only motive for permit trade. Our analysis is hence different in nature as we choose to focus on what we believe to be the more practically relevant case of ex-ante heterogeneous firms.<sup>8</sup>

This brings us to our third contribution to the literature, which exploits firms’ heterogeneity in abatement costs and allocations allowed by the model. Specifically, we utilize the universe of yearly allocations, emissions, transactions and prices in EU ETS Phase II to discipline the calibration of model parameters and the selection of practically relevant trading costs values. We propose a selection criterion minimizing the total number of sorting errors (i.e. discrepancies between firms’ market participation and net market positions in the model vs. the data) and their dispersion across error types (measured by Shannon’s entropy).<sup>9</sup> Respectively, we find fixed and proportional trading costs in the order of 5-25 k€ per annum and 0.5-1.5 € per permit traded (or 8-11% of the permit price) across years. Relative to zero trading costs, the selected trading costs reduce the total number of sorting errors by 40%, their dispersion by 160%, and can rationalize 70% of autarkic compliance cases. Our model calibration exercise thus shows how accounting for trading costs can be important for ex-post policy evaluation. It also provides first-pass estimates of trading costs in the EU ETS where related empirical studies have gathered anecdotal or indirect evidence (e.g. [Karpf et al., 2018](#); [Zaklan, 2021](#)) or utilized econometric estimation techniques, obtaining results of similar orders of magnitude

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<sup>7</sup>Similarly, in a permit trading model with transaction costs, [Constantatos et al. \(2014\)](#) show how permit allocation can be used as a strategic trade instrument on the product market even without market power.

<sup>8</sup>[Singh & Weninger](#) invoke an argument in the spirit of Samuelson’s Factor Price Equalization theorem whereby in mature ETSs productivity shocks should be the main drivers for trade. While this simplifies their analysis, which accounts for the interaction with the product market, it is our contention that existing ETSs are still far from mature in this respect, and therefore that heterogeneity in abatement costs and allocations remains the main motive for trade. See for instance [Bernard et al. \(2012\)](#) and [Melitz & Redding \(2014\)](#) for similar arguments in the more general context of international trade in goods.

<sup>9</sup>Our calibration methodology also replicates observed annual prices but this cannot be the key selection criterion as it is not robust enough in itself for our purposes (see e.g. [Carlson et al., 2000](#)). Moreover, the price level depends on a variety of other factors our model does not explicitly account for (though we partly control for them). Note also that we focus more on the extensive margin than on the intensive margin impacts of trading costs, as the latter are hard to quantify meaningfully without precise abatement cost data.

(e.g. [Medina et al., 2014](#); [Jaraitė-Kažukauskė & Kažukauskas, 2015](#); [Naegele, 2018](#)).<sup>10</sup>

Finally, we leverage our calibrated model to compare the quantitative results that a modeler or regulator would obtain in assessing the total costs the ETS imposes on firms or the market price impacts of additional supply-curbing policies, depending on whether or not transaction costs are accounted for. In our setting, extra compliance costs resulting from incurred trading costs and foregone efficiency gains are in the order of 7% of the compliance costs in a scenario where transaction costs are ignored. In a similar vein, we find that the price increase following a reduction in the total number of permits would be underestimated if one does not account for transaction costs. This is because in our setting some firms holding excess permits do not offer them for sale due to the transaction costs, implying that the price increase is inefficiently large. Specifically, we find an underestimation factor of two for a one-sixth reduction in the total cap, with variations in size of up to 30-40% depending on its incidence on firms.

The remainder is structured as follows. Section 2 provides background information on transaction costs and trading patterns in EU ETS Phase II. Section 3 develops the permit trading model in the presence of fixed and proportional trading costs and presents our theoretical results. Section 4.1 describes the model calibration and the selection of trading costs. Section 4.2 utilizes the calibrated model to evaluate supply-tightening policy impacts in the presence vs. absence of trading costs. Section 5 contextualizes our results within the existing literature and discusses some limitations of our analysis. Section 6 concludes. An Appendix collects the analytical derivations and proofs (A), analytical and numerical illustrations (B) as well as details on the consolidation methodology (C) and calibration results (D).

## 2 Background

In this section, we first review the related empirical literature on transaction costs in permit markets. We then analyze transaction and compliance data in Phase II of the EU ETS and uncover stylized patterns in firms' market behavior that point us towards the prevalence of pecuniary costs associated with inter-firm trading.

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<sup>10</sup>As we discuss in Section 4.1.2, our calibration metric entails that the calibrated trading costs reflect values that are more relevant for small (often long) firms which exhibit a tendency towards autarkic compliance in our dataset and are known to be subject to larger trading costs than large firms (e.g. [Jaraitė et al., 2010](#); [Naegele, 2018](#)). In Section 5, we also discuss the caveats one must apply when interpreting our calibration results. Specifically, our calibration approach can be seen as providing an upper bound on practically-relevant values for trading costs because it selects them to rationalize autarky and trading decisions based on foregone gains from trade. As a result, it also captures the aggregate impact of other behavioral, dynamic and structural factors that may hinder inter-firm trading but are not formally accounted for in our modeling framework.

## 2.1 Transaction costs and empirical literature

In practice, firms regulated under an ETS face all sorts of non abatement related costs. On the one hand, implementation, regulatory and other administrative costs associated with the monitoring, reporting and verification process account for a large share of collateral regulatory costs (e.g. [Jaraitė et al., 2010](#); [Heindl, 2017](#)). Since they are one-shot, sunk and faced by all firms, they do not affect compliance costs and choices at the margin and have no bearing on market outcomes. On the other hand, firms incur transaction costs entailed by (conditional on) permit trading, the focus of this paper. These include explicit monetary costs such as brokerage and exchange membership fees as well as implicit costs such as search, information, bargaining and internal decision-making costs (e.g. [Hahn & Stavins, 2011](#)).<sup>11</sup>

The vast majority of existing empirical analyses of transaction costs is based on the pioneering US cap-and-trade programs and the EU ETS. For instance, they are found to have decreased trading activity in the Wisconsin’s Fox River program ([Hahn & Hester, 1989](#)) and lowered cost effectiveness by 10-20% in the US lead phasedown program ([Kerr & Maré, 1998](#)). Similarly, in the Los Angeles basin (RECLAIM), [Foster & Hahn \(1995\)](#) analyze trading activity and find that large transaction costs altered market behavior. [Gangadharan \(2000\)](#) econometrically tests the existence and magnitude of transaction costs, finding that they were most influential in the early years of the program, with a decrease in the probability of trading of 32%. Similar evidence exists in the US Acid Rain Program where trading costs were sizable (e.g. [Toyama, 2019](#)) but decreased over time as the market matured and firms gained hands-on experience (e.g. [Joskow et al., 1998](#); [Carlson et al., 2000](#); [Schmalensee & Stavins, 2013](#); [Chen, 2018](#)).

In the EU ETS, we separate how the literature has approached the issue of transaction costs into two strands. The first one describes observed trading and compliance behaviors through surveys of managers’ practices or network-based analyses of transactions. Targeting subparts of the ETS, viz. Belgian ([Venmans, 2016](#)), German ([Heindl, 2012a, 2017](#)), Irish ([Jaraitė et al., 2010](#)), Swedish ([Sandoff & Schaad, 2009](#)) and manufacturing ([Martin et al., 2015](#)) firms, these surveys reveal that permit trading is sparse, used mostly for compliance rather than revenue purposes, and often a subsidiary objective in firms’ business operations. Analyses of patterns in transactions concur to underline the influential role of non-compliance market actors (e.g. [Cludius & Betz, 2020](#)). For instance, [Karpf et al. \(2018\)](#) unveil a hierarchical and assortative trading network structure in which most firms have to resort to local or costly intermediaries, which has implications for price discovery and informational efficiency. Similarly, [Borghesi &](#)

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<sup>11</sup>For instance, the European Energy Exchange (EEX, a major organized trading platform in the EU ETS) charges 2,500 € for an annual trading license plus 3 € per bundle of 1,000 permits.



Flori (2018) show that some national registries are more central than others in the network, and Hintermann & Ludwig (2018) identify a home-country bias in permit trades.

The second strand gathers econometric analyses. Using Phase-I transactions data and firm-level proxies for search and information transaction costs, Jaraitė-Kažukauskė & Kažukauskas (2015) show that the latter significantly influence firms’ decisions to participate in the market and trade directly or indirectly via third parties.<sup>12</sup> They find economies of scale as transaction costs constitute more of an impediment for smaller firms. Their proxies also negatively affect firms’ extent of trading, suggesting that transaction costs have both a fixed and a variable component. Similarly, Schleich et al. (2020) carry out multivariate analyses of firms’ trading behavior over 2005-2015 and find that firms with larger initial permit deficits or surpluses, facing a higher competitive pressure or belonging to the energy sector make a more active and efficient use of the market.<sup>13</sup> Finally, to our knowledge, Naegele (2018) is the only analysis to estimate the magnitude of trading costs over Phase II. She measures entry costs at the firm level as the foregone profits from choosing not to trade, finding median and mean costs of 7 and 21 k€. She also finds that firms holding excess permits are relatively more reluctant to trade, highlighting a key asymmetry between short and long firms – the former are under no compulsion to sell while the latter need to be proactive in one way or another (e.g. buying permits) in order to meet compliance (see also Liu et al., 2017).

## 2.2 Anecdotal evidence in EU ETS Phase II (2008-2012)

**EU ETS.** Every year the EU issues emissions allowances (EUA) through free allocations and auctions, whose total number makes up the cap on emissions. On 30 April of year  $t$ , regulated entities are required to remit the equivalent number of EUAs to cover their verified emissions in calendar year  $t - 1$ , one EUA accounting for one metric ton of carbon dioxide equivalent. Options to demonstrate compliance include abatement of emissions (e.g. production curtailment, input substitution, technological upgrade, end-of-pipe measure), purchasing EUAs on the market, and tapping into one’s bank of EUAs or next-year’s free allocation.<sup>14</sup>

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<sup>12</sup>Transaction costs have a greater impact on firms with a smaller number of installations, less experience with trading (e.g. no in-house trading desk), or no specialized units dealing with emissions abatement. These firms are more likely to trade less frequently or lower volumes, or to trade indirectly, or not to trade at all.

<sup>13</sup>Relatedly, Zaklan (2021) exploits the transition from free allocations to auctions for power producers in 2013 to assess whether emission decisions are independent of allocation, as theory predicts. He finds evidence of transaction costs for small firms (the drop in allocation led to a drop in emission) but not for large firms that make up the bulk of emissions. Independence thus cannot be rejected for the power sector as a whole.

<sup>14</sup>Unrestricted banking of issued EUAs is allowed since 2008 while borrowing is de facto permitted by the overlap between the compliance and allocation cycles, thus limited to year-on-year swaps.



Firms can purchase EUAs on primary markets (i.e. auctions) or trade on secondary markets (i.e. organized exchanges such as ICE and EEX, or over the counter). They may have recourse to registered brokers (i.e. intermediaries) to trade on their behalf. Over Phase II (2008-2012), our period of interest, the yearly averaged total trading volume amounted to 5.6 billion EUAs, about three times the size of the annual emissions caps. Out of these, about 40% were traded over the counter and 60% on exchanges ([European Commission, 2015](#)).

**Data.** Trading activity is recorded in an electronic registry, the EU Transaction Log (EUTL), whose aim is to track the EUA ownership structure across accounts and over time to guarantee an accurate accounting of all issued EUAs. That is, the EUTL records the activity of account holders by keeping track of any EUA transfer, allocation and reconciliation. Unfortunately, it only gathers physical movements on secondary markets so we lack direct information about derivatives (i.e. forwards, futures or options) and primary (i.e. auctions) trading.<sup>15</sup> In Phase II, Member States only marginally exercised their right to auction up to 10% of all allowances with a hefty 96% realized share of free allocations ([European Commission, 2015](#)).

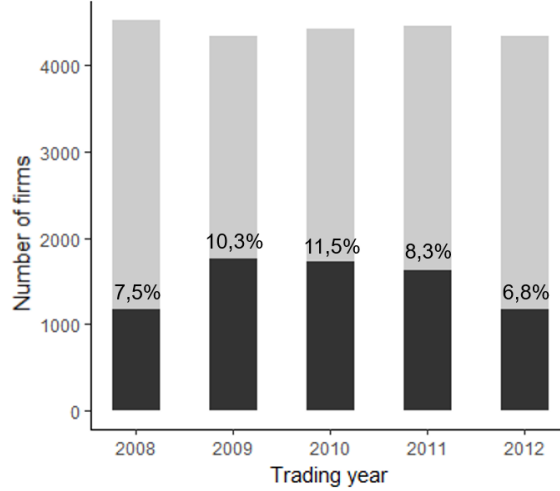
Compliance and transactions are recorded at the polluting site level (one account per installation). As the relevant unit of analysis is the firm (where trading, abatement and compliance decisions can be centralized and coordinated between subsidiary installations) we consolidate the EUTL database from the account to the firm level. Our consolidation methodology and results are described in [Appendix C](#). Our consolidated dataset contains 5,145 firms (binned in six sectors) and transactions between them. Consolidation eliminates intra-firm transfers, which can be used by firms as a primary tool to achieve compliance before having to trade on the market. Namely, a firm can pool the EUAs allocated to its installations in a central account and redistribute them back in accordance with installations' realized emissions. Despite that EUAs changed accounts, they have not explicitly been traded. Such intra-firm redistribution represents 27% of the total volume of transfers in Phase II.

**Observed firms' behavior.** We utilize the consolidated dataset to scrutinize firms' market behavior over Phase II. [Figure 1](#) reports individual annual market participation, showing that around a third of firms do not register any account activity, if not for annual allocation and reconciliation. Notice that autarkic firms are relatively small in size (representing only 9% of overall yearly emissions caps on average) and average number of installations (see [Table C.1](#))

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<sup>15</sup>Derivatives trading represents the biggest share of all transactions but individual trades and positions are not publicly disclosed. Because we aggregate EUTL data at the year level we capture the physical settlements of front-year derivative contracts (but note that the EUTL data do not specify whether transfers took place on an exchange or OTC). Accounting for the small share of auctioned EUAs would be data intensive as it would require obtaining auctions data from all Member States and then link them to EUTL accounts.

Figure 1: Firms' annual market participation in Phase II



*Note:* Grey = participation, black = autarky. Slight year-on-year changes in the number of observations are due to plant closures and new entrants. Percentages indicate the proportions of autarkic firms in volume as a share of the total number of distributed permits each year.

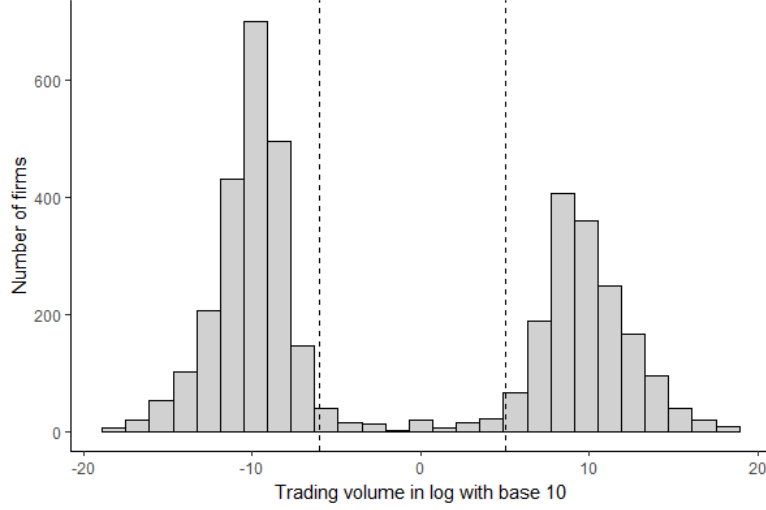
compared to active firms, whatever their sector. This was to be expected due to economies of scale and could point to the existence of *fixed* market entry costs.

We find that about 80% of autarkic firms received more permits than their verified emissions. They held on to their surplus, de facto banking the entirety of their excess permits.<sup>16</sup> Their private bank at the end of Phase II amounted to 140% of their 2012 endowment on average. The remaining 20% of autarkic firms emitted in excess of their annual allocations and engaged in borrowing. On average, these firms frontloaded 30% of their future allocation on a year-on-year rolling basis. [Martin et al. \(2015\)](#) find similar evidence of autarkic banking in Phase II and unveil a threshold effect: some firms start selling excess permits only when their surplus is large enough. As they argue, this behavior could be rationalized by a fixed cost of trading, controlling for other hedging and precautionary saving motives.

Figure 2 depicts the distributions of the volumes of EUA purchases and sales at the firm level in log base 10 for active firms in 2009 (notice that a firm can both buy and sell at different points during the year). We find that active firms rarely engage in trades below some volume cut-off and that they trade infrequently (we record only 4 to 16 transactions per firm per year on average across sectors, see Table C.1). This suggests that a wedge between sellers' and buyers' marginal abatement costs may persist in equilibrium and could point to the existence

<sup>16</sup>Because we do not observe firms' abatement and cannot rule out the implementation of some abatement measures, we cannot distinguish between firms' allocated surplus (e.g. passive banking) and resulting surplus (possibly associated with a proactive abatement and banking strategy). See also Section 5 for a discussion.

Figure 2: Distribution of participating firms' trading  $\log_{10}$  volumes in 2009



*Note:* The two vertical dotted lines demarcate the 5<sup>th</sup> percentiles, departing from zero, for the distributions of firm-level  $\log_{10}$  volumes of cumulative annual purchases (on the right) and sales (on the left).

of variable costs that are *proportional* to the extent (and frequency) of trading.

To summarize, the fact that gains from trade go unrealized at the extensive margin (autarkic firms, Figure 1) as well as at the intensive margin (stifled trade, Figure 2) is suggestive of the existence of both fixed and proportional trading costs.<sup>17</sup> As we shall see below in more detail, fixed costs only impact firms' participation in trading (extensive margin) while proportional costs also affect firms' extent of trading (intensive margin).

### 3 Model

We consider a unitary-mass continuum  $\mathcal{I}$  of cost-minimizing firms indexed by  $i \in \mathcal{I}$  regulated under a market for emission permits. The model is static and assumes away firms' production decisions, i.e. we rule out any incidence or indirect effect of the permit market on the goods markets that the firms serve. In the absence of the permit market, firm  $i$  releases  $u_i$  units of emission, its unregulated emission level, which can be abated at a cost of  $C_i(u_i - e_i)$ , where  $e_i$  are firm  $i$ 's final emissions after end-of-pipe abatement. As is standard, we assume that  $C_i'', C_i''' > 0$  and let  $C_i : a_i \mapsto \alpha_i a_i^2 / 2$  with  $a_i = u_i - e_i \geq 0$ , where we omit the linear term for analytical convenience and without loss of generality up to a translation of the results.

Initial permit allocation is also firm-specific and denoted  $q_i$ . We assume that the overall cap on

<sup>17</sup>As discussed in Section 5, other behavioral, dynamic and structural aspects may also hinder trade.

emissions  $\mathcal{Q}$  is binding relative to overall unregulated emissions  $\mathcal{U}$ ,  $\mathcal{Q} = \int_{\mathcal{I}} q_i di < \mathcal{U} = \int_{\mathcal{I}} u_i di$ . Yet, we allow for overallocation at the firm level, i.e. there exist some firms such that  $u_i < q_i$ , and we let  $\beta_i = u_i - q_i \geq 0$  denote firm  $i$ 's initial permit deficit. In this setting, the two firms' characteristics of interest are thus the  $\alpha_i$ 's and  $\beta_i$ 's, which we assume to be distributed over the bounded supports  $[\underline{\alpha}; \bar{\alpha}]$  and  $[\underline{\beta}; \bar{\beta}]$  where  $0 < \underline{\alpha} < \bar{\alpha} < \infty$  and  $\underline{\beta} < 0 < \bar{\beta} < \infty$ .

### 3.1 Benchmark: Frictionless equilibrium

Under autarky conditions, i.e. when firms cannot trade permits, firm  $i$  abates  $a_i^0 = \max\{0; \beta_i\}$  with  $p_i^0 = \alpha_i a_i^0$  the associated autarkic compliance shadow price. In other words, autarkic compliance implies that short firms abate just as much as to cover their permit deficits  $\beta_i > 0$  while long firms do not use their surplus permits  $-\beta_i > 0$ .

Under frictionless market conditions, i.e. with unrestricted inter-firm permit trading and no trading costs, all firms equate their marginal abatement costs to the prevailing market price  $p$ , i.e.  $\alpha_i(u_i - e_i) = p$  for any firm  $i$ . The sets of buying and selling firms are  $\mathcal{D}(p) = \{i \mid \alpha_i \beta_i > p\}$  and  $\mathcal{S}(p) = \{i \mid \alpha_i \beta_i < p\}$ . Note that a feasible market price must be positive as the cap is binding and it can be no larger than  $\max p_i^0 = \bar{\alpha} \bar{\beta}$  for otherwise no firm would be willing to buy permits. As Appendix A.1 shows, given a feasible market price  $p \in (0; \bar{\alpha} \bar{\beta})$ , individual efficiency gains from permit trading on the market (w.r.t. autarky) write, for any firm  $i$

$$G_i(p) = (p_i^0 - p)^2 / (2\alpha_i) + p \max\{0; -\beta_i\} \geq 0. \quad (1)$$

They consist of two non-negative components. The first is common to all firms and proportional to the squared distance in autarky-market prices. Specifically, selling (resp. buying) firms with  $p_i^0 < p$  (resp.  $p_i^0 > p$ ) find it profitable to abate more (resp. less) than in autarky and sell surplus (resp. purchase missing) permits on the market. The second component only accrues to overallocated firms as they sell the entirety of their initial permit surplus.<sup>18</sup>

Imposing market closure, i.e.  $\int_{\mathcal{I}} (u_i - e_i) di = \mathcal{U} - \mathcal{Q}$ , on top of firm-level optimality conditions defines the frictionless market equilibrium, characterized by the equilibrium price

$$p^* = (\mathcal{U} - \mathcal{Q}) / \int_{\mathcal{I}} di / \alpha_i > 0. \quad (2)$$

As is well known,  $p^*$  is independent of how the  $u_i$ 's and  $q_i$ 's (and thus the  $\beta_i$ 's) are distributed

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<sup>18</sup>This component complements the characterization of the effort-sharing gains in Doda et al. (2019).

among firms. This is the so-called Coasean independence property, i.e. frictionless equilibrium outcomes does not hinge on the initial permit allocation and individual abatement efforts are efficiently reallocated by the market. Note, however, that  $p^*$  depends on the distribution of the  $\alpha_i$ 's.<sup>19</sup> The individual efficiency gains defined in (1) with  $p = p^*$  stem from the cost-effective redistribution of the overall abatement effort  $\mathcal{U} - \mathcal{Q}$  among firms. Specifically, firm  $i$  abates in inverse proportion to  $\alpha_i$ , i.e.  $a_i^* = p^*/\alpha_i > 0$ , and all firms abate in equilibrium, even overallocated ones. We say that the frictionless equilibrium is cost-effective in the sense that (a) all firms are weakly better off participating to the market and (b) marginal abatement costs are equalized between them through the market price.

### 3.2 Equilibrium with trading costs: Characterization

We consider that both permit buyers and sellers incur a market participation cost  $F$  and a proportional trading cost  $T$ . Following Singh & Weninger (2017), trading costs are assumed to be common to all firms and exogenously given.<sup>20</sup> That is, firms have to pay a fixed fee  $F$  to enter the market and trade permits and  $T$  is a mark-up on the permit price  $p$ , i.e. buying firms pay  $p + T$  per permit purchased, selling firms receive  $p - T$  per permit sold.<sup>21</sup>

In the presence of positive trading costs, i.e.  $F > 0$  and/or  $T > 0$ , some firms can be better off under autarky: buying (resp. selling) firms in the frictionless equilibrium can remain buyers (resp. sellers) or prefer not to enter the market altogether (autarkic compliance). We consider that firms make and adjust decisions pertaining to their participation in and extent of trading to minimize individual compliance costs. That is, the only barrier to cost-effectiveness occurs in the form of trading costs – see Section 5 for a discussion of other barriers. We also assume that all firms fully acquit their compliance obligations (see e.g. Stranlund, 2017).

Specifically, when  $F > 0$  and  $T = 0$ , the market outcome is not cost-effective at the extensive margin (some firms do not participate in the market so that some trades that would otherwise be mutually beneficial go unrealized) but it remains cost-effective at the intensive margin (all

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<sup>19</sup> $p^*$  is proportional to the stringency of the overall constraint on emissions set by the cap, i.e.  $\mathcal{U} - \mathcal{Q}$ , and the harmonic mean of  $\{\alpha_i\}_i$ . Thus the more skewed  $\{\alpha_i\}_i$  towards lower values, the lower  $p^*$  and vice versa.

<sup>20</sup>This assumption enables both analytical tractability and model calibration. In practice, trading costs can be firm specific and have non-zero curvature, e.g. convexity is generally considered in finance (e.g. Gârleanu & Pedersen, 2013; Dávila & Parlato, 2021). To simplify, we assume that variable costs are linear in traded volume and we do not attempt to model how trading costs may arise endogenously (see e.g. Liski, 2001).

<sup>21</sup>In practice, the equilibrium price may also depend on how trading costs are distributed among buyers and sellers. Exogenously fixing how trading costs are shared between firms simplifies analytical computations in our multilateral trading framework, see Quemén & de Perthuis (2019) for a formal treatment of endogenously determined transaction prices in an analogous setting with regulatory restrictions on bilateral permit trading.

mutually beneficial trades materialize between participating firms as their marginal abatement costs are equalized). When  $T > 0$  and  $F = 0$ , cost-effectiveness at the intensive margin further drops as participating firms abate in proportion to the actual permit price that they face, i.e. inclusive of the proportional trading cost, which drives a wedge of size  $2T$  between buyers' and sellers' marginal abatement costs in equilibrium.

Hence, given a market permit price  $p$  and a proportional trading cost  $T < p$ , firm  $i$  will find it profitable to buy (resp. sell) permits on the market provided that  $p_i^0 > p+T$  (resp.  $p_i^0 < p-T$ ). Additionally, given a market participation cost  $F \geq 0$ , a buying (resp. selling) firm  $i$  will trade permits on the market when its efficiency gains from permit trading net of both trading costs  $G_i(p+T) - F$  (resp.  $G_i(p-T) - F$ ) are positive. As Appendix A.2 shows, firm  $i$  is better off buying permits when

$$p < \bar{p}_i = \alpha_i \beta_i - T - \sqrt{2\alpha_i F}. \quad (3)$$

Symmetrically, firm  $i$  is better off selling permits when

$$\begin{aligned} p > \underline{p}_i &= \alpha_i \beta_i + T + \sqrt{2\alpha_i F} \text{ if } \beta_i > 0 \\ \text{or when } p > \underline{p}_i &= \alpha_i \beta_i + T + \sqrt{\alpha_i^2 \beta_i^2 + 2\alpha_i F} \text{ if } \beta_i \leq 0. \end{aligned} \quad (4)$$

Intuitively, firm  $i$  will purchase permits only if the market price is below its autarkic shadow price  $p_i^0 = \alpha_i \beta_i$  adjusted for the fixed and proportional trading costs (note  $\bar{p}_i$  is decreasing with  $F$  and  $T$ ). Symmetrically, firm  $i$  will sell permits only if the market price is above its cost-adjusted autarkic shadow price  $\underline{p}_i$  (which is increasing with  $F$  and  $T$ ). As Appendix A.3 shows, the sets of buying and selling firms are defined by

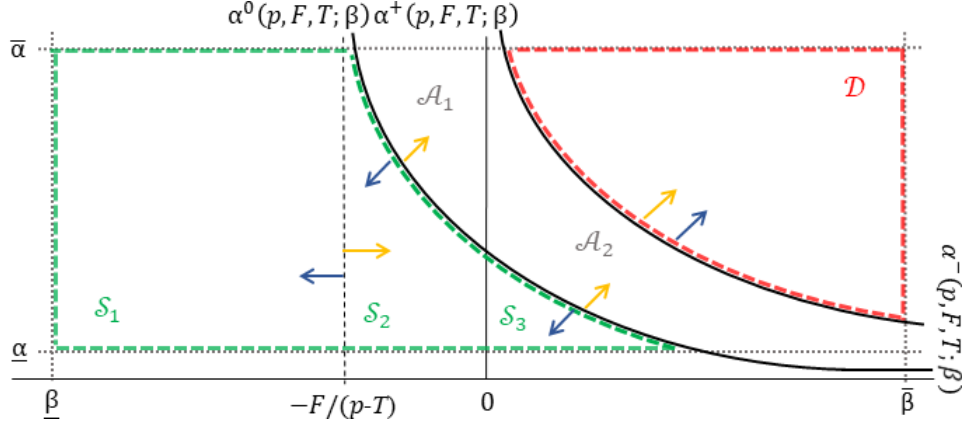
$$\begin{aligned} \mathcal{D}(p, F, T) &= \{i \mid \alpha_i > \alpha^+(p, F, T; \beta_i) \wedge \beta_i > 0\}, \\ \text{and } \mathcal{S}(p, F, T) &= \left\{ \{i \mid \alpha_i < \alpha^-(p, F, T; \beta_i) \wedge \beta_i > 0\} \cup \{i \mid \alpha_i < \alpha^0(p, F, T; \beta_i) \right. \\ &\quad \left. \wedge -F/(p-T) < \beta_i \leq 0\} \cup \{i \mid \beta_i \leq -F/(p-T)\} \right\}, \end{aligned} \quad (5)$$

and  $\mathcal{A}(p, F, T) = \mathcal{I} \setminus \{\mathcal{D}(p, F, T) \cup \mathcal{S}(p, F, T)\}$  denotes the set of autarkic firms, where

$$\begin{aligned} \alpha^\pm(p, F, T; \beta) &= \left( F + (p \pm T)\beta \pm \sqrt{F(F + 2(p \pm T)\beta)} \right) / \beta^2 > 0, \\ \text{and } \alpha^0(p, F, T; \beta) &= (p - T)^2 / (2(F + (p - T)\beta)) > 0. \end{aligned} \quad (6)$$

$\mathcal{D}$  and  $\mathcal{S}$  are of decreasing measure as  $F$  or  $T$  increases and  $\mathcal{D}$  (resp.  $\mathcal{S}$ ) is of decreasing (resp. increasing) measure as  $p$  increases, ceteris paribus. Importantly, with  $F = 0$  and  $T > 0$ , one

Figure 3: Market participation frontiers given price  $p$  and trading costs  $F$  and  $T$



Note: Blue (resp. yellow) arrows indicate how frontiers move in response to an increase in  $F$  and  $T$  (resp.  $p$ ).

has  $\mathcal{D} = \{i | \alpha_i > (p + T)/\beta_i \wedge \beta_i > 0\}$  and  $\mathcal{S} = \{\{i | \alpha_i < (p - T)/\beta_i \wedge \beta_i > 0\} \cup \{i | \beta_i \leq 0\}\}$ . That is, overallocated firms would always find it profitable to sell their extra permits at a price  $p > T$  so in our model a fixed entry cost is necessary to have that some overallocated firms prefer autarky over market participation.

For admissible values of  $F$ ,  $T$  and  $p$ , Figure 3 maps the zones where buying (red), selling (green) and autarkic (grey) firms are located in the  $(\alpha, \beta)$ -space. It is worthwhile describing firms' behavior in each zone, and we proceed from left to right and bottom to top:

- $\mathcal{S}_1$  When  $\beta_i \leq -F/(p - T)$ , firm  $i$  more than recovers the fixed cost by just selling its initial surplus  $(-\beta_i(p - T) \geq F)$ . Because this comes at no other cost for firm  $i$ , this holds whatever its marginal abatement cost  $\alpha_i$ . Moreover, firm  $i$  finds it profitable to also abate  $(p - T)/\alpha_i > 0$  and sell the corresponding amount of freed-up permits.<sup>22</sup>
- $\mathcal{S}_2$  When  $-F/(p - T) < \beta_i \leq 0$ , selling the initial surplus is not enough to cover the fixed cost. Because firm  $i$  can abate at a sufficiently low cost at the margin (i.e.  $\alpha_i < \alpha^0$ ), it make profits by selling both surplus and freed-up permits  $(p - T)/\alpha_i - \beta_i$ .
- $\mathcal{A}_1$  When  $-F/(p - T) < \beta_i \leq 0$ , selling the initial surplus is not enough to cover the fixed cost. Because firm  $i$  cannot abate at a sufficiently low cost at the margin (i.e.  $\alpha_i > \alpha^0$ ), it is better off under autarky, i.e. not using its surplus permits and not abating.
- $\mathcal{S}_3$  When  $\beta_i > 0$  but small and abatement is sufficiently cheap at the margin (i.e.  $\alpha_i < \alpha^-$ ) firm  $i$  abates to both meet compliance and sell some freed-up permits  $(p - T)/\alpha_i - \beta_i$ .

<sup>22</sup>With  $p$  given, one might think that firm  $i$  abates less than when  $T = 0$  by  $T/\alpha_i$ . However, because  $p$  in equilibrium hinges on the trading costs, one cannot conclude prima facie. This applies to all zones.



$\mathcal{A}_2$  When  $\beta_i > 0$  is relatively larger and/or abatement is relatively less cheap at the margin (i.e.  $\alpha^- \leq \alpha_i \leq \alpha^+$ ) firm  $i$  is better off abating its deficit only so as to comply without entering the market and incurring the associated trading costs.

$\mathcal{D}$  When  $\beta_i > 0$  becomes larger and/or abatement becomes more expensive at the margin (i.e.  $\alpha_i > \alpha^+$ ) firm  $i$  is better off incurring the trading costs so as to purchase permits to cover some portion of its deficit, the remainder being abated internally.

Therefore, permit supply and demand functions can then be defined as follows

$$S(p, F, T) = \int_{S(p, F, T)} (a_i^*(p - T) - \beta_i) di \text{ and } D(p, F, T) = \int_{D(p, F, T)} (\beta_i - a_i^*(p + T)) di, \quad (7)$$

where  $a_i^*(x) = x/\alpha_i$  is participating firm  $i$ 's optimal abatement decision given the net permit price  $x = p \pm T$ . With  $V = S - D$  the net supply function, we have the following result.

**Proposition 1.** *The fixed and proportional trading costs  $F$  and  $T$  are admissible when*

$$F < \bar{\alpha}\bar{\beta}^2/2 \text{ and } 2T + \sqrt{\beta^2\alpha^2 + 2\alpha F} + \sqrt{2\bar{\alpha}F} < \bar{\alpha}\bar{\beta} - \alpha\beta. \quad (8)$$

*Given admissible trading costs  $F$  and  $T$ , there exists a unique permit price  $\hat{p}$  that clears the market, i.e.  $V(\hat{p}, F, T) = 0$ , which is bounded by*

$$\beta\alpha + T + \sqrt{\beta^2\alpha^2 + 2\alpha F} < \hat{p} < \bar{\alpha}\bar{\beta} - T - \sqrt{2\bar{\alpha}F}. \quad (9)$$

*Proof.* See Appendix A.4. □

Trading costs are said admissible when positive supply and demand can emerge on the market (roughly speaking, provided that they are not too large). When this is not the case, i.e. one of the two conditions given in (8) does not hold, the market breaks down. To possibly clear the market, feasible price levels are necessarily bounded by the participation price thresholds of the last potential permit buyer  $(\bar{\alpha}, \bar{\beta})$  and seller  $(\alpha, \beta)$  on the market as given in (3-4).

Proposition 1 ensures the existence and uniqueness of a market equilibrium in the presence of admissible fixed and proportional trading costs. Except with zero costs where the equilibrium collapses to the frictionless one, i.e.  $V(p^*, 0, 0) = 0$ ,  $\hat{p}$  does not admit a general closed-form solution. We thus turn to comparative statics to derive some properties of the equilibrium.

### 3.3 Equilibrium with trading costs: Some properties

In this section, we leverage the equilibrium framework developed in Section 3.2 to extend the comparative static results in Stavins (1995) and Montero (1998). Specifically, we analyze the sensitivity of market equilibrium outcomes to incremental changes in the trading costs and firms' permit allocations. We complement our formal analysis with analytical examples.

#### 3.3.1 Impacts of a change in trading costs

Consider an arbitrarily small increase  $dK > 0$  in the trading cost  $K = F$  or  $T$ . By virtue of the implicit function theorem, the resulting price response  $d\hat{p}$  in the vicinity of the equilibrium reads

$$\frac{d\hat{p}}{dK} = -\frac{\partial V(\hat{p}, F, T)/\partial K}{\partial V(\hat{p}, F, T)/\partial p} \gtrless 0, \quad (10)$$

which cannot unambiguously be signed. While  $\partial V/\partial p > 0$ , the sign of  $\partial V/\partial K$  is indefinite and depends on the relative magnitudes of the demand and supply responses to the trading cost increase.<sup>23</sup> For instance, when demand is more responsive than supply, i.e.  $|\partial D/\partial K| > |\partial S/\partial K|$ , then  $d\hat{p}/dK < 0$ . In words, the equilibrium price is lowered as demand is relatively more constricted than supply, and vice versa. As a corollary, it follows that

$$\hat{p} \gtrless p^*, \quad (11)$$

depending on the distributions of the firms' characteristics  $\alpha_i$  and  $\beta_i$  and the levels of the trading costs. This showcases the break-down of the Coasean independence property in the presence of trading costs. Further taking the total differentials of supply and demand yields

$$\frac{dS}{dK} = \underbrace{\frac{\partial S}{\partial K}}_{<0} + \underbrace{\frac{\partial S}{\partial p}}_{>0} \underbrace{\frac{d\hat{p}}{dK}}_{\gtrless 0} \quad \text{and} \quad \frac{dD}{dK} = \underbrace{\frac{\partial D}{\partial K}}_{<0} + \underbrace{\frac{\partial D}{\partial p}}_{<0} \underbrace{\frac{d\hat{p}}{dK}}_{\gtrless 0}, \quad (12)$$

which, on the face of it, cannot unambiguously be signed either. Yet,  $dS/dK = dD/dK$  must hold in equilibrium,<sup>24</sup> which in conjunction with (12) implies that  $dS/dK = dD/dK < 0$ . In words, an increase in the trading costs always lowers the equilibrium volume of trade.

As a result, the total regulatory control costs, i.e. the costs of abatement and trading summed over all firms, always increase as  $K$  rises. Because firms choose whether to trade or not, and if

<sup>23</sup>Note that even taking (10) in the small as  $F$  and/or  $T \rightarrow 0$  also yields an indefinite sign.

<sup>24</sup>One can formally see this by unpacking (10) with  $V = S - D$  and term identification with (12).

so the extent thereof, by minimizing their compliance costs, there exists a decreasing mapping between the total volume of trade (which measures the degree of cost-effective reallocation of abatement among firms) and the total control costs. In words, an increase in the trading costs negatively impacts welfare by consuming more monetary resources and stifling more trades which otherwise would have been mutually beneficial, both at the extensive and intensive margins. Proposition 2 summarizes the above results.

**Proposition 2.** *In response to an increase in the fixed or proportional trading cost, the equilibrium volume of trade (resp. total regulatory control costs) always decreases (resp. increases) and vice versa. However, the market equilibrium price may increase or decrease.*

To illuminate our general results, we exclusively focus on the equilibrium price impacts of a shift in the trading costs for two reasons. First, because Stavins (1995) and Montero (1998) shut down this channel in their comparative static analyses of trading costs. Second, because price impacts can go both ways, it is worthwhile investigating their determinants per se.

To go beyond the equilibrium sensitivity to incremental changes in the trading costs characterized in Proposition 2, we provide analytical examples below. Specifically, we consider two simple cases for the distributions of the firms' characteristics in which we are able to derive implicit closed-form solutions for the equilibrium price that lend themselves to economic interpretation. To gain further insight into the price impacts of trading costs, three numerical examples in more general cases are developed in Appendix B.2.

**Analytical examples.** We primarily focus on the price impacts of the fixed trading cost, i.e. we let  $F \geq 0$  and  $T = 0$ . We also let firms be homogeneous in terms of initial net deficit, i.e.  $\beta_i = \beta = \mathcal{U} - \mathcal{Q} > 0$  for all  $i$  in  $\mathcal{I}$ , and proceed with two alternative distributions of the  $\alpha_i$ 's, namely

$$g_1(x) = 2x/(\bar{\alpha}^2 - \underline{\alpha}^2) \text{ and } g_2(x) = \bar{\alpha}\underline{\alpha}/(x^2(\bar{\alpha} - \underline{\alpha})),$$

for  $x \in [\bar{\alpha}; \underline{\alpha}]$  and  $g_{1,2}(x) = 0$  elsewhere. These density functions are normalized to a unitary mass and cherry-picked to ensure both analytical tractability and clear-cut results which are otherwise hard to come by.<sup>25</sup> They represent two opposite distributions of the  $\alpha_i$ 's, which is skewed towards high (resp. low) values with  $g_1$  (resp.  $g_2$ ). The sketches of the derivations leading to the following results are gathered in Appendix B.1.

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<sup>25</sup>For instance, when  $\{\alpha_i\}_i$  is uniformly distributed we arrive at an analytically intractable transcendental equation in  $\hat{p}$ . The ordering between  $\hat{p}$  and  $p^*$  thus depends on  $F$  in a non-straightforward way.

**Case 1.** Fix  $\beta_i = \beta > 0$  for all  $i$  in  $\mathcal{I}$  and let  $g = g_1$ . Then  $\hat{p}_1$  is implicitly defined by

$$\hat{p}_1 + \frac{2F\sqrt{F(F + 2\beta\hat{p}_1)}}{\beta^3(\bar{\alpha} - \underline{\alpha})} = p_1^*, \quad (13)$$

where  $p_1^* = \beta(\bar{\alpha} + \underline{\alpha})/2$ . In this case,  $\hat{p}_1 \leq p_1^*$  with equality in  $F = 0$  and  $d\hat{p}_1/dF < 0$ .

**Case 2.** Fix  $\beta_i = \beta > 0$  for all  $i$  in  $\mathcal{I}$  and let  $g = g_2$ . Then  $\hat{p}_2$  is implicitly defined by

$$\hat{p}_2 - \frac{4F\bar{\alpha}^2\underline{\alpha}^2}{(\bar{\alpha}^2 - \underline{\alpha}^2)\hat{p}_2^3}\sqrt{F(F + 2\beta\hat{p}_2)} = p_2^*, \quad (14)$$

where  $p_2^* = 2\beta\bar{\alpha}\underline{\alpha}/(\bar{\alpha} + \underline{\alpha})$ . In this case,  $\hat{p}_2 \geq p_2^*$  with equality in  $F = 0$  and  $d\hat{p}_2/dF > 0$ .

Observe that  $p_1^* > p_2^*$ . Indeed, with a homogeneous deficit  $\beta$  across firms the frictionless price is higher the more skewed the distribution of the  $\alpha_i$ 's towards high values. Crucially, a fixed trading cost tends to mitigate this. When the  $\alpha_i$ 's are tilted towards high values, introducing or increasing the fixed cost tends to evict more firms with a high  $\alpha_i$  (i.e. demanders) than with a low  $\alpha_i$  (i.e. suppliers), ceteris paribus. This entails that demand is more constricted than supply, hence a downward pressure on the price. The converse holds when the  $\alpha_i$ 's are skewed towards low values as a higher fixed cost shrinks supply more than demand, ceteris paribus. This suggests that a fixed trading cost tends to have a tempering effect on the price when the frictionless price is 'high' – and conversely, it tends to hike  $\hat{p}$  when  $p^*$  is 'low'.

### 3.3.2 Impacts of a change in total supply and individual allocations

We now study the equilibrium price impacts of a shift in total supply and firm-level allocations in the presence of constant trading costs. We refer the reader to [Stavins \(1995\)](#) and [Montero \(1998\)](#) for illustrations of how the total volume of trade and compliance costs vary with firms' initial allocations. Compared to these comparative static analyses taking the perspective of a given firm (i.e. assuming the market price is invariant), we use our equilibrium framework to analyze the case where all firms' allocations can vary simultaneously, which affects both the market price and firms' trading decisions. This in turn leads to different results. Contrary to [Stavins \(1995\)](#) for instance, the way permits are allocated among firms does affect equilibrium outcomes even with linear marginal trading costs.

We consider an arbitrarily small variation in  $\{\beta_i\}_i$ , i.e. we let  $\beta_i$  change to  $\beta_i + d\beta_i$  for all  $i$  in  $\mathcal{I}$ , possibly with  $d\beta_i \neq d\beta_j$ , and then let the price adapt to  $\hat{p} + d\hat{p}$  so that  $V(\hat{p} + d\hat{p}, F, T) = 0$  remains satisfied. This is tantamount to taking the total differential of  $V(\hat{p}, F, T) = 0$  w.r.t.  $\hat{p}$

and all  $\beta_i$ 's. With a slight abuse of notation for the partial derivatives w.r.t. the  $\beta_i$ 's, one has

$$\frac{\partial V(\hat{p}, F, T)}{\partial p} d\hat{p} + \int_{\mathcal{I}} \frac{\partial V(\hat{p}, F, T)}{\partial \beta_i} d\beta_i di = 0. \quad (15)$$

For the sake of the argument, we here only consider induced changes at the intensive margin (i.e. within  $\mathcal{S}$  and  $\mathcal{D}$  as given prior to the change in  $\{\beta_i\}_i$ ) and ignore those at the extensive margin (i.e. changes due to the shifts in the locations of the participation frontiers in Figure 3). Extensive margin impacts, which render the exposition more complex but do not change the nature of the results, are formally treated and discussed in Appendix A.5.

Noting that  $\frac{\partial V}{\partial \beta_i} = - \int_{\mathcal{S}(\hat{p}, F, T) \cup \mathcal{D}(\hat{p}, F, T)} \delta(j = i) dj$  where  $\delta(\cdot)$  denotes the Dirac distribution, (15) simplifies to

$$\frac{\partial V(\hat{p}, F, T)}{\partial p} d\hat{p} = \int_{\mathcal{S}(\hat{p}, F, T) \cup \mathcal{D}(\hat{p}, F, T)} d\beta_i di, \quad (16)$$

meaning that the sign and magnitude of  $d\hat{p}$  hinge upon the overall net change in the  $\beta_i$ 's over  $\mathcal{S}(\hat{p}, F, T) \cup \mathcal{D}(\hat{p}, F, T)$ . This is because allocation changes for autarkic firms have no market impacts given our exclusive focus on the intensive margin impacts. Interestingly, note that the mere reshuffling of individual allocations, while keeping total supply invariant, may also influence the price outcome as the  $d\beta_i$ 's may not cancel out over  $\mathcal{S}(\hat{p}, F, T) \cup \mathcal{D}(\hat{p}, F, T)$ .

Now consider that total supply is tightened by  $dQ > 0$  and that the tightening is uniformly distributed among all firms.<sup>26</sup> Because  $\mathcal{I}$  is of mass one, we have that  $d\beta_i = dQ$  for all  $i$ . If we let  $|\cdot|$  denote the mass (or measure) of a set, (16) then rewrites

$$\frac{d\hat{p}}{dQ} = \frac{|\mathcal{S}(\hat{p}, F, T)| + |\mathcal{D}(\hat{p}, F, T)|}{\partial V(\hat{p}, F, T)/\partial p} > 0, \quad (17)$$

that is, the price response to the tightening is always positive in the presence of trading costs. But how does its magnitude compare to that in the frictionless case? Without trading costs, (16) reads

$$\frac{\partial V(p^*, 0, 0)}{\partial p} dp^* = \int_{\mathcal{I}} d\beta_i di = dQ, \quad (18)$$

so that

$$\frac{d\hat{p}/dQ}{dp^*/dQ} = \underbrace{\left( |\mathcal{S}(\hat{p}, F, T)| + |\mathcal{D}(\hat{p}, F, T)| \right)}_{\text{distribution effect} \leq 1} \underbrace{\frac{\partial V(p^*, 0, 0)/\partial p}{\partial V(\hat{p}, F, T)/\partial p}}_{\text{price effect} \geq 1} \geq 1. \quad (19)$$

The ordering of  $d\hat{p}$  and  $dp^*$  is ambiguous in general and hinges on two countervailing forces. First, the overall impact on the net demand for permits (holding the price constant) relative

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<sup>26</sup>Two alternative firm-level distributions of the tightening are considered in Appendix A.5.

to that without trading costs which ultimately depends on how the tightening is distributed among firms. In the intensive margin only case, for a given incidence of the tightening, this *distribution effect* always works to mitigate the price increase, all the more so that trading costs are large and the mass of autarkic firms is sizable. Second, the ratios of the sensitivities of the net supply functions to a price change with and without trading costs. In the intensive margin only case, this *price effect* always works to magnify the price increase, all the more so that trading costs are large.<sup>27</sup> This yields the overall ambiguous effect in (19).

We now state the following result in the general case of any change in supply inclusive of the induced impacts at both the intensive and extensive margins.

**Proposition 3.** *The market price response to a supply change can be amplified or dampened in the presence of trading costs relative to frictionless conditions. This hinges on a distribution effect (the relative impact on net permit demand holding the price constant) and a price effect (the relative price elasticity of net permit demand) which are generally countervailing.*

*Proof.* See Appendix A.5. □

In the general case the distribution and price effects can be greater or lower than one. Specifically, the distribution (resp. price) effect is likely to be predominantly lower (resp. greater) than one, except possibly when trading costs are small. In particular, when  $F = 0$ , the extensive margin effects are nil so that this case collapses to the above analysis. Appendix A.5 also discusses how the magnitude of the distribution effect depends on the type of firm-level incidence of the supply change. We now turn to analytical examples.

**Analytical examples (cont'd).** We consider that pursuant to some regulatory amendment overall supply  $\mathcal{Q}$  is reduced by an arbitrarily small amount  $d\mathcal{Q} > 0$ , which translates into a small increase  $d\beta = d\mathcal{Q}$  in the firms' uniform deficit. We have the following results.

**Case 1.** The market price response to a small uniform supply tightening of  $d\beta$  is positive, i.e.  $d\hat{p}_1/d\beta > 0$ . However, only when  $\hat{p}_1$  is not too small does it hold that  $d\hat{p}_1/d\beta \geq dp_1^*/d\beta > 0$ , specifically when  $(p_1^* - 3F/\beta)/5 \leq \hat{p}_1 \leq p_1^*$ .

**Case 2.** The market price response to a small uniform supply tightening of  $d\beta$  is positive, i.e.  $d\hat{p}_2/d\beta > 0$ . However, only when  $\hat{p}_2$  is not too large does it hold that  $d\hat{p}_2/d\beta \geq dp_2^*/d\beta > 0$ , specifically when  $p_2^* \leq \hat{p}_2 \leq p_2^* + \sqrt{p_2^*(p_2^* + 3F/(2\beta))}$ .

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<sup>27</sup>Since  $|\mathcal{S}| + |\mathcal{D}| \leq |\mathcal{I}| = 1$ , *distribution effect*  $\leq 1$  and decreases as  $|\mathcal{A}|$  increases.  $\partial V(p^*, 0, 0)/\partial p = \int_{\mathcal{I}} di/\alpha_i$  while  $\partial V(\hat{p}, F, T)/\partial p = \int_{\mathcal{S} \cup \mathcal{D}} di/\alpha_i$  so *price effect*  $\geq 1$ . See Appendix A.5 for more details.

Intuitively, tightening supply always implies higher price levels in the presence of a fixed cost, but the price rise can be magnified or dampened relative to frictionless conditions. The two cases suggest that the price response is more likely to be magnified in the presence of a fixed cost when  $\hat{p}$  is not too distant from  $p^*$  prior to the tightening, *ceteris paribus*. In Appendix B.2, we investigate this further with numerical examples.

## 4 Illustration

In this section, we illustrate our theoretical results based on actual market data. Specifically, we consider the universe of allocations, emissions, transactions and prices in Phase II of the EU ETS (2008-2012) to discipline both the calibration of model parameters and the selection of practically relevant values for the fixed and proportional trading costs. We next leverage our calibrated model to compare the relative implications of various supply-tightening policies in terms of market price responses and compliance costs, with and without trading costs.

### 4.1 Calibration to EU ETS Phase II

We utilize our transaction and compliance database consolidated at the firm level to calibrate the model parameters for each year in Phase II. We proceed in two steps. First, we infer yearly firms' characteristics  $(\alpha_{i,t}, \beta_{i,t})$  conditional on given pairs of trading costs  $(F, T)$ . Second, we select the trading cost pair that best rationalizes firms' observed participation in trading and, where applicable, the sign of their net market positions.

#### 4.1.1 Inferring firms' characteristics with given trading costs

Yearly initial allocations and verified emissions are readily available at the polluting unit (or account) level from the EUTL which we consolidate at the firm level (see Appendix C for the methodology). We respectively denote them  $q_{i,t}^r$  and  $e_{i,t}^r$  for firm  $i$  in year  $t$ . We also compute yearly-averaged EUA prices  $p_t^r$  using ICE data (daily futures). Except for the consolidation procedure, this is quite straightforward. Next, we need to make assumptions to set firms' yearly baseline emissions and marginal abatement cost slopes, which are both unobservable quantities, and to control for banking and borrowing in our static setting. In a context where relevant quantities are scarce or hard to reconstruct *ex post*, we opt for workable assumptions allowing for a first-pass yet reasonable model calibration.



We set year- $t$  baseline emissions  $u_{i,t}$  as the moving averages of  $i$ 's verified emissions over the three preceding years  $t - 3$  to  $t - 1$ . This captures the persistence in emissions demand over time and a steadily declining aggregate trend (e.g. [Quemin & Trotignon, 2021](#)).<sup>28</sup> Next, we set firms' marginal abatement cost slopes based on the equimarginal value principle applied to the overall permit price (i.e. the market price adjusted for the proportional trading cost) using observed prices  $p_t^r$  and implied abatement levels  $u_{i,t} - e_{i,t}^r$ . The imputed  $\alpha_{i,t}$ 's thus need to be conditioned on observed market participation decisions and net positions, that is

$$\alpha_{i,t} = \begin{cases} (p_t^r + T)/(u_{i,t} - e_{i,t}^r) & \text{if } i \in \mathcal{D}_t^r \\ (p_t^r - T)/(u_{i,t} - e_{i,t}^r) & \text{if } i \in \mathcal{S}_t^r \\ p_t^r/(u_{i,t} - e_{i,t}^r) & \text{if } i \in \mathcal{A}_t^r \end{cases} \quad (20)$$

where  $\mathcal{D}_t^r$ ,  $\mathcal{S}_t^r$  and  $\mathcal{A}_t^r$  are the sets of observed net buying, net selling and autarkic firms in year  $t$ , respectively. In (20) we assume that autarkic firms treat the permit price as a relevant signal to guide their abatement decisions even though they do not effectively trade.

We then adjust firms' allocations for the market's temporal dimension that our static model does not capture, i.e. we compute effective allocation levels net of intertemporal intra-firm redistribution.<sup>29</sup> To that end, we begin by imputing firms' permit bank dynamics as

$$b_{i,t}^r = b_{i,t-1}^r + q_{i,t}^r + x_{i,t}^r - e_{i,t}^r, \quad (21)$$

where  $b_{i,t}^r$  is firm  $i$ 's observed bank carried over from year  $t$  to year  $t + 1$  with  $b_{i,2007}^r = 0$ , and  $x_{i,t}^r$  is firm  $i$ 's observed net permit purchase in year  $t$ . Then the banking-adjusted allocation for firm  $i$  in year  $t$ , denoted by  $q_{i,t}^a$ , is set as

$$q_{i,t}^a = \begin{cases} q_{i,t}^r - (b_{i,t}^r - b_{i,t-1}^r) = e_{i,t}^r - x_{i,t}^r & \text{if } i \in \mathcal{D}_t^r \cup \mathcal{S}_t^r \\ q_{i,t}^r - \frac{1}{2}(b_{i,t}^r - b_{i,t-1}^r) = \frac{1}{2}(q_{i,t}^r + e_{i,t}^r) & \text{if } i \in \mathcal{A}_t^r \end{cases} \quad (22)$$

For observed trading firms, effective allocations are simply raw allocations net of yearly bank increments  $b_{i,t}^r - b_{i,t-1}^r$ . That is, observed buying (resp. selling) firms are ex-ante short (resp. long) by their ex-post net traded volumes. For observed autarkic firms, we add an arbitrary  $\frac{1}{2}$  factor in front of the bank increment. Absent this factor, these firms would by construction have no need to trade ex ante as  $q_{i,t}^a$  would coincide with  $e_{i,t}^r$  since  $x_{i,t}^r = 0$ . However, firms'

<sup>28</sup>We exclude firms with implied negative abatement, i.e. with  $u_{i,t} - e_{i,t}^r < 0$ , which is the case for 30% of the firms on average across years. This leads to some changes in the size of the annual samples of firms.

<sup>29</sup>This implies that (1) trading costs only affect the extent of annual inter-firm trading in isolation of other years and (2) each year intertemporal intra-firm trading has precedence over (costly) inter-firm trading.

decisions to abstain from trading and exclusively use the market’s temporal flexibility margin can in part be driven by the existence of trading costs that reflect foregone gains from trade. Here, we consider a factor of  $\frac{1}{2}$  for lack of relevant empirical guidance, implying that half of the observed autarkic firms’ surpluses or shortages is passed on to the marketplace.<sup>30</sup> From (22) we finally compute annual permit deficits as  $\beta_{i,t} = u_{i,t} - q_{i,t}^a$  and Table D.1 contains some descriptive statistics on the inferred firms’ characteristics  $\{\alpha_{i,t}, \beta_{i,t}\}_{i,t}$  binned by sectors.

So equipped, we can populate the sets  $\mathcal{D}_t$ ,  $\mathcal{S}_t$  and  $\mathcal{A}_t$  defined in (5-6) for any feasible price  $p$  and admissible trading costs  $(F, T)$ . We consider a mesh where  $F$  and  $T$  respectively range from 0 to 200 k€ and 0 to 3 €/tCO<sub>2</sub> with steps of 1 k€ and 0.1 €/tCO<sub>2</sub>, and  $p$  varies freely within the feasibility region as per (9). This defines supply  $S_t$  and demand  $D_t$  as per (7) for any discretized pair  $(F, T)$ . For any given pair, we can then solve for the year- $t$  equilibrium price  $\hat{p}_t$ , namely  $\hat{p}_t = \min p$  subject to  $D_t - S_t > 0$ .

#### 4.1.2 Selecting relevant trading costs

As Carlson et al. (2000, p. 1319) observe, the failure of firms to realize cost savings through trading cannot be inferred simply by comparing price levels obtained under different modeling scenarios with those that actually prevailed. Specifically in our case, a multiplicity of trading cost pairs can replicate the observed price levels  $p_t^r$ . Additionally, price formation is influenced by a variety of other factors our model does not explicitly account for. As such, the ability to replicate observed prices is not robust enough a criterion to discriminate between cost pairs. Accordingly, we eliminate the difference between  $p_t^r$  and the  $\hat{p}_t$ ’s for all pairs.<sup>31</sup>

To do so, we introduce additive yearly fixed effects  $\eta_t$  that adjust firms’ marginal abatement cost schedules to  $\alpha_{i,t}(u_{i,t} - e_{i,t}) + \eta_t$  and pick the  $\eta_t$  that erases the simulated-observed price wedge: for every cost pair  $(F, T)$  and year  $t$  there corresponds a unique  $\eta_t$  such that  $\hat{p}_t = p_t^r$  (if initially  $\hat{p}_t < p_t^r$  then  $\eta_t > 0$  and vice versa). Because it de facto shifts firms’ initial permit deficits by  $\eta_t/\alpha_{i,t}$ , the calibrated  $\eta_t$  can be thought of as partly controlling for common shocks to or trends in firms’ baseline emissions or for firms’ intertemporal trading decisions that our first-pass proxies for baselines and banking-adjusted allocations do not capture. Specifically,  $\eta_t > 0$  corrects for higher baselines or market-wide incentives to bank or both. Accordingly,

<sup>30</sup>In Appendix D.2, we discuss and analyze the sensitivity of our calibration results to this factor. In short, a higher factor implies lower individual surpluses available on the market or lower shortages to be purchased from the market, hence lower trading costs to rationalize autarkic compliance, and vice versa.

<sup>31</sup>This implies that our approach ignores the direct impacts that trading costs may have on price formation when we select a cost pair. Yet, it does capture their indirect impacts, i.e. as firms adjust their participation in, and their extent of, trading based on the cost levels.

Table 1: Typology of sorting errors

	Observations		
	Autarkic	Buyer	Seller
Model	Autarkic	$\mathcal{E}_1$	$\mathcal{E}_2$
	Buyer	$\mathcal{E}_3$	$\mathcal{E}_5$
	Seller	$\mathcal{E}_4$	$\mathcal{E}_6$

a calibrated  $\eta_t$  significantly different from zero indicates that we hit the limits of our static model, i.e. the assumptions behind the model parametrization do not allow us to reproduce observed prices without substantial correction to the model parameters.

To make an educated guess about practically relevant trading cost values and discriminate between cost pairs, we propose to discipline the selection of trading costs by jointly minimizing the total number of modeling sorting errors and their dispersion across error types. That is, our selection criterion minimizes discrepancies between firms' market participation decisions and their net market positions as predicted by the model vs. as observed in the data.

Among the six error types listed in Table 1, types 1-4 relate to the firms' market participation decisions while types 5-6 relate to their net market positions conditional on participation. For example, the set  $\mathcal{E}_1$  (resp.  $\mathcal{E}_5$ ) contains observed buyers (resp. sellers) mistakenly sorted as autarkic (resp. buyers) by the model given a triplet  $(F, T, \eta_t)$ . When  $F = T = 0$ , no firm chooses autarky in the model so that  $\mathcal{E}_1 = \mathcal{E}_2 = \emptyset$ . As  $F$  and/or  $T$  rises and the autarkic zone in Figure 3 widens the cardinalities of these sets,  $|\mathcal{E}_1|$  and  $|\mathcal{E}_2|$ , increase while both  $|\mathcal{E}_3|$  and  $|\mathcal{E}_4|$  decrease, indicating a trade-off in the cost levels. Recall also that  $F > 0$  is necessary to explain that some overallocated firms may remain autarkic, which causes  $|\mathcal{E}_4|$  to shrink. We finally notice that  $|\mathcal{E}_5|$  and  $|\mathcal{E}_6|$  are negligible relative to the numbers of participation-related errors. This was to be expected since trading firms' effective allocations are by construction set in line with their observed net market positions in (22).

Formally, our twin objective is to (1) minimize the total number of sorting errors and (2) favor balanced distributions of these errors among error types. Goal (2) is congruent with maximizing Shannon's entropy applied to the distribution of error types  $\{|\mathcal{E}_1|, \dots, |\mathcal{E}_6|\}$ . Specifically, letting  $\mathcal{P}_i = |\mathcal{E}_i| / \sum_{j=1}^6 |\mathcal{E}_j|$  denote the proportion of type- $i$  errors, Shannon's entropy  $\mathcal{H}$  is defined by

$$\mathcal{H} = - \sum_{i=1}^6 \mathcal{P}_i \log(\mathcal{P}_i) \in [0; \log(6)],$$

and is maximal when the errors are evenly distributed, i.e.  $\mathcal{P}_i = \mathcal{P}_j$  for all  $i \neq j$ . With  $N$  the

Table 2: Annual calibration results

	$p_t^r$	$F$	$T$	$T/p_t^r$	$\eta_t$	$\mathcal{H}/\log(6)$	$1 - \sum_{i=1}^6  \mathcal{E}_i /N$
2009	13.3	18 [15;19]	1.4 [1.3;1.5]	10.5%	-0.31 [-0.31;-0.20]	0.66	0.85
2011	13.1	16 [15;16]	1.3 [1.1;1.6]	9.9%	0.36 [0.23;0.41]	0.66	0.87
2012	7.4	8 [7;9]	0.6 [0.3;0.8]	8.1%	0.26 [0.26;0.32]	0.67	0.90

Note:  $p_t^r$ ,  $\eta_t$  and  $T$  given in €/tCO<sub>2</sub>.  $F$  given in k€. 1%-sensitivity intervals given within brackets.

total number of firms in the sample, we thus select  $(F, T)$  to maximize the normalized index

$$\left(\mathcal{H}/\log(6)\right) \times \left(1 - \sum_{i=1}^6 |\mathcal{E}_i|/N\right) \in [0; 1]. \quad (23)$$

Given the aforementioned trade-off in trading cost levels and as detailed further in Appendix D.1, the normalized index is primarily driven by its entropy component which has an inverted U shape – hence it is globally concave. Table 2 reports our calibration results for 2009, 2011 and 2012. We discard 2008 and 2010 because the  $\eta_t$ ’s for these years are significantly larger than zero, pointing to an ill-suited model parametrization (see Appendix D.1 for detail). By contrast, for the other years, the  $\eta_t$ ’s are close to zero (representing only 2-4% of the permit price) and vary negligibly over the range of admissible trading costs. This aspect is important to ensure that our selection of trading costs does not depend on (variations in)  $\eta_t$ .

The selected annual values for  $F$  and  $T$  vary between 8 and 18 k€, and 0.6 and 1.4 €/tCO<sub>2</sub> (or 8.1 and 10.5% of the permit price) across years. Table 2 also reports sensitivity intervals for the selected trading cost values in a neighborhood of the index’s maximum (here of relative size 1%).<sup>32</sup> To substantiate the improvement relative to zero trading costs on average across years, the selected cost pairs decrease the number of sorting errors by 40%, rationalize 70% of individual autarkic compliance decisions and reduce the dispersion across sorting error types as measured by a 160% increase in Shannon’s entropy. In Appendix D, we provide additional calibration and sensitivity results as well as graphical illustrations.

Although our approach to selecting trading costs differs from the various methods used in the related empirical literature, our results are in the same range. For instance, Naegele (2018) estimates median and mean fixed permit market entry costs of 7 and 21 k€ across firms in Phase II, respectively. Similarly, estimates of proportional trading costs are in the order of

<sup>32</sup>These intervals show cost ranges that yield closely similar market outcomes, see Appendix D.1 for details.

0.1 € per permit traded but can go up to 2 € for small firms (e.g. Jaraitė et al., 2010; Heindl, 2012b; Joas & Flachsland, 2016). Additionally, Frino et al. (2010) and Medina et al. (2014) find bid-ask spreads for Phase II futures contracts ranging from 1 to 10% of the permit price, which can give a rough sense of the magnitude of proportional trading costs. Finally, while our model assumes trading costs that are common to all firms, our calibration exercise selects values that are more relevant for small and often long (i.e. potentially selling) firms.<sup>33</sup> Indeed, autarkic and impaired trading behaviors are more salient for this class of firms, as the related literature (Section 2.1) and trading data (Section 2.2) attest.<sup>34</sup> In Section 5, we discuss other modeling aspects and caveats that must be applied when interpreting our calibration results.

## 4.2 Supply control with vs. without trading costs

Trading costs affect equilibrium outcomes, which has important implications for policy design, evaluation and implementation. Here, we utilize our calibrated model to appraise the market price responses to supply-curbing policies in the presence vs. absence of trading costs and how they depend on their incidence across firms.<sup>35</sup> We also evaluate how the total compliance costs vary as supply is tightened and firms alter their trading behavior.

### 4.2.1 Impacts on market prices

We evaluate the price impacts of an arbitrary one-sixth tightening in (annual) supply in 2009 and 2012 for each select sample of firms.<sup>36</sup> We consider these two years because they feature differing values for the trading cost pairs and market price levels  $p_t^r$ . We assume that permits are withdrawn directly from firms' allocations according to four alternative scenarios: (1) proportionally to their initial allocations, (2) uniformly across all firms, or uniformly across overallocated (3) or underallocated (4) firms exclusively. We take two alternative perspectives in this appraisal: one which is oblivious to the trading costs in the model calibration, the

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<sup>33</sup>Although  $F$  can be thought of as size invariant, the selected values can only preclude firms from trading when expected gains from trade are small, which is more likely to be the case for small firms all else equal. While in practice  $T$  typically decreases with trading volume, the selected values are in the literature's higher estimated range, which is more relevant for small firms. Also, their dispersion around the index's maximum (see Appendix D) also reflects the heterogeneity of relevant  $T$ -values across firms.

<sup>34</sup>Hence, the calibration index in (23) purposely does not discriminate between firms by size, for otherwise the gains in minimizing modeling sorting errors due to trading costs would be dwarfed by construction.

<sup>35</sup>This is a timely issue in a context where the EU is bound to raise its climate ambition target by further restricting permit supply over time (via an increase in the linear reduction factor of the emissions cap) and change the free allocation profile among firms (as a result of a carbon border adjustment mechanism).

<sup>36</sup>The size of the tightening does not affect the qualitative nature of our results. See Section 4.2.2 for a broader spectrum of tightening policy magnitude.

Table 3: Price responses to a one-sixth supply tightening with different incidence scenarios

		Incidence scenario			
		(1)	(2)	(3)	(4)
2009 ( $p^r=13.3$ )	$(p^* - p^r)/p^r$	0.70	0.70	0.70	0.70
	$(\hat{p} - p^r)/p^r$	1.11	1.29	1.19	1.59
	$(\hat{p} - p^r)/(p^* - p^r)$	1.59	1.84	1.70	2.27
2012 ( $p^r=7.4$ )	$(p^* - p^r)/p^r$	1.04	1.04	1.04	1.04
	$(\hat{p} - p^r)/p^r$	2.14	2.47	2.27	2.79
	$(\hat{p} - p^r)/(p^* - p^r)$	2.06	2.38	2.18	2.68

*Note:*  $p^r$  is the pre-tightening reference price in €/tCO<sub>2</sub>,  $p^*$  (resp.  $\hat{p}$ ) is the post-tightening price without (resp. with calibrated) trading costs. Incidence scenario: permits are withdrawn (1) proportionally to firms' allocations, uniformly across all (2), overallocated (3) or underallocated (4) firms in the annual samples.

other in which trading costs are accounted for and selected as in Section 4.1.2.

Table 3 reports our results. As expected, the incidence of the cutback across firms is neutral vis-à-vis the magnitude of the market price increase under the assumption of no trading costs. This no longer holds when one accounts for trading costs: as Proposition 3 indicates, the size of the market price increase, relative to the frictionless case, depends on a price effect and a distribution effect, i.e. how the tightening is distributed among firms.

Two findings emerge from our calibrated examples. First, the price increase is always larger when one accounts for trading costs than in the frictionless case, irrespective of the incidence scenario. This is because in our samples of firms some potential suppliers are autarkic due to the trading costs so that the market is initially tighter than in the frictionless case, which in turn tends to amplify the tightening-induced price increase. Additionally, the lower the price level to start with, the larger the relative tightening-induced price increase and the larger the absolute price increase in the absence vs. presence of trading costs. Importantly, note that larger trading costs (as in 2009 w.r.t. 2012) should not be thought of as a sufficient condition to sustain larger price responses to a supply tightening.

Second, the incidence of the tightening has significant impacts on the resulting price increase, which can vary in size by 30-40% across incidence scenarios. Intuitively, we see that uniformly targeting the supply tightening on underallocated (resp. overallocated) firms leads to a larger (resp. smaller) price increase than when it is evenly distributed among all firms. The lowest price increase obtains when the tightening is spread across firms in proportion to their initial permit endowments, a proxy for their size under grandfathering-based allocation. As Section 4.2.2 will confirm with a welfare analysis, this incidence type leaves less (costly) reallocations

to occur through the market than the others (relative to the least-cost optimum). As such, it mitigates induced additional market strain and thus the resulting price increase.

In summary, modeling assumptions (here considering trading costs or not) matter for supply policy evaluation (e.g. size of the price response) and implementation (e.g. role of the incidence on firms). Specifically, our simulation results suggest that a modeler/regulator who does not account for trading costs though they prevail in reality may underestimate the price impacts of supply-curbing policies, here by a factor of about two. This underestimation bias is slightly more pronounced the lower the pre-tightening price and varies with the incidence type.

#### 4.2.2 Impacts on compliance costs

We evaluate compliance costs over a 0–30% range of tightening in supply for the 2009 select sample of firms and compare them depending on (1) whether trading costs are accounted for or not and (2) the type of incidence on firms. Overall compliance costs comprise abatement costs and incurred trading costs (if any) which we sum over all firms. By construction, they are increasing and convex in the stringency of the tightening and always higher in the presence of trading costs (Proposition 2). Relative to frictionless conditions, extra compliance costs result from incurred trading costs and foregone efficiency gains at the extensive and intensive margins. Figure 4 depicts these extra costs in relative terms as a function of the stringency of the tightening with the same four types of incidence as in Section 4.2.1.

Two findings emerge from our simulations. First, the extra compliance costs attributable to trading costs are in the order of 7% with the reference supply.<sup>37</sup> This figure should be taken as illustrative only because it results from a comparison of modeling outputs under different modeling assumptions, not from a proper counterfactual analysis which we by construction cannot perform in our framework. As supply is tightened, the relative extra compliance costs decrease as the associated increase in compliance costs in absolute terms gradually dwarfs the difference in compliance costs with and without trading costs.

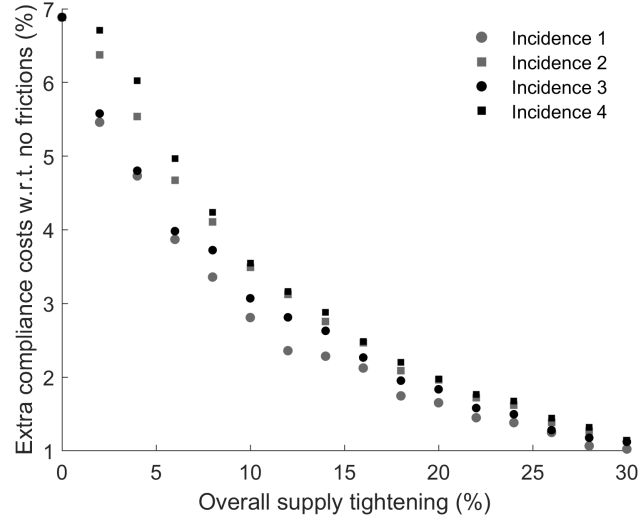
Second, the incidence of the tightening has notable impacts on the size of the extra compliance costs, which are higher by 15 to 35% between the most and least welfare-deteriorating type of incidence. Although there are many moving parts, most of this wedge can be explained by the relative changes in the number of autarkic firms as supply is tightened across incidence types. Indeed, autarkic firms’ compliance costs are invariant when supply varies, namely nil when

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<sup>37</sup>The welfare loss remains ‘relatively small’ as our calibrated cost values allow us to better represent the behavior of small firms, which are numerous but only cover 5-10% of emissions (see Sections 2.2 and 4.1.2).



Figure 4: Compliance costs for a 0–30% supply tightening with different incidence scenarios



*Note:* Based on the 2009 select sample of firms. Incidence scenario: permits are withdrawn (1) proportionally to firms’ allocations, (2) uniformly across all, (3) overallocated or (4) underallocated firms.

they are overallocated, positive but constant when underallocated. Simulations reveal that the number of autarkic firms (mostly overallocated) is relatively stable under incidence type (1) while it immediately collapses under types (2) and (4) as they induce the largest changes in market structure (here, initial individual deficits/surpluses).<sup>38</sup> An incidence proportional to firms’ allocations thus appears as the least distortive incidence type.

Finally, we note that for a given emissions cap stringency, the simulated market price level is commensurate with the market strain which is reflected in the size of unrealized gains from trade and incurred trading costs. That is, the ranking of incidence types in terms of welfare loss visible in Figure 4 is identical to that in terms of price level given in Table 3, specifically incidence type (1)  $\succ$  (3)  $\succ$  (2)  $\succ$  (4) where  $\succ$  denotes welfare dominance.

## 5 Discussion

In this section, we discuss some limitations of our approach in order to put into perspective our modeling choices and results. These relate to temporal, dynamic, behavioral and institutional factors which may impinge on firms’ participation in and extent of inter-firm trading, but are not formally treated in our framework. Because these interrelated factors distort and impair

<sup>38</sup>The share of autarkic firms under a uniform targeting of overallocated firms is also stable at first before starting to drop at a 7% cutback. This separation between incidence types (1) and (3) is visible in Figure 4.

trading incentives, our approach may overstate the size and impacts of trading costs. Yet, as we discuss below, the related literature generally ignores these factors or, more exceptionally, analyzes them individually. Against this background, we believe that our formal equilibrium analysis of the impacts of transaction costs constitutes a welcome addition to the literature. Relatedly, our model calibration in Section 4.1 can be thought of as capturing the aggregate impact of these various factors rather than the exclusive impacts of transaction costs.<sup>39</sup>

**Banking and borrowing.** Firms generally have some leeway in banking issued permits for future use or borrowing future permits for present use. As a result, intertemporal reshuffling can be a substitute to costly inter-firm trading.<sup>40</sup> For instance, in the US Acid Rain Program (ARP), [Toyama \(2019\)](#) numerically estimates significant trading costs, in a range of 15-35% of the market price per permit traded, which in turn imply excess banking and less dispersed emissions as a result of lower inter-firm trading relative to an idealized counterfactual scenario without trading costs. However, except in [Toyama’s](#) numerical model, the interplay between trading and banking decisions with transaction costs is seldom accounted for. More generally, to investigate specific policy impacts, the temporal dimension of permit markets is often shut down in both numerical and analytical approaches. For instance, [Fowlie et al. \(2016\)](#) develop a dynamic oligopoly model to numerically compare firms’ entry-exit and investment decisions on the product market under different permit allocation regimes, but do not consider banking to isolate the allocation impacts. Similarly, to assess cost savings and health impacts in the ARP, [Chan et al. \(2018\)](#) use a static model of compliance choices (fuel switch, permit purchase, scrubber installation) to sidestep the complexities associated with modeling permit purchase and banking as options to install a scrubber or fuel switch at a later date.<sup>41</sup> Both approaches, like ours, are thus likely to overemphasize the inter-firm trading dimension.

As in [Singh & Weninger \(2017\)](#), we develop a static permit trading model in order to be able to derive and exploit novel analytical results on the equilibrium impacts of transaction costs. Because the temporal dimension is not formally treated, our calibration exercise should thus be seen as providing upper bounds for the transaction costs and their impacts.<sup>42</sup> However, we take firms’ observed banking dynamics as a given to adjust their allocations and mitigate

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<sup>39</sup>For the same reasons, [Naegele’s \(2018\)](#) estimates of fixed trading costs capture all existing frictions.

<sup>40</sup>Although the intertemporal flexibility margin reduces trading incentives, it is not sufficient to rationalize autarkic compliance as one should still expect some potential profits from inter-firm trading. For instance, some firms may not want to bear the opportunity cost of not selling at least some of their excess permits.

<sup>41</sup>Similarly, [Carlson et al. \(2000\)](#) compute long-run gains from trade in a steady state of the ARP, bypassing the issue of modeling intertemporal decisions by taking firms’ banking behavior as a given.

<sup>42</sup>Similarly, [Jaraitė-Kažukauskė & Kažukauskas \(2015\)](#) and [Naegele \(2018\)](#) employ static setups for their econometric estimations of transaction costs and their impacts on firms in the EU ETS.

this limitation. Additionally, we wish to underline that the temporal dimension is also likely to be subject to other specific costs and limitations, which relate to the other biases discussed below. It is indeed difficult to elicit firms’ degree of intertemporal optimization (e.g. [Ellerman et al., 2016](#); [Hintermann et al., 2016](#)) and there is evidence of limited farsightedness or biased beliefs (e.g. [Chen, 2018](#); [Quemin & Trotignon, 2021](#)).

**Uncertainty and irreversible investments.** Our framework does not account for uncertainty and investment in abatement technology, although investment can be a substitute for permit trading (e.g. [Slechten, 2013](#)). Under uncertainty and if abatement is at least partly irreversible, option theory implies that the permit price has to exceed the marginal abatement cost by an irreversibility premium for investment to occur (e.g. [Chao & Wilson, 1993](#); [Insley, 2003](#); [Zhao, 2003](#); [Taschini, 2020](#)). In turn, trading incentives may be altered independently of transaction costs.<sup>43</sup> In particular, the effect of an irreversibility premium is observationally equivalent to that of a variable trading cost – both introduce a mark-up on the permit price. However, whether this mark-up accrues due to an irreversibility premium or variable trading costs or both, it is not sufficient to corroborate observed firm behavior (Section 2.2). Indeed, as discussed on the basis of Figure 3, it cannot explain why long firms stick to autarky, which nonetheless account for 80% of all autarkic cases in our dataset. Only the existence of a fixed transaction cost makes it possible to rationalize such behavior.

Furthermore, in line with real-option theory, there is empirical evidence that demand ([Bailey, 2020](#)) or regulatory ([Dorsey, 2019](#)) uncertainty hinders firms’ investment in low-carbon technology. In the EU ETS, more specifically, the literature finds that the scheme has primarily encouraged low-investment, often reversible cost-management strategies such as fuel switching (e.g. [Schmalensee & Stavins, 2017](#); [Teixidó et al., 2019](#)). For instance, it has stimulated innovation (rather than adoption) with no short-term effect on emissions (e.g. [Calel & Dechezleprêtre, 2016](#); [Calel, 2020](#)) and free allocation has also been shown to hamper investment, especially in Phases I & II. Therefore, the fact that distortions entailed by transaction costs and uncertainty exist independently of each other and do not exactly overlap, in addition to the lack of evidence for an investment dynamics in our sample period, provides some ground for the static framework used in this paper.

**Behavioral biases.** Autarkic compliance and stifled trading may also result from behavioral

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<sup>43</sup>Note that the irreversibility premium exists independently of transaction costs but can be increased by transaction costs. For instance, in the event of a market downturn, firms that are ex-post long would like to avoid selling excess permits freed up by investment at too low a price to cover their sunk cost of investment, illustrating that low-carbon investment is not a good substitute for permit trading. Because transaction costs restrict selling, the relative value of low-carbon investment is decreased even further.

biases. For instance, autarkic firms can be thought of as trading off profits from entering the market with higher associated organizational and decision-making complexity. As heuristics or rules of thumb, autarkic banking and borrowing may thus constitute viable, if not rational, strategies when deemed to perform satisfactorily well relative to more complex procedures (e.g. [Baumol & Quandt, 1964](#); [Simon, 1979](#); [Radner, 1996](#); [Gigerenzer & Selten, 2003](#)). As a case in point, some firms perceive the EU ETS as a compliance instrument rather than as a compliance market, especially when commodity trading is not part of their core business (e.g. [Martin et al., 2015](#); [Venmans, 2016](#); [Schleich et al., 2020](#)).<sup>44</sup> That is, firms may rather seek to comply with the least disruption possible to their routine operations than maximize profits from permit trading. More generally, an insight from behavioral economics is that firms are likely to be subject to endowment effects w.r.t. their permit holdings, which can also frustrate trading. These «effects are predicted for property rights [...] such as transferable pollution permits» ([Kahneman et al., 1990](#)) and confirmed empirically by [Murphy & Stranlund \(2007\)](#) and [Venmans \(2016\)](#). As a result, firms' willingness to pay for extra permits is larger than their willingness to sell excess permits, implying that differences in firms' marginal abatement costs can persist post trading independently of transaction costs.<sup>45</sup>

**Intermediaries and trading venues.** Our framework also restrains the compliance choice space to a blunt 'autarky vs. trading', does not account for the involvement of non-regulated financial actors (e.g. [Cludius & Betz, 2020](#)), and does not distinguish between various trading platforms (e.g. auctions, exchanges, over the counter), products and partners that firms may possibly select. Relatedly, it only represents trading as a way of minimizing compliance costs but it ignores other motives to trade such as hedging or generating additional revenues (e.g. [Schleich et al., 2020](#)). We note that these aspects structure the trading network (e.g. [Borghesi & Flori, 2018](#); [Karpf et al., 2018](#)), which highlights the need to understand how the market microstructure influences transaction costs. Finally, there is evidence of bid-ask spreads and anomalies in cost-of-carry relationships in the EU ETS, suggesting that permit trades are not exclusively driven by complementarity in marginal abatement costs and that informational efficiency might be hampered (see e.g. [Friedrich et al. \(2020\)](#) for a review). These aspects can be attributed to trading frictions (e.g. [Frino et al., 2010](#); [Charles et al., 2013](#); [Medina et al., 2014](#); [Schultz & Swieringa, 2014](#)) that we cannot capture in our deterministic framework (see e.g. [Dávila & Parlatoe \(2021\)](#) for a formal analysis in financial markets).

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<sup>44</sup>For instance, [Cludius & Betz \(2020\)](#) observe that small firms are more likely to pursue a single, simple trading strategy compared to larger, more professionalized firms. This is due to the fixed costs of establishing and maintaining sophisticated trading strategies, with clear economies of scale (e.g. [Hortaçsu & Puller, 2008](#)).

<sup>45</sup>For instance, small firms' reluctance to sell excess permits may be explained by a cautious inclination to keep permits for future compliance only rather than by transaction costs per se (e.g. [Jaraitė et al., 2010](#)).

## 6 Conclusion

This paper advances the frontier of research on markets for permits with transaction costs and makes three contributions to the literature. First, we develop a consolidation procedure for annual transaction and compliance data allowing us to scrutinize firms' market behavior over EU ETS Phase II. This reveals two important empirical facts, which we interpret as pointing to the existence of fixed and variable trading costs: autarkic behavior is pervasive, especially among small or long firms, and those firms that engage in trade do so quite sparsely and only for sufficiently large volumes. Second, we incorporate fixed and proportional trading costs in a standard permit market model. In our equilibrium framework, the permit price and firms' participation in and extent of trading are determined endogenously. This allows us to analyze the sensitivity of the equilibrium to shifts in the trading costs and firms' allocations, and we characterize the properties of the market price impacts. Third, we calibrate our model to EU ETS Phase II data and show how trading costs in the order of 10 k€ per annum plus 1 € per permit traded noticeably reduce the discrepancies between observations and theoretical predictions for firms' behavior. Our simulations also suggest that ignoring trading costs may lead to underestimating the price impacts of supply-curbing policies, with the size of the bias hinging on the specific incidence of such policies on firms.

Based on the discussion of the caveats one must apply when interpreting our results in Section 5, we wish to highlight two alleys for future research. First, while our measure of transaction costs captures various frictions one should seek to formally disentangle 'hard' financial trading costs from 'soft' behavioral factors such as the endowment effect. Second, one should aim to refine the market structure modeling to account for the temporal channel and non-compliance actors to understand how they affect transaction costs and market efficiency. The theoretical and quantitative caveats of our modeling framework notwithstanding, we believe that it is a valuable contribution in the direction of bringing models closer to practical realities, and as such, making them better equipped for policy design and evaluation.

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# Appendices

## A Analytical derivations and collected proofs

### A.1 Proof of Equation (1)

Given a market price  $p > 0$ , firm  $i$ 's optimal abatement is  $a_i^*(p) = p/\alpha_i$  and its individual efficiency gains from permit trading are defined by

$$G_i(p) = C_i(a_i^0) - \left( C_i(a_i^*(p)) + p(\beta_i - a_i^*(p)) \right),$$

where  $a_i^0 = \max\{0; \beta_i\}$ . Recalling that  $p_i^0 = \alpha_i a_i^0$  and  $C_i(a_i) = \alpha_i a_i^2/2$ , the above rewrites

$$\begin{aligned} G_i(p) &= C_i(a_i^0) - \left( C_i(a_i^*(p)) + p(\max\{0; \beta_i\} + \min\{0; \beta_i\} - a_i^*(p)) \right) \\ &= C_i(a_i^0) - \left( C_i(a_i^*(p)) + p(a_i^0 + \min\{0; \beta_i\} - a_i^*(p)) \right) \\ &= \left( (p_i^0)^2 - p^2 - 2pp_i^0 + 2p^2 \right) / (2\alpha_i) - p \min\{0; \beta_i\} \\ &= (p_i^0 - p)^2 / (2\alpha_i) - p \min\{0; \beta_i\} = (p_i^0 - p)^2 / (2\alpha_i) + p \max\{0; -\beta_i\}. \end{aligned}$$

Firm  $i$  is better off buying (resp. selling) permits when  $p_i^0 > p$  (resp.  $p_i^0 < p$ ) which defines the sets  $\mathcal{D}$  and  $\mathcal{S}$ . Consequently, no firm is willing to buy (resp. sell) permits on the market when  $p \geq \bar{\alpha}\bar{\beta}$  (resp.  $p = 0$ ). Hence, a market price is feasible when  $p \in (0; \bar{\alpha}\bar{\beta})$ .

### A.2 Proof of Equations (3-4)

Below, we define market participation price thresholds for prospective buying/selling firms.

For  $\beta_i \leq 0$ ,  $i$  sells permits on the market if  $G_i(p - T) - F > 0$ , i.e.  $X^2 - 2\alpha_i\beta_i X - 2\alpha_i F > 0$  with  $X = p - T$ . Only keeping the positive root, this occurs if  $p - T > \alpha_i\beta_i + \sqrt{\alpha_i^2\beta_i^2 + 2\alpha_i F}$ , which is nil for  $F = 0$  and positive for  $F > 0$ .

For  $\beta_i > 0$ ,  $i$  buys (+) or sells (-) permits on the market if  $X^2 - 2\alpha_i(F + \beta_i X) + \alpha_i^2\beta_i^2 > 0$  with  $X = p \pm T$ . For a seller, we only keep the relevant root  $X = p - T > \alpha_i\beta_i$  so  $i$  partakes in the market if  $p - T > \alpha_i\beta_i + \sqrt{2\alpha_i F}$ , which is always positive. For a buyer, we only keep the relevant root  $X = p + T < \alpha_i\beta_i$  so  $i$  partakes in the market if  $p + T < \alpha_i\beta_i - \sqrt{2\alpha_i F}$ . This is positive provided that  $F$  is not too large, i.e.  $F < \alpha_i\beta_i^2/2$ . This must at least be true for the last potential buyer so  $F < \bar{\alpha}\bar{\beta}^2/2$ , see e.g. Appendix A.4.

### A.3 Proof of Equations (5-6)

Expanding firm  $i$ 's market participation constraint  $G_i(p \pm T) - F > 0$  gives

$$\begin{aligned} & (p_i^0)^2 - 2p_i^0(p \pm T) + (p \pm T)^2 - 2\alpha_i(p \pm T) \min\{0; \beta_i\} - 2\alpha_i F > 0 \\ \Leftrightarrow & \alpha_i^2(\max\{0; \beta_i\})^2 - 2\alpha_i(p \pm T)(\max\{0; \beta_i\} + \min\{0; \beta_i\}) - 2\alpha_i F + (p \pm T)^2 > 0 \\ \Leftrightarrow & \alpha_i^2(\max\{0; \beta_i\})^2 - 2\alpha_i(\beta_i(p \pm T) + F) + (p \pm T)^2 > 0. \end{aligned}$$

Substantiating the three different cases depending on the pairs  $(\alpha_i, \beta_i)$ , this rewrites

$$\begin{aligned} & \alpha_i^2 \beta_i^2 - 2\alpha_i(F + (p + T)\beta_i) + (p + T)^2 > 0 \quad \text{when } \alpha_i \beta_i > p + T, \\ & \alpha_i^2 \beta_i^2 - 2\alpha_i(F + (p - T)\beta_i) + (p - T)^2 > 0 \quad \text{when } 0 < \alpha_i \beta_i < p - T, \text{ or} \\ & -2\alpha_i(F + (p - T)\beta_i) + (p - T)^2 > 0 \quad \text{when } \beta_i \leq 0. \end{aligned}$$

When  $\beta_i \leq 0$  (resp.  $\beta_i > 0$ ) the  $\alpha_i$ -thresholds obtain by solving a first-order (resp. second-order) polynomial inequality and keeping the relevant roots. When  $\beta_i \leq -F/(p - T)$ , the third inequality above holds for all  $\alpha_i > 0$ . This defines the sets  $\mathcal{D}(p, F, T)$  and  $\mathcal{S}(p, F, T)$ .

We verify that  $\mathcal{S}(p, F, T)$  (resp.  $\mathcal{D}(p, F, T)$ ) effectively contains all selling (resp. buying) firms. To see this, observe that  $i$  is a seller (resp. buyer) i.f.f.  $\beta_i - a_i^*(p - T) < 0 \Leftrightarrow \alpha_i < (p - T)/\beta_i$  (resp.  $\beta_i - a_i^*(p + T) > 0 \Leftrightarrow \alpha_i > (p + T)/\beta_i$ ). This suffices to demonstrate our claim since  $i$ 's thresholds can easily be shown to satisfy  $\alpha_i^0, \alpha_i^- < (p - T)/\beta_i$  and  $(p + T)/\beta_i < \alpha_i^+$ .

Below, we provide the partial derivatives of the  $\alpha$ -thresholds with their signs:

$$\begin{aligned} \partial \alpha^\pm / \partial p &= (1 \pm F/X_1^\pm) / \beta > 0 & \partial \alpha^\pm / \partial \beta &= -X_2^\pm (1 \pm F/X_1^\pm) / \beta^3 < 0 \\ \partial \alpha^\pm / \partial F &= (1 \pm X_3^\pm / X_1^\pm) / \beta^2 \gtrless 0 & \partial \alpha^\pm / \partial T &= (\pm 1 + F/X_1^\pm) / \beta^2 \gtrless 0 \\ \partial \alpha^0 / \partial p &= (p - T)X_2^- / 2(X_3^-)^2 > 0 & \partial \alpha^0 / \partial \beta &= -(p - T)^3 / 2(X_3^-)^2 < 0 \\ \partial \alpha^0 / \partial F &= -(p - T)^2 / 2(X_3^-)^2 < 0 & \partial \alpha^0 / \partial T &= -(p - T)X_2^- / 2(X_3^-)^2 < 0 \end{aligned}$$

where  $X_1^\pm = \sqrt{F(F + 2(p \pm T)\beta)} > F$ ,  $X_2^\pm = 2F + (p \pm T)\beta > 2F$  and  $X_3^\pm = X_2^\pm - F > X_1^\pm$ . This proves our claim on the changes in the measures of  $\mathcal{D}(p, F, T)$  and  $\mathcal{S}(p, F, T)$  as  $p$ ,  $F$  or  $T$  increases. Note also that  $\lim_{\beta \rightarrow 0^+} \alpha^+ = \lim_{\beta \rightarrow 0^+} 2F/\beta^2 = +\infty$ . To get at  $\lim_{\beta \rightarrow 0^+} \alpha^-$ , we first compute the second-order Taylor expansion of the numerator in  $\alpha^-$ , namely

$$F + (p - T)\beta - F \left( 1 + \frac{1}{2} \frac{2(p - T)\beta}{F} - \frac{1}{8} \left( \frac{2(p - T)\beta}{F} \right)^2 \right) = \frac{(p - T)^2 \beta^2}{2F},$$

so that  $\alpha^- \sim_{\beta \rightarrow 0^+} (p - T)^2 / (2F) = \alpha^0(p, F, T; 0)$ , i.e. there is continuity between  $\alpha^-$  and  $\alpha^0$  in  $\beta = 0$ . By a similar token,  $\partial \alpha^- / \partial \beta \sim_{\beta \rightarrow 0^+} -(p - T)^3 / 2F^2 = \partial \alpha^0 / \partial \beta(p, F, T; 0)$ , i.e. there is also continuity in slope. Finally,  $\lim_{\beta \rightarrow 0^+} \partial \alpha^+ / \partial \beta = \lim_{\beta \rightarrow 0^+} -4F / \beta^3 = -\infty$ ,  $\lim_{\beta \rightarrow +\infty} \alpha^\pm = 0$ ,  $\lim_{\beta \rightarrow -F/(p-T)} \alpha^0 = +\infty$  and  $\lim_{\beta \rightarrow -F/(p-T)} \partial \alpha^0 / \partial \beta = -\infty$ , which completes the description of the behaviors of the supply and demand frontiers in Figure 3.

## A.4 Proof of Proposition 1

*Feasible prices and admissible trading costs.* A permit price is feasible as long as there is at least one buyer and one seller left in the market. The last permit supplier has characteristics  $(\underline{\alpha}, \underline{\beta})$ , i.e. it drops out of the market when  $\alpha^0(p, F, T; \underline{\beta}) = \underline{\alpha}$ . Symmetrically, the last buyer has characteristics  $(\bar{\alpha}, \bar{\beta})$ , i.e. it switches to autarkic compliance when  $\alpha^+(p, F, T; \bar{\beta}) = \bar{\alpha}$ . The two price bounds in (9) thus obtain by solving  $\alpha^0(p, F, T; \underline{\beta}) = \underline{\alpha}$  and  $\alpha^+(p, F, T; \bar{\beta}) = \bar{\alpha}$ . Trading costs are admissible iff the set of feasible prices in (9) is non-empty. This requires  $\underline{\beta}\underline{\alpha} + T + \sqrt{\underline{\beta}^2\underline{\alpha}^2 + 2\underline{\alpha}F} < \bar{\alpha}\bar{\beta} - T - \sqrt{2\bar{\alpha}F}$  and  $\bar{\alpha}\bar{\beta} - \sqrt{2\bar{\alpha}F} > p + T > 0$ , which gives (8).

We next prove the following lemma:

*For any admissible trading costs  $F$  and  $T$  and feasible market price  $p$ , it holds that*

$$\frac{\partial S}{\partial p} > 0, \quad \frac{\partial S}{\partial F} < 0, \quad \frac{\partial S}{\partial T} < 0, \quad \frac{\partial D}{\partial p} < 0, \quad \frac{\partial D}{\partial F} < 0, \quad \text{and} \quad \frac{\partial D}{\partial T} < 0.$$

If we denote by  $h$  the density function of the  $\beta_i$ 's and by  $g(\cdot|\beta)$  that of the  $\alpha_i$ 's conditional on the  $\beta_i$ 's, permit supply and demand functions rewrite

$$\begin{aligned} S(p, F, T) = & \int_{\underline{\beta}}^{-F/(p-T)} \int_{\underline{\alpha}}^{\bar{\alpha}} \left( (p - T)/x - y \right) g(x|y) h(y) dx dy \\ & + \int_{-F/(p-T)}^0 \int_{\underline{\alpha}}^{\alpha^0(p, F, T; y)} \left( (p - T)/x - y \right) g(x|y) h(y) dx dy \\ & + \int_0^{\bar{\beta}} \int_{\underline{\alpha}}^{\alpha^-(p, F, T; y)} \left( (p - T)/x - y \right) g(x|y) h(y) dx dy, \end{aligned} \quad (\text{A.1})$$

$$\text{and } D(p, F, T) = \int_0^{\bar{\beta}} \int_{\alpha^+(p, F, T; y)}^{\bar{\alpha}} \left( y - (p + T)/x \right) g(x|y) h(y) dx dy, \quad (\text{A.2})$$

Note that  $D$  and  $S$  are continuous and differentiable in  $p$ ,  $F$  and  $T$ .

*Partial derivatives w.r.t.  $p$ .*  $D$  (resp.  $S$ ) is strictly decreasing (resp. increasing) with  $p$ . In the case of  $D$ , it suffices to see that  $p \mapsto y - (p + T)/x$  is strictly decreasing with  $p$  and that  $\alpha^+$  is strictly increasing with  $p$ . A similar argument follows for  $S$ , although the behavior of



the second term in (A.1) is unclear as the bound  $-F/(p-T)$  is increasing with  $p$ . To clarify, we compute the partial derivatives of the two terms of interest in (A.1) using Leibniz's rule in conjunction with Fubini's theorem. This yields

$$\begin{aligned} & F/(p-T)^2 \int_{\underline{\alpha}}^{\bar{\alpha}} \left( (p-T)/x + F/(p-T) \right) g(x|y = -F/(p-T)) h(-F/(p-T)) dx \\ & - F/(p-T)^2 \int_{\underline{\alpha}}^{\alpha^0} \left( (p-T)/x + F/(p-T) \right) g(x|y = -F/(p-T)) h(-F/(p-T)) dx, \end{aligned}$$

which concludes since by Chasles' rule the above simplifies to

$$F/(p-T)^2 \int_{\alpha^0}^{\bar{\alpha}} \left( (p-T)/x + F/(p-T) \right) g(x|y = -F/(p-T)) h(-F/(p-T)) dx > 0.$$

*Partial derivatives w.r.t.  $F$ .* A qualitative argument as in the above could suffice but formal calculus will prove helpful in the following. Differentiating (A.2) and (A.1) w.r.t.  $F$  gives

$$\begin{aligned} \frac{\partial D}{\partial F} &= - \int_0^{\bar{\beta}} \frac{\partial \alpha^+(p, F, T; y)}{\partial F} \left( y - (p+T)/\alpha^+(p, F, T; y) \right) g(\alpha^+(p, F, T; y)|y) h(y) dy < 0, \\ \frac{\partial S}{\partial F} &= -1/(p-T) \int_{\underline{\alpha}}^{\bar{\alpha}} \left( (p-T)/x + F/(p-T) \right) g(x|y = -F/(p-T)) h(-F/(p-T)) dx \\ &\quad + 1/(p-T) \int_{\underline{\alpha}}^{\alpha^0} \left( (p-T)/x + F/(p-T) \right) g(x|y = -F/(p-T)) h(-F/(p-T)) dx \\ &\quad + \int_{-F/(p-T)}^0 \frac{\partial \alpha^0(p, F, T; y)}{\partial F} \left( (p-T)/\alpha^0(p, F, T; y) - y \right) g(\alpha^0(p, F, T; y)|y) h(y) dy \\ &\quad + \int_0^{\bar{\beta}} \frac{\partial \alpha^-(p, F, T; y)}{\partial F} \left( (p-T)/\alpha^-(p, F, T; y) - y \right) g(\alpha^-(p, F, T; y)|y) h(y) dy. \end{aligned}$$

By Chasles' rule again, the first two terms in  $\partial S/\partial F$  reduce to

$$-1/(p-T) \int_{\alpha^0}^{\bar{\alpha}} \left( (p-T)/x + F/(p-T) \right) g(x|y = -F/(p-T)) h(-F/(p-T)) dx < 0.$$

Thus  $\partial S/\partial F < 0$  as the last two terms in  $\partial S/\partial F$  are also negative.

*Partial derivatives w.r.t.  $T$ .* Similar arguments show that  $\partial S/\partial T$  and  $\partial D/\partial T$  are negative.

*Existence and uniqueness of equilibrium.* The proof relies on the intermediate value theorem applied to  $V$ , which the lemma shows to be continuous and strictly increasing with  $p$ .

Denote the upper (resp. lower) feasible price bound in (9) by  $\bar{p}$  (resp.  $\underline{p}$ ). Assume trading costs are admissible as in (8), thus  $\bar{p} > \underline{p}$ . By definition,  $D(\bar{p}, F, T) = 0$  since  $\alpha^+(\bar{p}, F, T; \bar{\beta}) = \bar{\alpha}$  and  $\alpha^+ > \bar{\alpha}$  for all  $0 < \beta < \bar{\beta}$  as  $\alpha^+$  is strictly decreasing with  $\beta$ . Because  $D$  is strictly

decreasing with  $p$ ,  $D(p, F, T) > 0$  for any  $p < \bar{p}$ . Similarly, by definition  $S(\underline{p}, F, T) = 0$ . Indeed the first integral in  $S$  is nil since  $\underline{\beta} > -F/(\underline{p} - T)$ ; the second and third integrals are also nil since  $\alpha^0(\underline{p}, F, T; \underline{\beta}) = \underline{\alpha}$  so that  $\alpha^0 < \underline{\alpha}$  and  $\alpha^- < \underline{\alpha}$  for all  $\beta > \underline{\beta}$  since  $\alpha^0$  and  $\alpha^-$  are decreasing with  $\beta$ . Because  $S$  is strictly increasing with  $p$ ,  $S(p, F, T) > 0$  for any  $p > \underline{p}$ . Therefore,  $V(\underline{p}, F, T) = -D(\underline{p}, F, T) < 0$  and  $V(\bar{p}, F, T) = S(\bar{p}, F, T) > 0$ . The intermediate value theorem concludes: there exists  $\hat{p} \in (\underline{p}, \bar{p})$  such that  $V(\hat{p}, F, T) = 0$  and it is unique.

## A.5 Proof of Proposition 3

We compute and determine the magnitudes of both the price and distribution effects in the face of a small variation in individual allocation levels accounting for induced changes at both the intensive and extensive margins. We study the two effects in turn.

*Price effect.* We aim to rank  $\partial V(\hat{p}, F, T)/\partial p$  and  $\partial V(p^*, 0, 0)/\partial p$ . We first note that

$$\frac{\partial D(\hat{p}, F, T)}{\partial p} = \underbrace{-\int_0^{\bar{\beta}} \int_{\alpha^+}^{\bar{\alpha}} (1/x)g(x|y)h(y)dx dy}_{\text{intensive margin} \leq 0} - \underbrace{\int_0^{\bar{\beta}} \frac{\partial \alpha^+}{\partial p} \left( y - (\hat{p} + T)/\alpha^+ \right) g(\alpha^+|y)h(y)dx dy}_{\text{extensive margin} \leq 0},$$

where we omit the arguments in  $\alpha^+$  to reduce clutter. The intensive margin term captures the decrease in demand on the part of firms in  $\mathcal{D}(\hat{p}, F, T)$ . The extensive margin term captures the coexistent decrease in demand as the  $\mathcal{A}_2$ - $\mathcal{D}$  frontier moves to the northeast (see Figure 3). On that frontier the net demand  $y - (\hat{p} + T)/\alpha^+$  is zero when  $F = 0$  for any  $T \geq 0$  since  $\alpha^+ = (\hat{p} + T)/y$ ; and positive whenever  $F > 0$  (specifically, firms enter or exit  $\mathcal{D}$  with positive individual demands). This means that the extensive margin drops to zero when  $F = 0$ .

We proceed similarly for  $S$ , see Appendix A.4 for some computation details. In total, we get

$$\begin{aligned} \frac{\partial V(\hat{p}, F, T)}{\partial p} &= \overbrace{\frac{\partial V(p^*, 0, 0)}{\partial p} - \int_0^{\bar{\beta}} \int_{\alpha^-}^{\alpha^+} (1/x)g(x|y)h(y)dx dy - \int_{-F/(p-T)}^0 \int_{\alpha^0}^{\bar{\alpha}} (1/x)g(x|y)h(y)dx dy}^{\text{intensive margin}} \\ &\quad + \underbrace{\text{sum of positive terms}}_{\text{extensive margin}} \geq \frac{\partial V(p^*, 0, 0)}{\partial p} = \int_{\underline{\beta}}^{\bar{\beta}} \int_{\underline{\alpha}}^{\bar{\alpha}} (1/x)g(x|y)h(y)dx dy. \end{aligned}$$

When  $F = 0$  the extensive margin effects are nil so  $\partial V(\hat{p}, 0, T)/\partial p < \partial V(p^*, 0, 0)/\partial p$ , i.e. the price effect is above one. It can however be below one for some pairs  $(F > 0, T)$  for which the extensive margin effects surpass those at the intensive margin. This is more likely to occur for small costs as the intensive margin terms decrease with the cost levels.

*Distribution effect.* Consider the collection of individual deficit shifts  $\{\beta_i + \gamma(\beta_i)\}_i$  for some bounded function  $\gamma$  such that  $|\gamma| \ll 1$ . Subsequent demand  $D_t$  evaluated at  $(\hat{p}, F, T)$  reads

$$D_t(\hat{p}, F, T) = \int_0^{\bar{\beta}} \int_{\alpha^+(y_0 + \gamma(y_0))}^{\bar{\alpha}} (y_0 + \gamma(y_0) - (\hat{p} + T)/x) g(x|y_0) h(y_0) dx dy_0,$$

where we omit the arguments in  $\alpha^+$  that are irrelevant for the proof to reduce clutter. Note that for all  $y_0$  we can expand  $\alpha^+$  in powers of  $\gamma$  as follows

$$\alpha^+(y_0 + \gamma(y_0)) = \alpha^+(y_0) + \gamma(y_0) \frac{\partial \alpha^+}{\partial y} \Big|_{y=y_0} + \mathcal{O}(|\gamma(y_0)|^2).$$

Denoting equilibrium demand prior to small cap change by  $D_0$ , one gets

$$\begin{aligned} D_t(\hat{p}, F, T) &= D_0(\hat{p}, F, T) + \int_0^{\bar{\beta}} \int_{\alpha^+(y_0)}^{\bar{\alpha}} \gamma(y_0) g(x|y_0) h(y_0) dx dy_0 \\ &\quad - \int_0^{\bar{\beta}} \int_{\alpha^+(y_0)}^{\alpha^+(y_0) + \gamma(y_0) \frac{\partial \alpha^+}{\partial y} \Big|_{y=y_0}} (y_0 + \gamma(y_0) - (\hat{p} + T)/x) g(x|y_0) h(y_0) dx dy_0 + \mathcal{O}(|\gamma(y_0)|^2). \end{aligned}$$

The last line in the above expression can be approximated by

$$- \int_0^{\bar{\beta}} \gamma(y_0) \frac{\partial \alpha^+}{\partial y} \Big|_{y=y_0} (y_0 - (\hat{p} + T)/\alpha^+(y_0)) g(\alpha^+(y_0)|y_0) h(y_0) dx dy_0 + \mathcal{O}(|\gamma(y_0)|^2),$$

where the approximation becomes exact in the limit as  $|\gamma| \rightarrow 0$ . Further assuming a uniformly distributed cap tightening, i.e.  $\gamma$  is constant and positive,  $\lim_{\gamma \rightarrow 0} (D_t - D_0)/\gamma$  writes

$$\underbrace{\int_0^{\bar{\beta}} \int_{\alpha^+(y_0)}^{\bar{\alpha}} g(x|y_0) h(y_0) dx dy_0}_{\text{intensive margin } \geq 0} - \underbrace{\int_0^{\bar{\beta}} \frac{\partial \alpha^+}{\partial y} \Big|_{y=y_0} (y_0 - (\hat{p} + T)/\alpha^+(y_0)) g(\alpha^+(y_0)|y_0) h(y_0) dx dy_0}_{\text{extensive margin } \geq 0}$$

as  $\lim_{\gamma \rightarrow 0} \mathcal{O}(\gamma) = 0$ . The intensive margin term captures the increase in demand on the part of firms in  $\mathcal{D}$  prior to the tightening. The extensive margin term captures what happens at the  $\mathcal{A}_2$ - $\mathcal{D}$  frontier, i.e. the novel demand on the part of firms exiting  $\mathcal{A}$  and entering  $\mathcal{D}$ . Note again that the extensive margin component drops for any  $T \geq 0$  when  $F = 0$ .

We proceed similarly for  $S$  (computations are longer but follow the same logic). Then, all the terms in  $\lim_{\gamma \rightarrow 0} (V_t - V_0)/\gamma$  can be grouped into two categories, namely

$$\lim_{\gamma \rightarrow 0} (V_t(\hat{p}, F, T) - V_0(\hat{p}, F, T))/\gamma = \underbrace{|\mathcal{I}| - |\mathcal{A}(\hat{p}, F, T)|}_{\text{intensive margin}} + \underbrace{\text{sum of positive terms}}_{\text{extensive margin}} \geq |\mathcal{I}|,$$

where  $|\mathcal{I}| = \lim_{\gamma \rightarrow 0} (V_t(p^*, 0, 0) - V_0(p^*, 0, 0))/\gamma$ . Roughly put, the larger the set of autarkic firms, i.e. the larger the trading costs, the more likely the distribution effect is below one, i.e.  $\lim_{\gamma \rightarrow 0} (V_t(\hat{p}, F, T) - V_0(\hat{p}, F, T))/\gamma < |\mathcal{I}|$  holds. With  $F = 0$ , this holds for all  $T > 0$ .

Finally, we consider alternative distributions of supply tightening in the intensive margin only case treated in the body of the paper. When uniformly distributed among all firms,  $d\beta_i = d\mathcal{Q}$  holds for all  $i \in \mathcal{I}$ . When uniformly targeted on all firms with positive (resp. negative) deficits,  $d\beta_i = d\mathcal{Q}/(|\bar{\mathcal{S}}_3| + |\bar{\mathcal{D}}| + |\bar{\mathcal{A}}_2|) > d\mathcal{Q}$  (resp.  $d\beta_i = d\mathcal{Q}/(|\bar{\mathcal{S}}_1| + |\bar{\mathcal{S}}_2| + |\bar{\mathcal{A}}_1|) > d\mathcal{Q}$ ) holds for all  $i$  with  $\beta_i > 0$  (resp.  $\beta_i < 0$ ) where the sets  $\mathcal{S}_k$  and  $\mathcal{A}_k$  are defined in Figure 3 and the upper bar is a shorthand meaning ‘evaluated at  $(\hat{p}, F, T)$ ’. In these three cases the distribution effect is

$$\begin{aligned} & (|\bar{\mathcal{S}}_1| + |\bar{\mathcal{S}}_2| + |\bar{\mathcal{S}}_3| + |\bar{\mathcal{D}}|)/|\mathcal{I}| < 1, \\ \text{or } & (|\bar{\mathcal{S}}_3| + |\bar{\mathcal{D}}|)/(|\bar{\mathcal{S}}_3| + |\bar{\mathcal{D}}| + |\bar{\mathcal{A}}_2|) < 1, \\ \text{or } & (|\bar{\mathcal{S}}_1| + |\bar{\mathcal{S}}_2|)/(|\bar{\mathcal{S}}_1| + |\bar{\mathcal{S}}_2| + |\bar{\mathcal{A}}_1|) < 1. \end{aligned}$$

The magnitude of the price increase in the face of a given supply tightening thus depends on the way it is allocated among firms. The ranking between the three incidence types presented above is unclear *prima facie*: it hinges on the levels of the trading costs  $F$  and  $T$  and on the distributions of the firms’ characteristics  $\{\alpha_i\}_i$  and  $\{\beta_i\}_i$ .

## B Analytical and numerical examples

### B.1 Analytical examples

After tedious but standard calculus (13) and (14) obtain by solving  $D(p, F, 0) = S(p, F, 0)$  for  $p$  and  $p^*$  solves  $D(p, 0, 0) = S(p, 0, 0)$ . Below we sketch out the key steps of the computations for *Case 1* and omit those for *Case 2* as they follow the same lines. Define function  $J$  by

$$J = \hat{p}_1 + \frac{2F\sqrt{F(F + 2\beta\hat{p}_1)}}{\beta^3(\bar{\alpha} - \alpha)} - p_1^*,$$

which is constant (in specie, nil) according to (13). The implicit function theorem yields

$$\frac{d\hat{p}_1}{dF} = -\frac{\partial J/\partial F}{\partial J/\partial \hat{p}_1} \quad \text{and} \quad \frac{d\hat{p}_1}{d\beta} = -\frac{\partial J/\partial \beta}{\partial J/\partial \hat{p}_1}.$$

One then has  $d\hat{p}_1/dF < 0$  and  $d\hat{p}_1/d\beta > 0$  as it is easy to check that  $\partial J/\partial F > 0$ ,  $\partial J/\partial \hat{p}_1 > 0$  and  $\partial J/\partial \beta < 0$ . In particular, it is convenient to rewrite the second equality above as follows

$$\frac{d\hat{p}_1}{d\beta}(1 + \beta^2 X) = X(3F + 5\beta\hat{p}_1) + \frac{dp_1^*}{d\beta} \text{ with } X = 2F^2 / \left( \beta^4(\bar{\alpha} - \underline{\alpha})\sqrt{F(F + 2\beta\hat{p}_1)} \right) > 0.$$

By linearity of  $p_1^*$  in  $\beta$  we have  $\beta \frac{dp_1^*}{d\beta} = p_1^*$  so that it finally comes

$$\left( \frac{d\hat{p}_1}{d\beta} - \frac{dp_1^*}{d\beta} \right) (1 + \beta X^2) = X(3F + 5\beta\hat{p}_1 - \beta p_1^*) \Rightarrow \frac{d\hat{p}_1}{d\beta} \geq \frac{dp_1^*}{d\beta} \text{ iff } \hat{p}_1 \geq (p_1^* - 3F/\beta)/5.$$

## B.2 Numerical examples

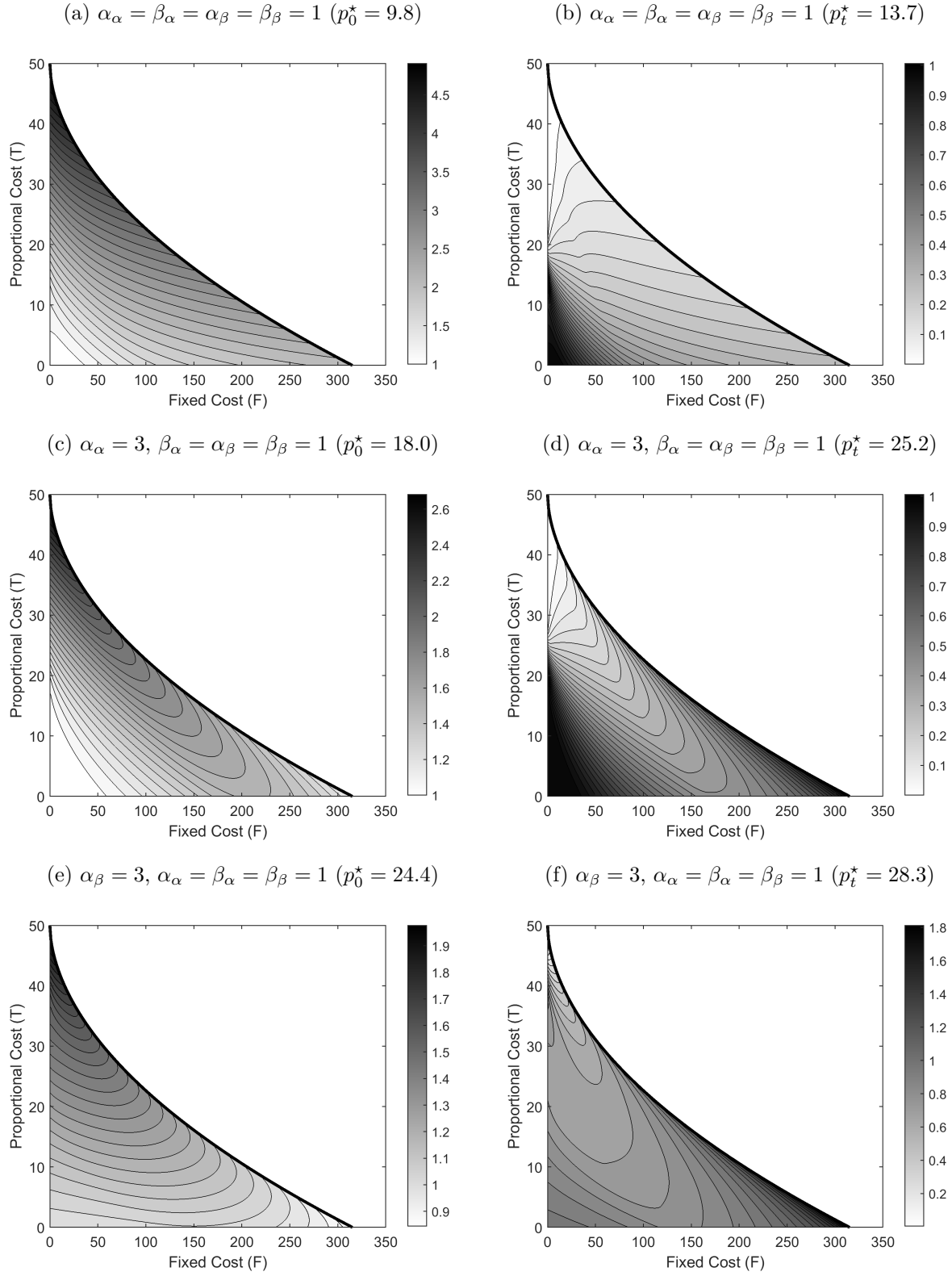
We let  $\{\alpha_i\}_i$  and  $\{\beta_i\}_i$  follow independent beta distributions  $B(\alpha_\alpha, \beta_\alpha)$  and  $B(\alpha_\beta, \beta_\beta)$ . We consider both fixed and proportional trading costs simultaneously and set  $\underline{\alpha} = 1$ ,  $\bar{\alpha} = 10$ ,  $\underline{\beta} = -5$  and  $\bar{\beta} = 10$ . We analyze three cases: both  $\{\alpha_i\}_i$  and  $\{\beta_i\}_i$  uniform (i.e.  $\alpha_\alpha = \alpha_\beta = \beta_\alpha = \beta_\beta = 1$ );  $\{\alpha_i\}_i$  skewed towards high values (i.e.  $\alpha_\alpha = 3$ ,  $\beta_\alpha = 1$ ) with  $\{\beta_i\}_i$  uniform; and  $\{\beta_i\}_i$  skewed towards high values (i.e.  $\alpha_\beta = 3$ ,  $\beta_\beta = 1$ ) with  $\{\alpha_i\}_i$  uniform. The cases where  $\{\alpha_i\}_i$  or  $\{\beta_i\}_i$  are skewed towards low values lead to magnified but qualitatively similar results as for the case of  $\{\alpha_i\}_i$  and  $\{\beta_i\}_i$  both uniform, hence omitted here.

*Price impacts of a change in trading costs.* Given  $F$  and  $T$ , we solve numerically for  $\hat{p}_0$  such that  $V(\hat{p}_0, F, T) = 0$ , jointly verifying the cost admissibility conditions. Specifically, we seek  $\hat{p}_0 = \min p$  such that  $D - S > 0$  and  $\hat{p}_0$  is feasible. The left column in Figure B.1 depicts the ratios  $\hat{p}_0/p_0^*$  in the  $(F, T)$ -space in the three cases with  $V(p_0^*, 0, 0) = 0$ . The thick black line delineates the admissible cost range defined in (8) above which the market breaks down.

With  $\{\alpha_i\}_i$  and  $\{\beta_i\}_i$  both uniform (Figure B.1a) the market price in the presence of trading costs is always larger than absent trading costs ( $\hat{p}_0/p_0^* \geq 1$ ) and it gets larger the larger  $F$  or  $T$  (contour lines are downward-sloping) but increases relatively more with  $T$  than  $F$  (contour lines are convex). For instance,  $\hat{p}_0$  can be five times as large as  $p_0^*$  when  $F = 0$  and  $T$  is large while it is at most twice as large when  $T = 0$  and  $F$  is large. This is no longer so in the other two cases:  $\hat{p}_0$  can be lower than  $p_0^*$  for some trading costs (e.g. when  $F$  is large and  $T$  small in Figure B.1e) and is non-monotonic in the trading costs (i.e. contour lines have distorted U shapes in Figures B.1c and B.1e). In particular,  $\hat{p}_0$  increases with the trading costs when they are ‘low enough’ but the converse holds when they are ‘large enough’.

Generally speaking, we find that the higher the frictionless price to start with, the relatively lower the market price in the presence of trading costs. Moreover, only when the frictionless

Figure B.1: Ratios  $\hat{p}_0/p_0^*$  (left) and  $\frac{\hat{p}_t - \hat{p}_0}{\hat{p}_0} / \frac{p_t^* - p_0^*}{p_0^*}$  (right)



*Note:* The subscript 0 (resp.  $t$ ) indicates the pre (resp. post) supply tightening situation.

price is sufficiently high can trading costs lead to a lower price level for some cost pairs. This relates to the tempering price effect of trading costs mentioned in Section 3.3.1.

*Price impacts of a change in individual allocations.* We illustrate a uniform supply tightening with a shift in the support of the distribution  $\{\beta_i\}_i$  from  $[-5; 10]$  (indexed by 0) to  $[-4; 11]$  (indexed by  $t$ ). The right column in Figure B.1 depicts our results and shows the ratios of the relative induced price increase  $\frac{\hat{p}_t - \hat{p}_0}{\hat{p}_0}$  with trading costs to the relative induced price increase under frictionless conditions  $\frac{p_t^* - p_0^*}{p_0^*}$  in the  $(F, T)$ -space in the three cases considered.

We find that the relative induced price increase in the presence of trading costs is less pronounced the larger  $\hat{p}_0$  relative to  $p_0^*$  to start with. Consequently, it tends to be larger under frictionless conditions than present trading costs most of the time in our simulations. Only in one case do we find that the relative price increase is larger with trading costs than without, namely in Figure B.1f when  $F$  is large and  $\hat{p}_0$  is close to or lower than  $p_0^*$ .

## C Consolidation methodology

Data recorded in the European Union Transaction Log (EUTL) contains both compliance and trading related information (at the account level) in two separate databases: the compliance database keeps track of the initial allocation and reconciliation of allowances; the transaction database records every physical exchange completed across accounts (including the account holder names of trading parties, date and volume traded). There are three main categories of accounts: Operator Holding Accounts (OHAs, one per regulated installation), Person Holding Accounts (PHAs) and Trading Accounts. The latter two can be opened and managed by non-regulated entities with no compliance obligations (e.g. intermediaries, financiers).

These two databases need to be consolidated at the company level – the relevant granularity level for abatement, compliance, trading and wider economic decisions. However, two issues arise when trying to match accounts to parent companies. First, only limited or incomplete information is available on the firms and sectors associated to each account. For instance, no dedicated field in the account characteristics indicates the name of a parent company, when it exists (e.g. account holders must fill an ‘Account Holder Name’ field but it is uneven across accounts as to the precision of company-specific details). Second, there is no key to match the two databases so we need to create our own beforehand.

To get at the ownership structure within the EUTL, we first construct a list of parent company names from the compliance database which we then use as a key to consolidate the trading



Table C.1: Descriptive statistics for consolidated regulated firms (2009 sample)

**Trading firms**

Sector	Number of firms	$\langle$ Number $\rangle$ of accounts	% of total emissions	Median deficit	$\langle$ Number $\rangle$ of transactions	$\langle$ Volume $\rangle$ of transactions
Combustion	872	2.6	71.2	70,654	15.8	39,517
Refining	23	4.0	8.5	72,063	10.9	211,449
Metallurgy	37	3.4	3.2	-114,510	6.8	218,805
Cement & Lime	344	3.1	15.1	-25,474	5.5	34,095
Chemicals	8	3.1	0.2	-11,056	6.1	52,201
Paper & Glass	164	2.6	1.6	-8,272	8.3	23,242
Other	3	6.0	$\approx 0$	-5,600	4.0	1,494

Total number of observations: 1451.

**Autarkic firms**

Sector	Number of firms	$\langle$ Number $\rangle$ of accounts	% of total emissions	Median deficit
Combustion	848	2.3	62.6	3,665
Refining	14	2.1	11.0	267,178
Metallurgy	41	2.0	3.7	-52,835
Cement & Lime	165	2.3	13.6	-7,749
Chemicals	4	2.0	1.2	-13,266
Paper & Glass	217	2.4	8.9	-3,114
Other	1	1.0	$\approx 0$	-11,139

Total number of observations: 1290.

*Note:* Median deficits and average volumes of transactions given in tCO<sub>2</sub>.  $\langle \cdot \rangle$  denotes the average.

information from the transaction database at the company level. To that end, we first clean the ‘Account Holder Name’ fields in the compliance database, totaling about 17,000 accounts over all years. Specifically, we remove punctuation marks, prefixes, suffixes, etc and separate words. We then run a first round of matching for duplicates on the first word the character strings contain, and obtain a first-pass list which associates the so-extracted parent companies to their accounts. We gradually refine the list by repeating this procedure with the second, third and fourth words for the remaining unassigned accounts.

In practice, a company name – when explicitly specified – often appears in the first or second word of the search field so that our simple method allows us to get a reasonably good idea of which company owns which accounts. After the fourth iteration of the matching procedure, around 10% of accounts are single. We manually assign them to a parent company (e.g. with dedicated web searches) and those for which manual matching is unsuccessful remain single. Our final parent company list contains 7,215 entries in total over Phase II (2008-2012).

In parallel, a total of 7,210 accounts recorded some trading activity (at least one exchange) in the transaction database over Phase II, some of which with no compliance obligations. Only

considering compliance entities reduces the transaction database to 5,145 active accounts. This essentially amounts to keeping OHAs, or PHAs opened and run by a regulated company (typically to first pool allocations and later dispatch EUAs for compliance). Figure 1 is based on this select database, where (1) a compliance entity is deemed autarkic if it records no trade with compliance or non-compliance entities alike; (2) year-on-year changes in the number of observations occur due to installation/account closures and new entries as they occur.

We cross-check our consolidation outputs with those in [Jaraitė-Kažukauskė & Kažukauskas \(2015\)](#), [Naegele \(2018\)](#) or [Hintermann & Ludwig \(2018\)](#) who link EUTL accounts to the Orbis database (Bureau van Dijk) to match installations to parent companies. Their methodologies are similar to that underpinning the Ownership Links and Enhanced EUTL Dataset, hosted by the European University Institute. Although we were not aware of this publicly available database linking accounts to parent companies when we started our project, it allows us to perform an ex-post sanity check for our consolidation methodology. Our respective results are found to be similar, e.g. [Naegele](#) finds a close 4,578 firms with her method.

The [Illustration](#) requires us to merge the compliance and transaction databases as we want the allocation, verified emissions and trading activity at the regulated firm level. Because the ‘Account Holder Name’ field is present in both databases, this is in principle straightforward. Due to matching discrepancies, however, the merged database only contains 2,500 entries. It is used to plot Figure 2 but needs further cleaning to be used in the [Illustration](#). Specifically, we exclude firms whose reported information is anomalous (e.g. emissions are nil) or missing (e.g. no allocation nor market position provided). This leads to slight changes in the number of yearly entries. Table C.1 below draws on these datasets. Finally, we remove firms with implied negative abatement and our yearly datasets are ready for use. This leads, again, to slight changes in the number of yearly entries, see Table D.1 for descriptive statistics.

## D Calibration details

This Appendix provides additional calibration details, namely on the model parametrization (Section 4.1.1) and the selection of trading costs (Section 4.1.2). We begin with the reference case (i.e. the case analyzed in the main text) and then provide a sensitivity analysis.

### D.1 Reference case

Table D.1 provides basic descriptive statistics for the annual  $\{\alpha_{i,t}, \beta_{i,t}\}_{i,t}$  imputations.

Table D.1: Annually inferred firms' characteristics (rounded)

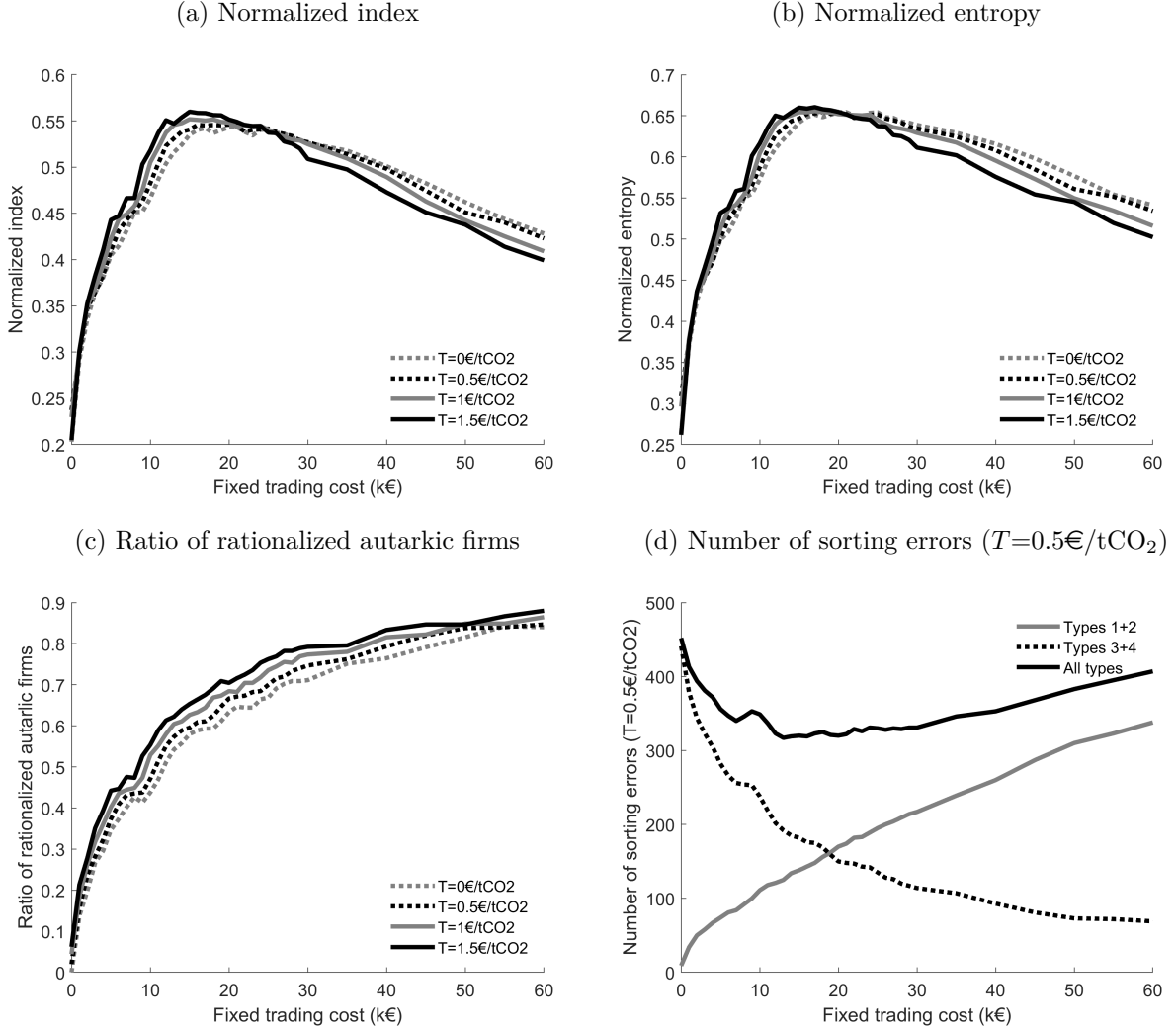
	Year	#Firms	Min	Max	Mean	Median	% Positive
$\alpha$	2008	1,868	$2.1 \cdot 10^{-6}$	59	$9.4 \cdot 10^{-2}$	$7.1 \cdot 10^{-3}$	100
	2009	1,954	$1.3 \cdot 10^{-6}$	13	$2.9 \cdot 10^{-2}$	$3.6 \cdot 10^{-3}$	100
	2010	1,378	$1.6 \cdot 10^{-6}$	43	$7.1 \cdot 10^{-2}$	$5.1 \cdot 10^{-3}$	100
	2011	1,592	$3.8 \cdot 10^{-6}$	11	$5.6 \cdot 10^{-2}$	$5.5 \cdot 10^{-3}$	100
	2012	1,496	$3.4 \cdot 10^{-6}$	22	$4.5 \cdot 10^{-2}$	$3.1 \cdot 10^{-3}$	100
$\beta$	2008	1,868	$-4.0 \cdot 10^6$	$1.9 \cdot 10^7$	$23 \cdot 10^3$	-29	49
	2009	1,954	$-2.8 \cdot 10^6$	$2.2 \cdot 10^7$	$50 \cdot 10^3$	39	51
	2010	1,378	$-7.7 \cdot 10^6$	$1.8 \cdot 10^7$	$17 \cdot 10^3$	-1,100	38
	2011	1,592	$-2.2 \cdot 10^6$	$1.4 \cdot 10^7$	$26 \cdot 10^3$	-320	46
	2012	1,496	$-4.9 \cdot 10^6$	$7.5 \cdot 10^6$	$30 \cdot 10^3$	810	59

Note:  $\alpha$  given in  $\text{€}/(\text{tCO}_2)^2$  for  $T = 0$ .  $\beta$  given in  $\text{tCO}_2$ , not adjusted for year-on-year bank variations.

Figure D.1 graphically depicts how our cost selection criteria evolve with  $F$  and  $T$  for the year 2009. In Figure D.1d we see that as  $F$  increases the number of observed autarkic firms sorted as autarkic by the model increases, i.e. the number of type 3-4 errors decreases (similarly, in Figure D.1c, the number of rationalized autarkic decisions is ranked by increasing  $F$  and  $T$  values). Simultaneously, however, a larger  $F$  also implies that the model sorts more observed active firms as autarkic, i.e. the number of type 1-2 errors increases. As a result, the overall number of sorting errors is U-shaped and minimal at the  $F$ -value where the grey and dotted lines intersect. By the same token, for a given  $T$ , Shannon's entropy has an inverted U shape and is maximal in the vicinity of the same  $F$ -value (Figure D.1b) as the distribution of errors among error types is most balanced there. Thus, since the total number of errors is relatively more stable, the index behavior in Figure D.1a is chiefly driven by its entropy component. As mentioned in Section 4.1.2, the number of type 5-6 errors is negligible compared to that of type 1-4 errors, hence not depicted in Figure D.1d. Specifically,  $|\mathcal{E}_5|$  and  $|\mathcal{E}_6|$  become nil for small positive values of  $F$  and  $T$ .

Table D.2 provides the calibration results for all years in Phase II with sensitivity intervals for selected  $F$ ,  $T$  and  $\eta_t$  values in three neighborhoods of the index's maximum (denoted by a  $\star$ ) of relative sizes of 1, 2 and 5%. First, we note that the  $\eta_t$ 's are significantly larger than 0 in 2008 and 2010, for all trading cost values, respectively representing 21 and 56% of the annual permit price (compared to 2–4% in 2009, 2011, and 2012). This shows the limits of our static model and parametrization to capture all relevant factors for market outcomes. In 2010, for instance, the  $\eta$ -value implies that a significant upward shift in the firms' initial permit deficits is necessary to reproduce observed price levels. This can be explained by the

Figure D.1: Selection criteria as functions of  $F$  and  $T$  (2009 sample)



economic downturn which dramatically decreased emissions in the three preceding years and thus our proxy for 2010 baseline emissions.

Second, we briefly turn to the robustness of the selected trading cost values. The sensitivity intervals indicate which  $F$  and  $T$  values achieve a similar improvement in replicating observed firms' behavior as measured by the index in (23). We observe a greater dispersion for  $T$  than for  $F$  around the index's maximum. As Figure D.1 illustrates, this is because  $F$  weighs more heavily on our calibration criteria, notably as it is more instrumental than  $T$  to rationalize autarkic decisions (especially for overallocated firms). Thus, around the index's maximum in Figure D.1a, the feasible values for  $T$  can be fuzzier (i.e. subject to more variability) than those for  $F$ . For instance, note this reversal: for  $F$  low (resp. high) enough, index values are ranked by increasing (resp. decreasing)  $T$ -values. Moreover, because of the discrete nature

Table D.2: Detailed calibration results (reference case,  $\theta = 0.5$ )

	SI	$F$	$T$	$\eta_t$
2008	★	10	0.6	4.01
	1%	[10;12]	[0.3;0.6]	[3.92;4.01]
	2%	[9;13]	[0.3;0.7]	[3.92;4.01]
	5%	[9;15]	[0.2;0.7]	[3.88;4.01]
2009	★	18	1.4	-0.31
	1%	[15;19]	[1.3;1.5]	[-0.31;-0.20]
	2%	[10;21]	[1.0;1.8]	[-0.31;-0.19]
	5%	[10;28]	[0.2;2.0]	[-0.35;-0.11]
2010	★	5	0.6	8.09
	1%	[5;6]	[0.5;0.7]	[8.07;8.19]
	2%	[2;7]	[0.4;0.7]	[8.07;8.19]
	5%	[2;8]	[0.4;0.7]	[8.07;8.19]
2011	★	16	1.3	0.36
	1%	[15;16]	[1.1;1.6]	[0.23;0.41]
	2%	[15;19]	[0.5;1.6]	[0.20;0.41]
	5%	[14;29]	[0.3;1.6]	[0.16;0.52]
2012	★	8	0.6	0.26
	1%	[7;9]	[0.3;0.8]	[0.26;0.32]
	2%	[7;9]	[0.1;0.8]	[0.26;0.32]
	5%	[5;12]	[0.1;0.8]	[0.25;0.36]

Note:  $\eta_t$  and  $T$  given in €/tCO<sub>2</sub>.  $F$  given in k€. SI = sensitivity interval, ★ = index's maximum.

of our problem, the index can be locally non-concave, potentially implying some additional fuzziness in the selected cost values.

## D.2 Sensitivity analysis

We now discuss the sensitivity of our calibration results to the way we adjust autarkic firms' allocations for banking and borrowing in (22), i.e.  $q_{i,t}^a = q_{i,t}^r - \theta(b_{i,t}^r - b_{i,t-1}^r) = (1 - \theta)q_{i,t}^r + \theta e_{i,t}^r$  where  $\theta \in [0; 1]$  is a preference parameter for the market's temporal vs. spatial dimension, which our static model does not explicitly account for. Specifically, when  $\theta$  is close to one, long (resp. short) firms prefer to bank (resp. borrow) the entirety of their annual surplus (resp. shortage). Conversely, when  $\theta$  is close to zero, long (resp. short) firms prefer to sell (resp. buy) the entirety of their annual surplus (resp. shortage) in the market.

Because of a lack of empirical guidance, we assume  $\theta = 0.5$  in the reference case in Section

Table D.3: Detailed calibration results ( $\theta$ -sensitivity)

		$\theta = 0.4$			$\theta = 0.6$		
	SI	$F$	$T$	$\eta_t$	$F$	$T$	$\eta_t$
2009	$\star$	22	2.2	-1.25	14	0.3	0.86
	1%	[18;36]	[1.5;2.3]	[-1.31;-1.13]	[13;18]	[0.2;1.1]	[0.76;0.88]
	2%	[17;39]	[0.6;2.4]	[-1.31;-1.13]	[10;20]	[0.1;1.9]	[0.76;1.09]
	5%	[14;44]	[0.1;2.5]	[-1.31;-1.11]	[10;25]	[0.1;2.0]	[0.76;1.09]
2012	$\star$	7	1.8	-0.20	1	0.2	0.66
	1%	[6;8]	[0.6;1.9]	[-0.20;-0.15]	[1;2]	[0.1;0.4]	[0.66;0.76]
	2%	[4;11]	[0.3;2.0]	[-0.20;-0.06]	[1;2]	[0.1;0.4]	[0.66;0.76]
	5%	[3;15]	[0.1;2.1]	[-0.20;-0.04]	[1;3]	[0.1;0.5]	[0.65;0.78]

Note:  $\eta_t$  and  $T$  given in €/tCO<sub>2</sub>.  $F$  given in k€. SI = sensitivity interval,  $\star$  = index's maximum.

4.1.1. That is, half of the observed autarkic long firms' surplus is in principle available for trading while short firms have to cover their shortage with permit purchases or abatement. For instance, [Martin et al. \(2015\)](#) noticed that firms are willing to sell part of their surplus permits only in excess of some threshold. Additionally, in Section 5 we discuss the interactions between the market's temporal and spatial dimensions when inter-firm trading is costly. Were it not for trading costs, autarkic firms could otherwise increase profits by trading rather than exclusively exploiting the temporal flexibility margin of the scheme.

By construction, our calibration results in Section 4.1.2 depend on the chosen  $\theta$ -value, notably because we introduce trading costs to rationalize autarkic decisions. Intuitively, the larger  $\theta$ , the lower the selected trading costs should be (e.g. when  $\theta = 1$  there is no autarkic decision left to rationalize). Table D.3 reports calibration results for  $\theta = 0.4$  and  $0.6$  in 2009 and 2012 compared to the reference case with  $\theta = 0.5$  in Table D.2.

The changes in selected trading cost values and sensitivity intervals conform with intuition. In terms of sensitivity, the selected  $F$ -values are rather stable (except in 2012 with  $\theta = 0.6$ ) while, as could be expected from Section D.1, the selected  $T$ -values are more dispersed with larger sensitivity intervals. We also note that a lower  $\theta$  entails a lower  $\eta_t$ . Indeed, because of an overall bank build-up in Phase II, a lower  $\theta$  implies more surplus permits up for grabs in the market, hence a lower  $\eta_t$  is needed for our static model to replicate the annual price  $p_t^r$ .